## Mining Behavior Patterns in Streaming Multivariate Data

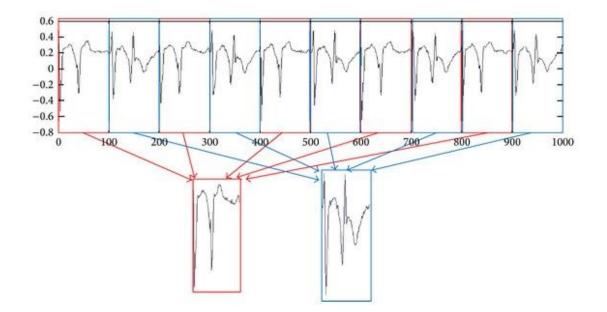
#### Klaus Mueller and Wei Xu

Visual Analytics and Imaging Lab Computer Science Department Stony Brook University

Computational Science Initiative Brookhaven National Laboratory

## What's a Behavior Pattern?

#### A salient subsequence in a time series



- can be clustered and mined
- can be treated as a motif and associated with a scalar ID
- the scalar ID then becomes a scalar data point

## What's a Multivariate Behavior Pattern?

#### Really just a simultaneous set of such patterns

1 MAMM miningannininininannannannininini mannam Monteringhamman 2 MMMMMM 31 5 11 6 M ~ 8 10 ^ 17 P7 11 P7-01 12 13MNF8-T8 14 1 T8-P8 15 2 16 ^ 17 TRANK 18 V

# What's a Multivariate Behavior Pattern?

#### Really just a simultaneous set of such patterns

- can be clustered and mined
- can be treated as motif and associated with a scalar ID
- the scalar ID then becomes a <u>multivariate</u> data point

# Similarity Functions

#### Important metric

- Manhattan (L1)
- Euclidian (L2)
- cosine
- correlation
- structural



$$SSIM(xy) = \left[\frac{2\mu_x\mu_y + c_1}{\mu_x^2 + \mu_y^2 + c_1}\right]^{\alpha} \cdot \left[\frac{2\sigma_x\sigma_y + c_2}{\sigma_x^2 + \sigma_y^2 + c_2}\right]^{\beta} \cdot \left[\frac{\sigma_{xy} + c_3}{\sigma_x\sigma_y + c_3}\right]^{\gamma}$$
  
Iuminance contrast structure

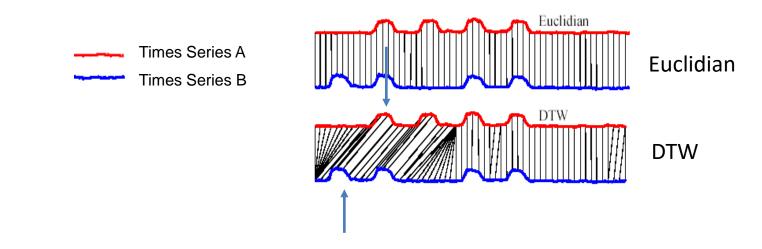
domain-specific features

## How About Sub Seq Window Size?

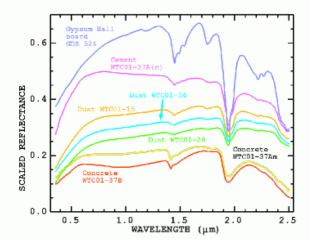
#### Can be found via

- optimization from prior samples
- possibly involving the users
- detect periodicity via wavelets and Fourier analysis

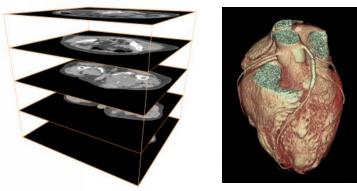
Use DTW (Dynamic Time Warping) to align two sub sequences of possibly unequal lenghth



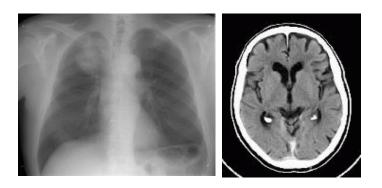
### How To Visualize? 1-3 D Data



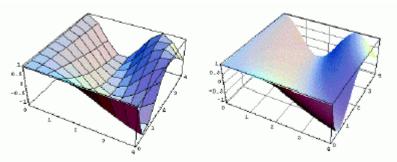
1D signal f(x)



3D signal f(x, y, z)



2D signal f(x, y)



2D signal, shown as height field

4D signal *f*(*x*, *y*, *z*, *t*=time) example: 3D heart in motion

## How About Multivariate Data?

#### Consider the salient features of a car (not really big data):

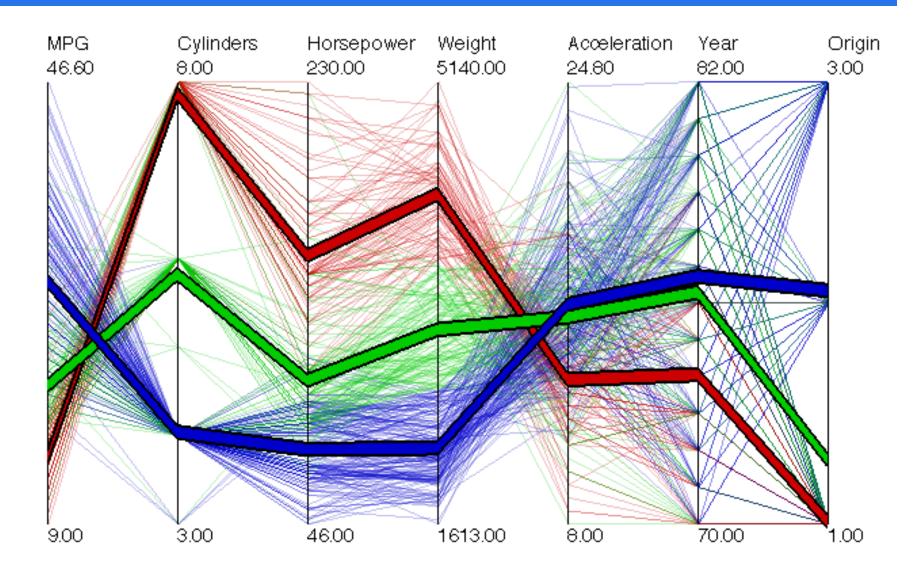
- miles per gallon (MPG)
- top speed
- acceleration
- number of cylinders
- horsepower
- weight
- year
- country origin
- brand
- number of seats
- number of doors
- reliability (average number of breakdowns)
- and so on...

### Can You See Patterns in a Spreadsheet?

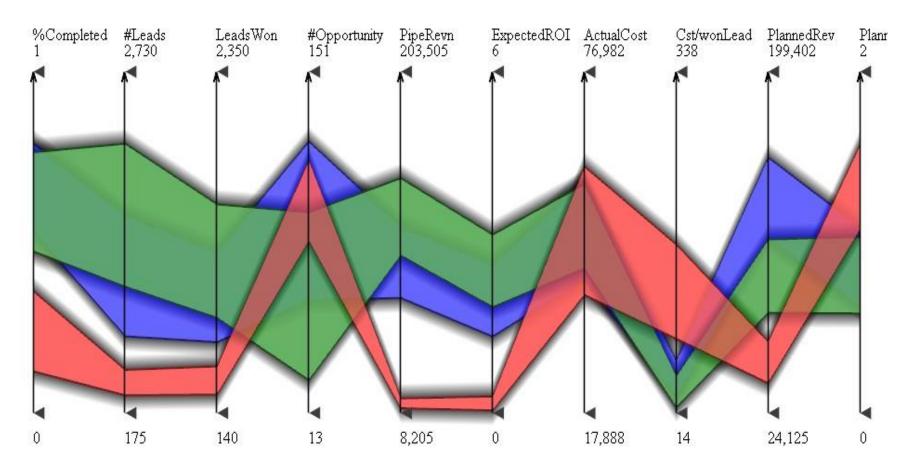
| A                       | В        | С        | D        | E        | F          | G              | Н        | 1   | 1        | K        | Í.       | M        | N         | 0        | Р        |
|-------------------------|----------|----------|----------|----------|------------|----------------|----------|---|----------|----------|----------|----------|-----------|----------|----------|
| 1 Urban population      | 1960     | 1961     | 1962     | 1963     | 1964       | 1965           | 1966     | 1967  | 1968     | 1969     | 1970     | 1971     | 1972      | 1973     | 1974     |
| 2 Afghanistan           | 769308   | 811389   | 855131   | 900646   | 948060     | 997499         | 1053104  | 1110728   | 1170961  | 1234664  | 1302370  | 1391081  | 1483942   | 1579748  | 167665   |
| 3 Albania               | 494443   | 511637   | 529182   | 547024   | 565117     | 583422         | 601897   | 620508  | 639234   | 658062   | 676985   | 698179   | 719561    | 741149   | 76297    |
| 4 Algeria               | 3293999  | 3513320  | 3737362  | 3969886  | 4216744    | 4483048        | 4644898  | 4822860   | 5015071  | 5218184  | 5429743  | 5618190  | 5813978   | 6017932  | 623138   |
| 5 American Samoa        |          |          |          |          |            |                |          |   |          |          |          |          |           |          |          |
| 6 Andorra               |          |          |          |          | -3         |                |          |   |          | -22      |          |          |           |          |          |
| 7 Angola                | 521205   | 552777   | 585121   | 618345   | 652638     | 688181         | 729595   | 772643  | 817418   | 863993   | 912486   | 982944   | 1056617   | 1133936  | 121543   |
| 8 Antigua and Barbuda   | 21699    | 21737    | 21878    | 22086    | 22309      | 22513          | 22717    | 22893   | 23053    | 23218    | 23394    | 24046    | 24718     | 25342    | 2582     |
| 9 Argentina             | 15224096 | 15588864 | 15957125 | 16328045 | 16700303   | 17073371       | 17432905 | 17793789  | 18160868 | 18540720 | 18938137 | 19335571 | 19750609  | 20180707 | 20621674 |
| 10 Armenia              | 957974   | 1008899  | 1061551  | 1115546  | 1170414    | 1225785        | 1281346  | 1337060   | 1393199  | 1450241  | 1508526  | 1565054  | 1622558   | 1680709  | 173901   |
| 11 Aruba                | 24996    | 25514    | 26019    | 26498    | 26941      | 27337          | 27683    | 27984   | 28247    | 28491    | 28726    | 28959    | 29188     | 29409    | 29610    |
| 12 Australia            | 8375329  | 8585577  | 8840666  | 9055650  | 9279777    | 9508980        | 9770529  | 9937118   | 10157212 | 10416192 | 10668471 | 11050785 | 11271606  | 11461308 | 11771589 |
| 13 Austria              | 4560057  | 4589541  | 4621666  | 4653194  | 4685421    | 4715750        | 4754585  | 4778506   | 4798552  | 4817322  | 4849178  | 4871380  | 4904030   | 4932109  | 4939293  |
| 14 Azerbaijan           | 1857673  | 1929429  | 2004258  | 2080816  | 2157307    | 2232355        | 2306310  | 2378380   | 2448728  | 2517815  | 2586000  | 2660687  | 2734631   | 2807879  | 288049   |
| 15 Bahamas              | 65457    | 69655    | 74179    | 78961    | 83902      | 88918          | 93931    | 98974   | 103944   | 108721   | 113219   | 117339   | 121142    | 124761   | 128393   |
| 16 Bahrain              | 128480   | 133815   | 139791   | 146052   | 152097     | 157596         | 162844   | 167630  | 172373   | 177677   | 183997   | 191379   | 199768    | 209201   | 21967    |
| 17 Bangladesh           | 2761049  | 2947191  | 3141372  | 3344120  | 3556037    | 3777716        | 4047121  | 4329144   | 4624445  | 4933701  | 5257558  | 5710277  | 6184871   | 6682073  | 720250   |
| 18 Barbados             | 84884    | 85284    | 85761    | 86285    | 86797      | 87259          | 87707    | 88117   | 88526    | 88986    | 89532    | 90518    | 91596     | 92713    | 9379     |
| 19 Belarus              | 2656152  | 2774166  | 2896449  | 3022217  | 3150553    | 3280410        | 3415984  | 3554673   | 3695363  | 3836802  | 3977600  | 4131179  | 4285735   | 4439788  | 459170   |
| 20 Belgium              | 8435075  | 8489549  | 8548773  | 8620194  | 8709437    | 8796088        | 8865259  | 8924327   | 8968568  | 9003536  | 9040444  | 9086816  | 9134227   | 9175144  | 921708   |
| 21 Belize               | 49165    | 50608    | 52156    | 53734    | 55226      | 56561          | 57756    | 58820   | 59746    | 60532    | 61186    | 61883    | 62445     | 62984    | 6366     |
| 22 Benin                | 211033   | 229172   | 248065   | 267765   | 288321     | 309788         | 337282   | 366019  | 396065   | 427482   | 460341   | 500355   | 542251    | 586179   | 63232    |
| 23 Bermuda              | 44400    | 45500    | 46600    | 47700    | 48900      | 50100          | 51000    | 52000   | 53000    | 54000    | 55000    | 54600    | 54200     | 53800    | 5340     |
| 24 Bhutan               | 8064     | 8778     | 9526     | 10311    | 11137      | 12010          | 13089    | 14230   | 15445    | 16750    | 18158    | 19926    | 21827     | 23858    | 2600     |
| 25 Bolivia              | 1233398  | 1271250  | 1310294  | 1350615  | 1392328    | 1435536        | 1480255  | 1526529   | 1574517  | 1624419  | 1676370  | 1730434  | 1786553   | 1844596  | 1904355  |
| 26 Bosnia and Herzegovi | 604204   | 637337   | 671124   | 705395   | 739884     | 774380         | 812856   | 851325  | 890011   | 929301   | 969514   | 1008688  | 1048890   | 1089898  | 113131   |
| 27 Botswana             | 16240    | 17379    | 18583    | 19855    | 21203      | 22631          | 28191    | 34090   | 40352    | 46995    | 54038    | 61638    | 69689     | 78254    | 87422    |
| 28 Brazil               | 32662018 | 34463344 | 36353068 | 38320171 | 40346703   | 42418482       | 44548227 | 46722996  | 48945984 | 51223962 | 53563179 | 56042505 | 58587770  | 61207586 | 6391338  |
| 29 Brunei               | 35501    | 38753    | 42173    | 45802    | 49699      | 53916          | 58461    | 63355   | 68595    | 74157    | 80024    | 83802    | 87671     | 91616    | 9562     |
| 30 Bulgaria             | 2918659  | 3085061  | 3251675  | 3418610  | 3588246    | 3756058        | 3889518  | 4022040   | 4159890  | 4301340  | 4440270  | 4554810  | 4667059   | 4782931  | 490710   |
| 31 Burkina Faso         | 221872   | 230199   | 238713   | 247472   | 256558     | 266039         | 275958   | 286311  | 297074   | 308196   | 319642   | 332556   | 345877    | 359655   | 37396    |
| 32 Burundi              | 58810    | 61055    | 63344    | 65696    | 68137      | 70683          | 73370    | 76186   | 79034    | 81779    | 84324    | 90879    | 97308     | 103757   | 11049    |
| 33 Cambodia             | 559631   | 578678   | 598248   | 618631   | 640243     | 663272         | 747219   | 835638  | 927177   | 1019449  | 1110079  | 962037   | 806676    | 645287   | 47963    |
| 34 Cameroon             | 751711   | 801009   | 852578   | 906523   | 962928     | 1021891        | 1088521  | 1158289   | 1231375  | 1307967  | 1388275  | 1522958  | 1664410   | 1813278  | 197038   |
| 35 Canada               | 12375125 | 12764121 | 13145207 | 13536503 | 13941055   | 14345262       | 14727261 | 15108962  | 15470875 | 15800439 | 16142268 | 16381341 | 16640381  | 16920220 | 1722176  |
| 36 Cape Verde           | 32791    | 34353    | 35972    | 37672    | 39487      | 41435          | 43592    | 45884   | 48200    | 50383    | 52314    | 54103    | 55620     | 56940    | 5818     |
| 37 Cayman Islands       | -        | -        |          |          | 1000000000 | to provide the |          | in and in the second | -        |          |          |          | 100000000 | -        |          |
| 38 Central African Rep. | 302157   | 317715   | 333986   | 351001   | 368787     | 387357         | 408129   | 429825  | 452326   | 475441   | 499036   | 526414   | 554452    | 583376   | 61353    |
| 39 Chad                 | 198777   | 213406   | 228652   | 244499   | 260903     | 277834         | 305390   | 333898  | 363523   | 394530   | 427153   | 467662   | 510348    | 554973   | 60104    |
| 40 Channel Islands      | 42565    | 42665    | 42792    | 42941    | 43102      | 43269          | 43437    | 43604   | 43765    | 43916    | 44051    | 44028    | 43987     | 43907    | 4376     |

Very hard....

### Method 1: Parallel Coordinates

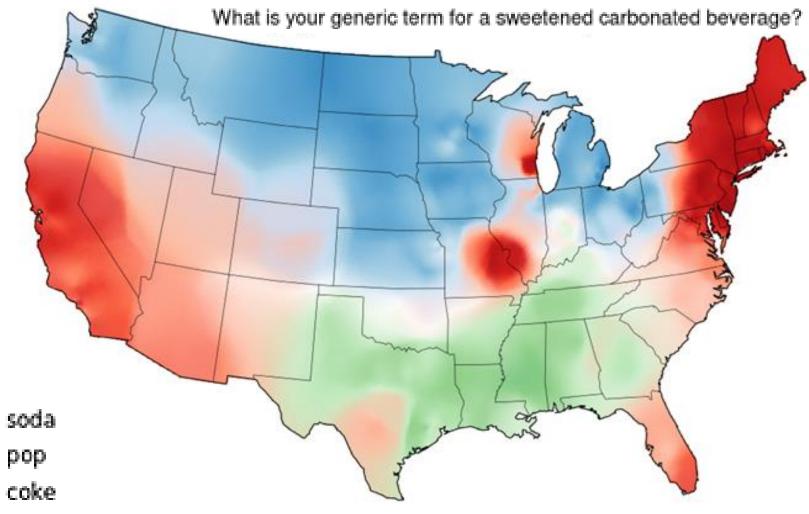


### PC With Illustrative Abstraction



all put together – three clusters

## Method 2: How About A Map?



soft drink

# Data Map Via Space Embedding

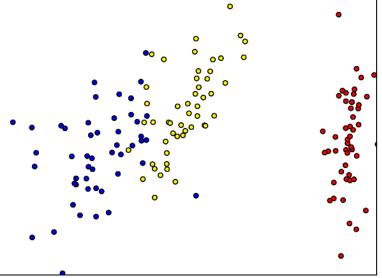
General idea:

- preserve N-D space distances δ<sub>ii</sub> in 2-D space d<sub>ii</sub>
- comes to down to an optimization problem
- minimize

$$stress = \sqrt{\frac{\sum_{ij} (d_{ij} - \delta_{ij})^2}{\sum_{ij} \delta_{ij}^2}}$$

- Multi-Dimensional Scaling (MDS)
- similar data map to similar places
  → Similarity Map





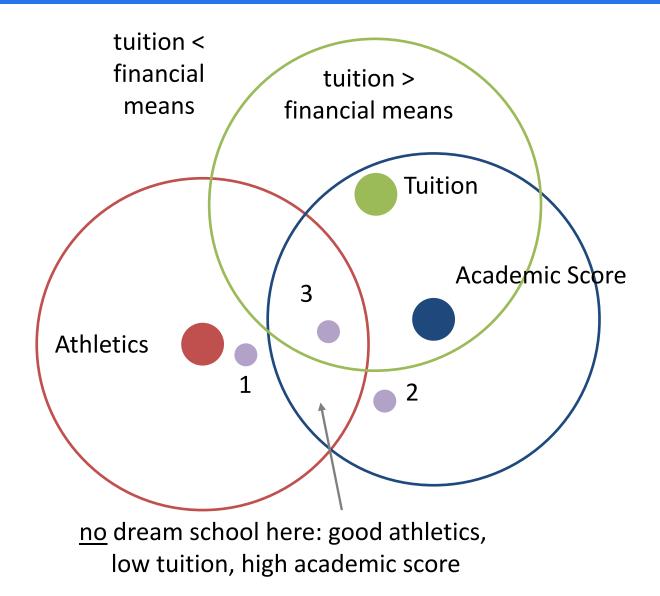
But....



### ... are these clusters so different?

## We Need to Map The Attributes, Too

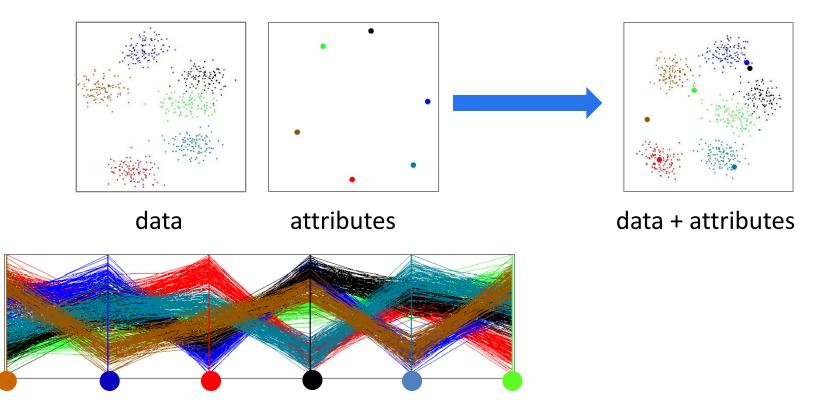
#### Example College Selection



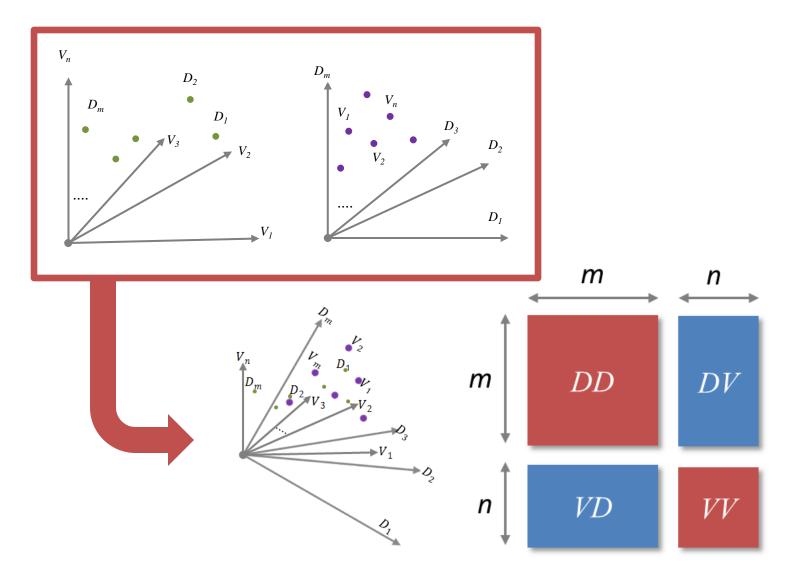
## The Data Context Map

#### Best of both worlds

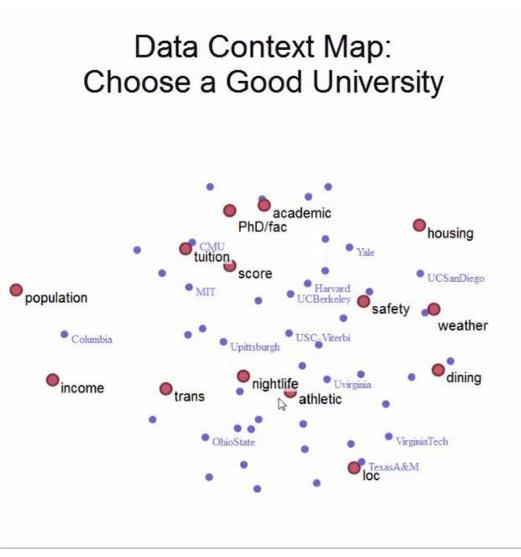
- similarity layout of the data based on vector similarity
- similarity layout of the attributes based on pairwise correlation



## Achieved by Joint Matrix Optimization



### The Data Context Map



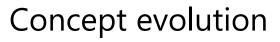
| academic   | 7     | 12      |
|------------|-------|---------|
| athletic   | 0     | 12      |
| housing    | 4     | 12      |
| loc        | 1     | 12      |
| nightlife  | 3     |         |
| safety     | 4     | 11      |
| trans      | 2     | 12      |
| weather    | 2     | 12      |
| score      | 0     |         |
| tuition    | 8712  | 37110   |
| dining     | 4     | 12      |
| PhD/fac    | 0.8   |         |
| population | 13315 | 8274527 |
| income     | 0     | 188697  |

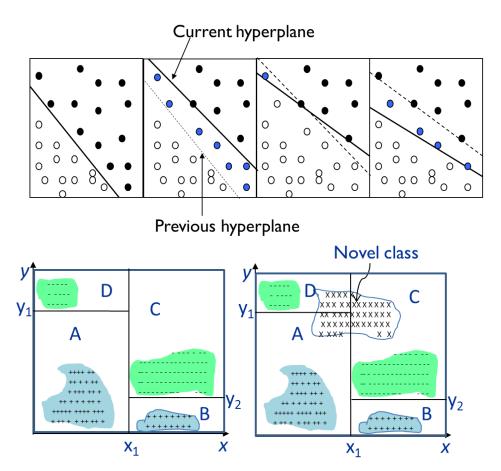
## Streaming Data

#### **One-pass constraint**

data can be processed only once and not all be stored

Concept drift



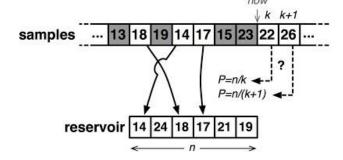


# Synopsis

Keep representative samples as a synopsis

Simplest form is reservoir sampling

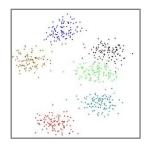
- purely probabilistic and sample-based
- p (sample in reservoir) is k/n

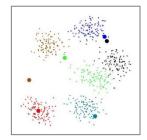


More informative is to evolve clusters (not samples)

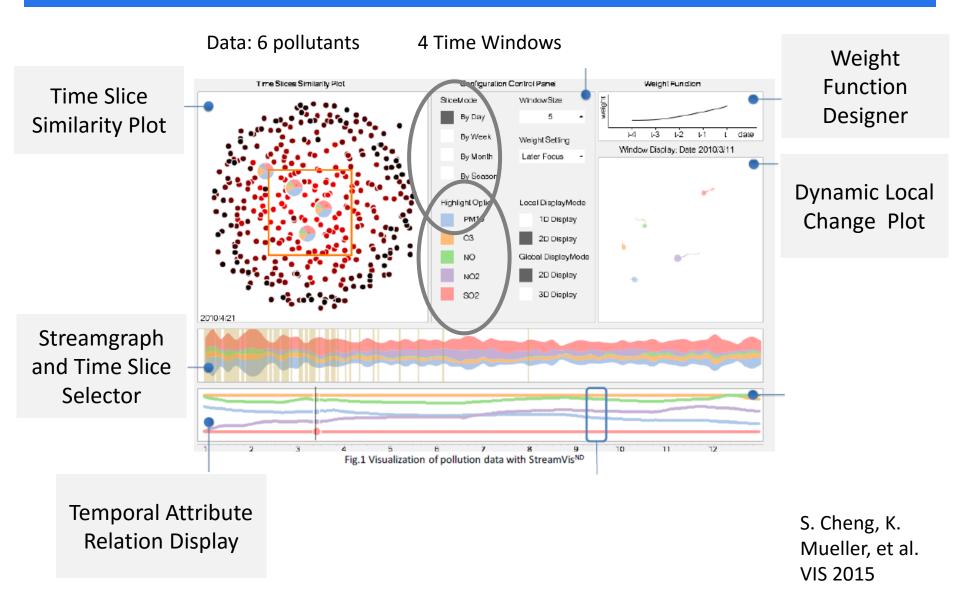
- more apt to keep up with concept drift and evolution
- add new samples and remove stale samples
- update clusters by merging, splitting, or removal
- maintain anomalies

Extend data context map into a synopsis context map





#### STREAMVISND



## More Detail? Visit my Webpage...



<u>http://www.cs.stonybrook.edu/~mueller</u> (for videos see dedicated paper web pages) <u>http://nd-scope.net</u> Any questions?