

# Nature of Exotic Mesons and Detection Methods

Adam Szczepaniak<sup>1</sup>, Misha Mikhasenko<sup>2,3</sup>,  
for the JPAC collaborations

<sup>1</sup>Indiana University/Jefferson Lab

<sup>2</sup>Universität Bonn, HISKP, Bonn, Germany, <sup>3</sup>COMPASS

LHCb meeting

17.07.2017

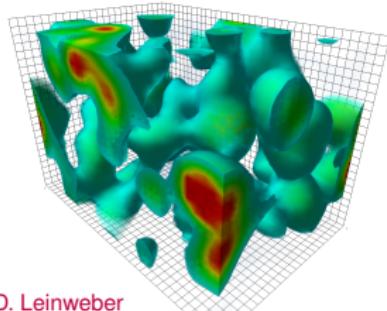


# Overview

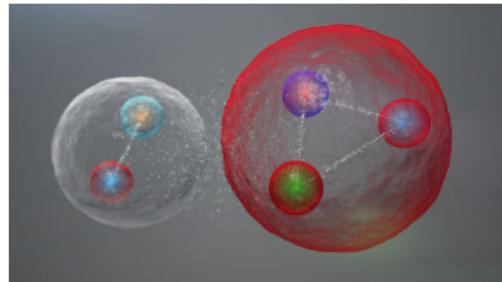
- 1 Hadrons as laboratory for QCD
  - Effective gluons
- 2 Hybrids: expectations
  - Lattice results
  - Experimental results
- 3 How to identify them. Amplitude analysis
  - Resonance pole positions
  - Thresholds

# Why spectroscopy

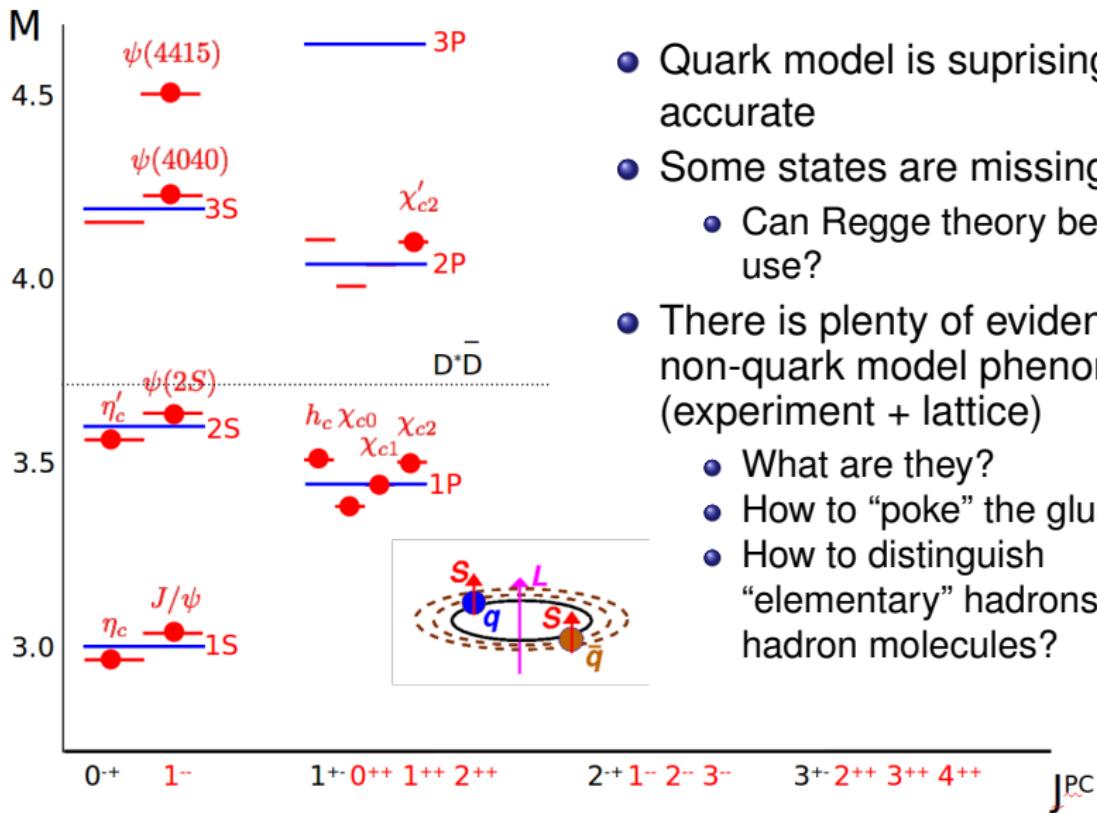
$$\begin{aligned} \mathcal{L} = & -\frac{1}{4} F_{\mu\nu} F^{\mu\nu} \\ & + i \bar{\psi} \gamma^\mu \psi + h.c. \\ & + \bar{\psi}_i y_{ij} \psi_j \phi + h.c. \\ & + D_\mu \phi^\dagger - V(\phi) \end{aligned}$$



- Gluons are responsible for the mass generation and the color confinement
- States of matter dominated by radiation: glueballs, hybrids
- Quarks and gluons are not realized in the nature.
- Hadrons are the basic excitations of the QCD condensed matter (the vacuum)**

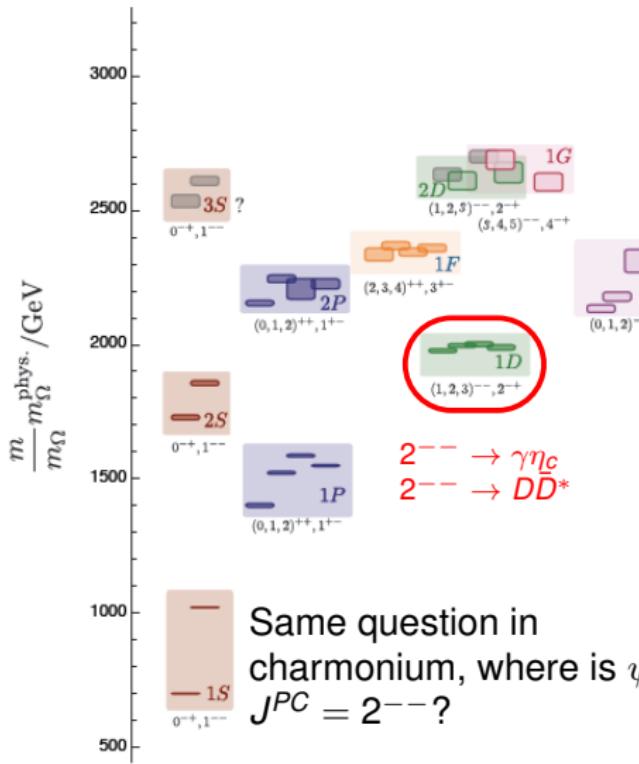


# Quark model



- Quark model is surprisingly accurate
- Some states are missing
  - Can Regge theory be of use?
- There is plenty of evidence of non-quark model phenomenon (experiment + lattice)
  - What are they?
  - How to “poke” the glue?
  - How to distinguish “elementary” hadrons from hadron molecules?

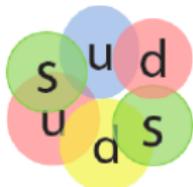
# Lattice results and Regge trajectories



$J^G$	naturality $= P(-1)^J$	twist $= +1$ if $J=0, 2, \dots$ $= -1$ if $J=1, 3, \dots$	name
0+	+1	+1	$f_0, f_2, \dots$
0+	+1	-1	$\eta/\eta', \eta/\eta' \dots (1^+, 3^+, \dots)$
0+	-1	+1	$\eta/\eta', \eta/\eta' \dots$
0+	-1	-1	$f_1, f_3, \dots$
0-	+1	+1	$h_0, h_2, \dots (0^-, 2^+, \dots)$
0-	+1	-1	$\omega/\phi_1, \omega/\phi_3, \dots$
0-	-1	+1	$\omega/\phi_0, \omega/\phi_2, \dots (0^-, 2^-, \dots \text{not seen})$
0-	-1	-1	$b_1, b_3, \dots$
1+	+1	+1	$b_0, b_2, \dots (0^-, 2^+, \dots)$
1+	+1	-1	$\rho_1, \rho_3, \dots$
1+	-1	+1	$\rho_0, \rho_2, \dots (0^-, 2^-, \dots \text{not seen})$
1+	-1	-1	$b_1, b_3, \dots$
1-	+1	+1	$a_0, a_2, \dots$
1-	+1	-1	$m_1, m_3, \dots (1^+, 3^+, \dots)$
1-	-1	+1	$\Gamma_1, \Gamma_2, \dots$
1-	-1	-1	$a_1, a_3, \dots$

# Hadrons beyond the quark model

QCD: There are many other possible color singlets.



dibaryon



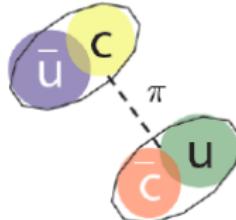
pentaquark



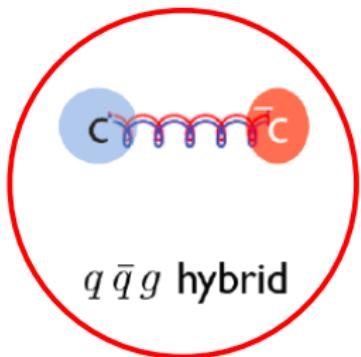
glueball



diquark + di-antiquark



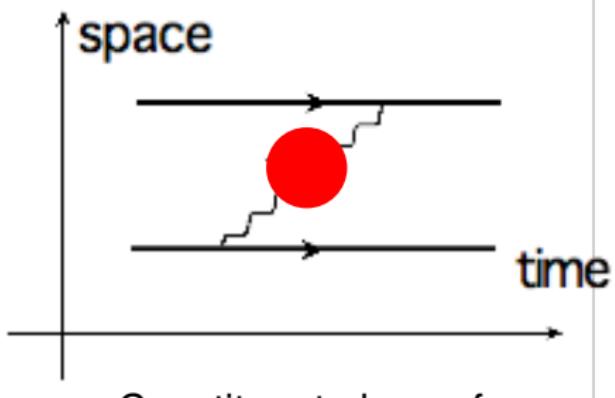
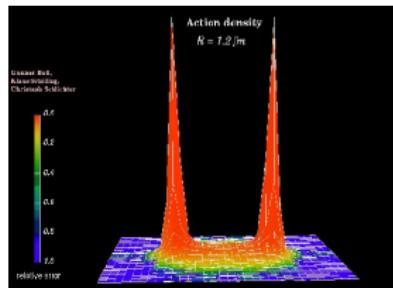
dimeson molecule



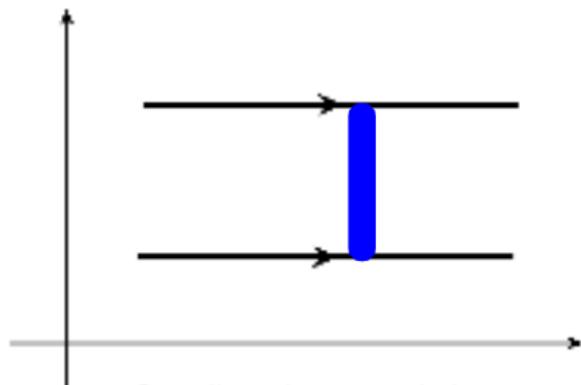
$q \bar{q} g$  hybrid

# Confining and confined gluons

- provide confinement  $\Rightarrow$  long range correlations
- are confined  $\Rightarrow$  short range correlations



Constituent gluon of  
large effective mass

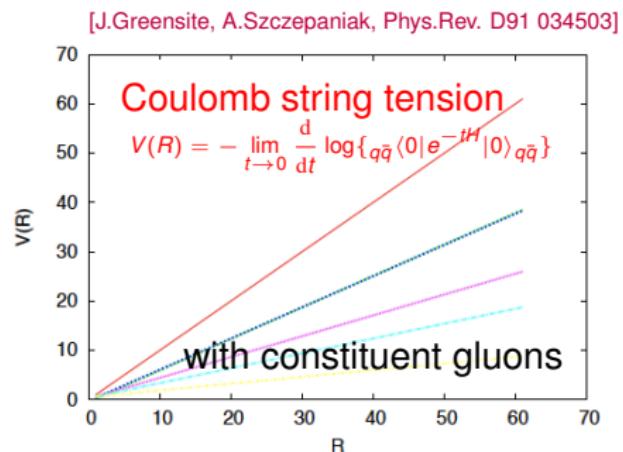
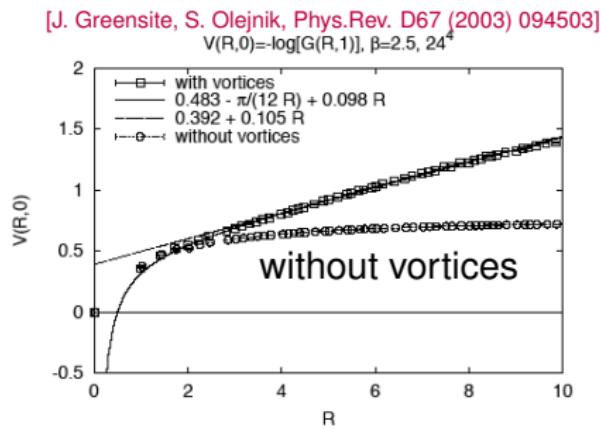


Confined potential  
between external sources

# Some hints from the classical theory

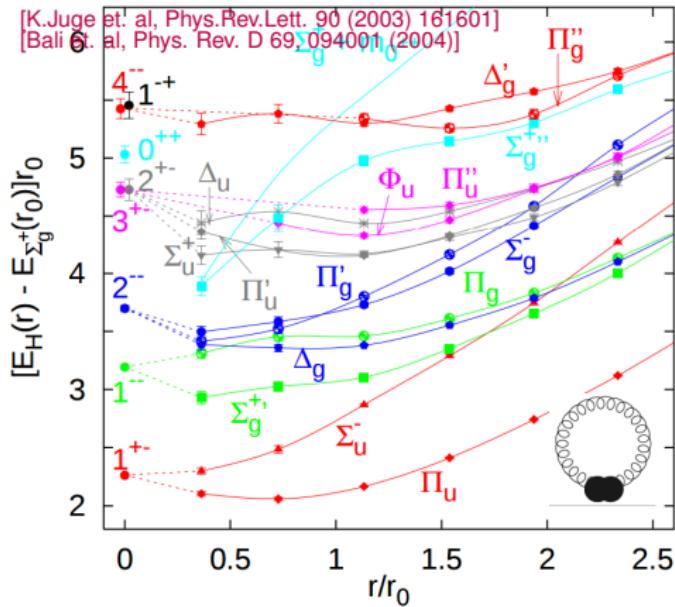
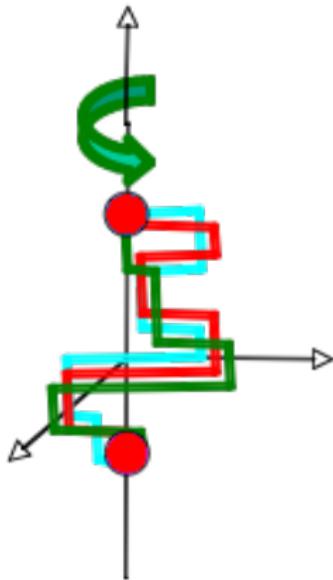
QCD hamiltonian approach,

- slope of the confining potential



- Physical quarks appear to move in a gluon mean field
- The condensate can be excited leading to effective (constituent) gluons

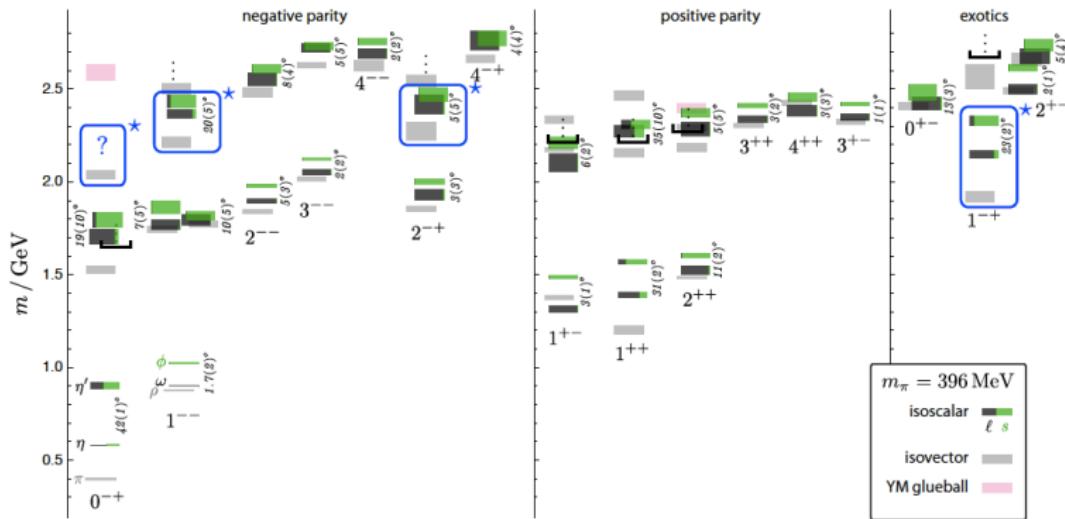
# Static $q\bar{q}$ pair as a diatomic molecule



- Three-body forces are responsible for the energy level inversion
- Gluons behave as quasiparticles with  $J^{PC} = 1^{+-}$

[P.Krupinski, A.Szczepaniak, Phys.Rev. D73 (2006) 116002]

# Constituent gluons lead to the hybrid multiplets

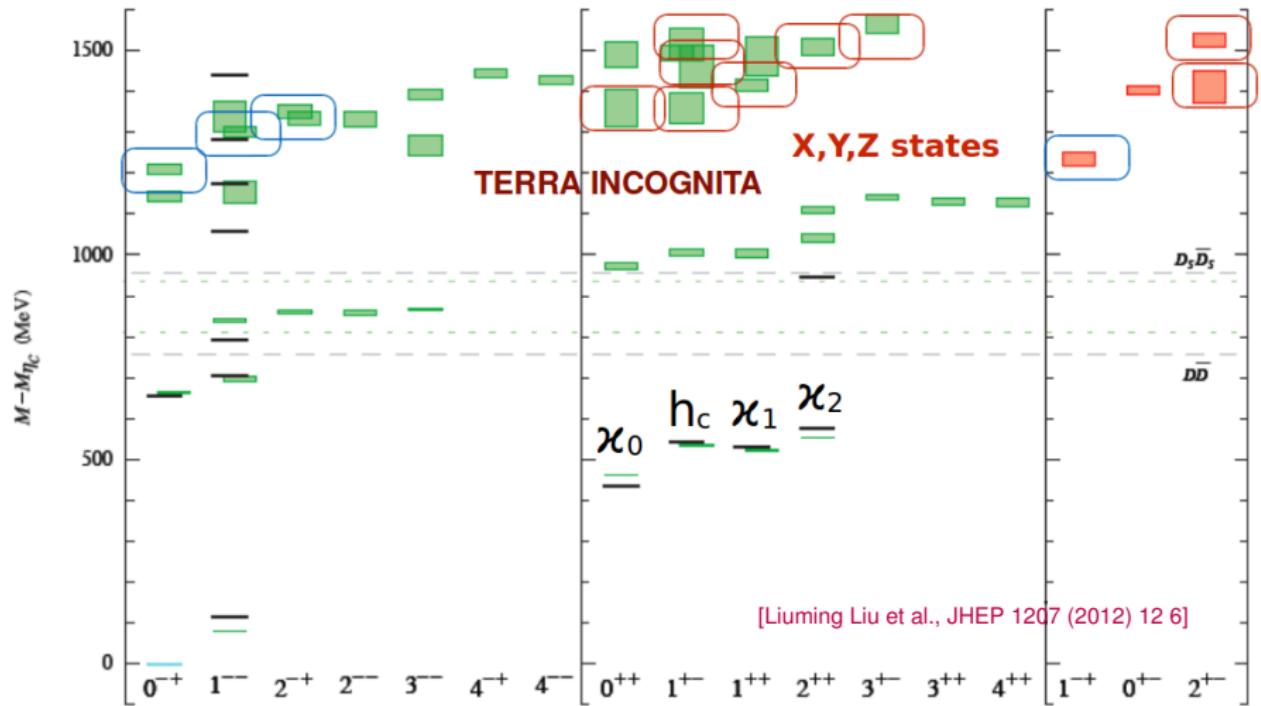


[Dudek et. al, Phys. Rev. D83 (2011) 111502]

- Four lowest multiplets in the hybrid super-multiplet:
  - $1^{+-} \otimes 0^{-+} = 1^{--}$ ,
  - $1^{+-} \otimes 1^{-+} = 0^{-+}, 1^{-+}, 2^{--}$ .
- 10 multiplets of 1<sup>st</sup> orbital excitation.

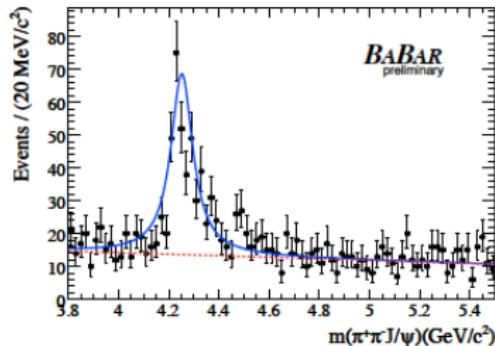
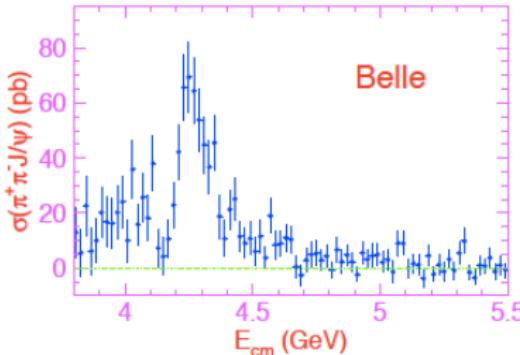
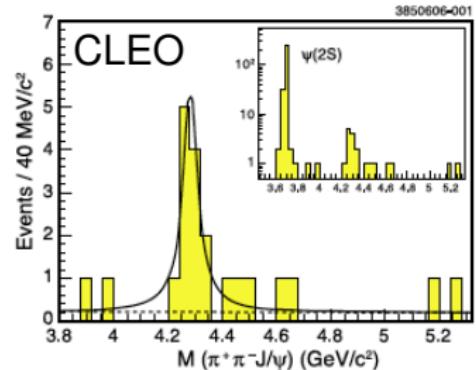
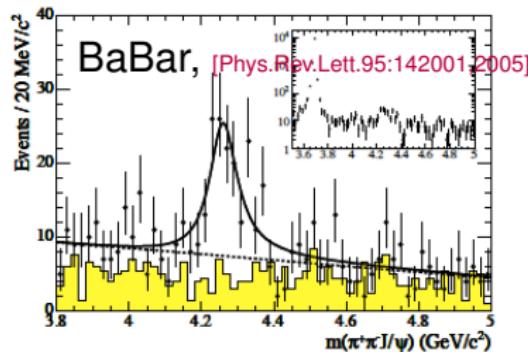
# Charmonium spectrum form lattice

Expected hybrids:  $0^{-+}, 1^{-+}, 2^{-+}, 1^{--}$ ,  $0^{++}, 1^{++}, 2^{++}, 0^{+-}, 1^{+-}, 1^{+-}, 1^{+-}, 2^{+-}, 2^{+-}, 3^{+-}$



# Y(4260) is a hybrid candidate

Discovered by Babar in  $J/\psi\pi^+\pi^-$ , confirmed by CLEO, Belle



# Exotics $1^{-+}$ in the experiment, [from A.Szczepaniak]

$\pi^- p \rightarrow \eta \pi^- p$

$$M = 1370 \pm 16^{+50}_{-30} \text{ MeV / } c^2$$

$$\Gamma = 385 \pm 40^{+65}_{-105} \text{ MeV / } c^2$$

$\pi^- p \rightarrow \eta \pi^0 n$

No consistent B-W interaction is possible but a weak  $\eta \eta \pi$  exists and can reproduce the exotic  $\nu$

$\pi^- p \rightarrow \eta' \pi^- p$

$$M = 1597 \pm 10^{+45}_{-10} \text{ MeV / } c^2$$

$$\Gamma = 340 \pm 40^{+50}_{-50} \text{ MeV / } c^2$$

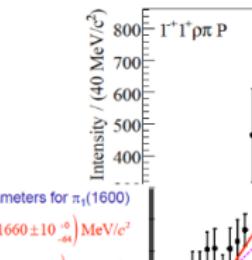
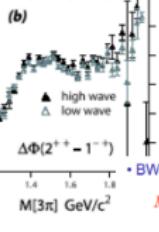
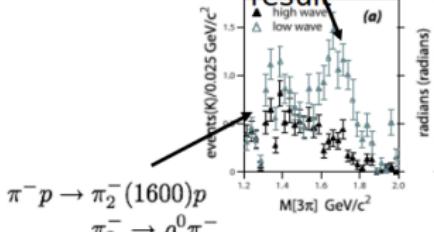
$\pi^- p \rightarrow \rho^0 \pi^- p$

$$M = 1593 \pm 8^{+29}_{-47} \text{ MeV / } c^2$$

$$\Gamma = 168 \pm 20^{+150}_{-12} \text{ MeV / } c^2$$

BNL (E852) yes/no  
COMPASS yes

E852  $1^{-+}$  P-wave  $p\pi$  ( $\pi^- \pi^- \pi^+$ )  
result



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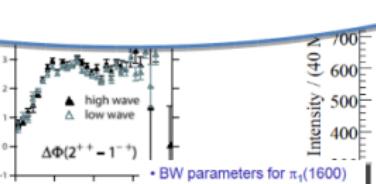
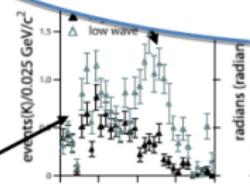
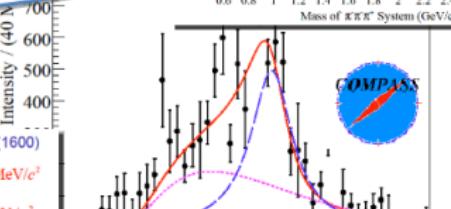
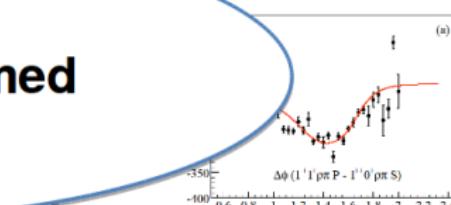
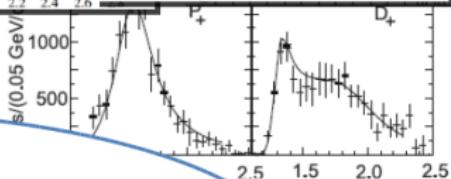
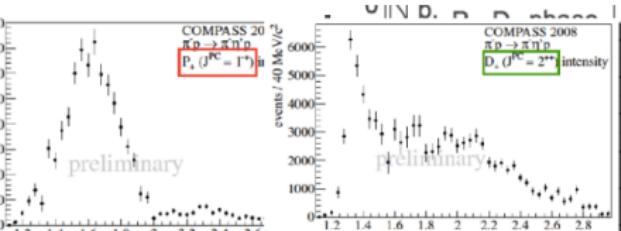
$$\Gamma = 24$$

$\pi^- p \rightarrow \rho^0$

Need to be confirmed

$\pi^- p \rightarrow \pi_2^- (1600) p$

$\pi_2^- \rightarrow \rho^0 \pi^-$



Amplitude analysis

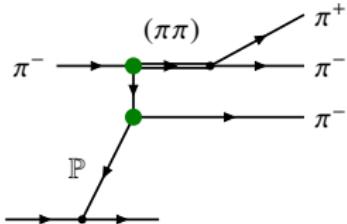
# $1^{-+} \rho\pi P$ -wave at the $3\pi$

PWA at COMPASS

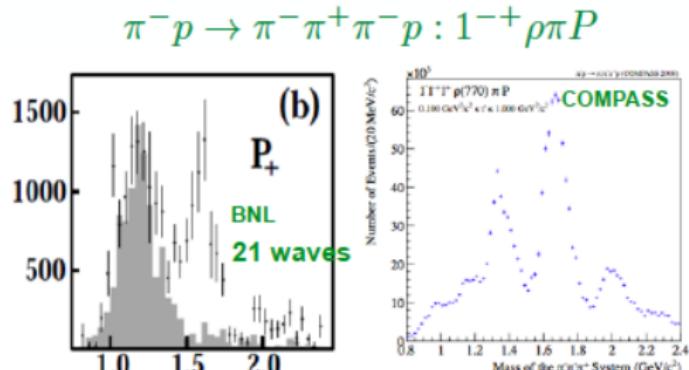
$$\sum_{J^{PC} M^{\epsilon}}^{88} F_{LS}^{JM}(m_{3\pi}) \left[ \begin{array}{c} \xi \\ J^{PC} M^{\epsilon} \end{array} \right]$$

Isobars:  $\rho$ ,  $\rho_3$ ,  $f_2$ ,  $f_0(980)$ ,  $f_0(600)$

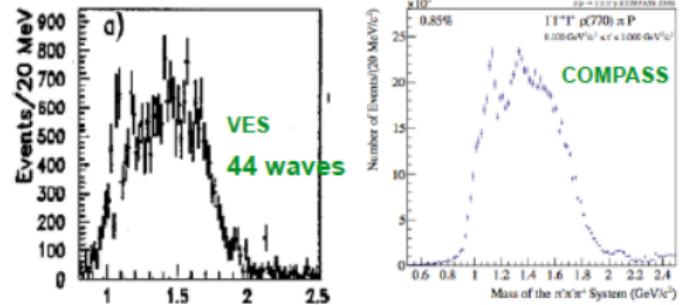
Exchange process ("force") is decomposed to an infinite number of partial waves



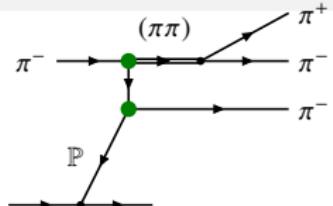
Interpretation ambiguous without implementing force-resonance duality



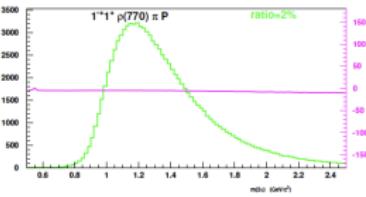
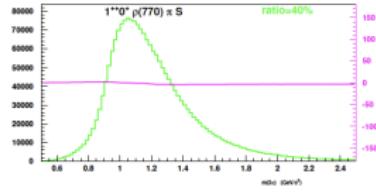
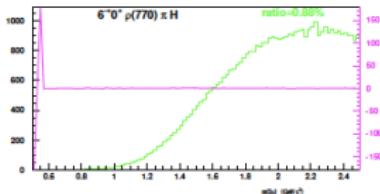
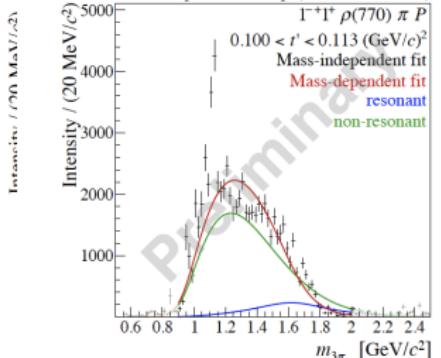
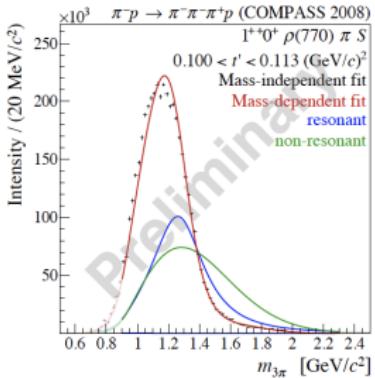
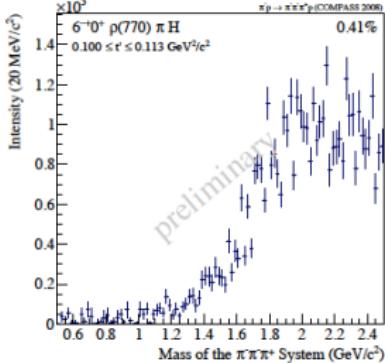
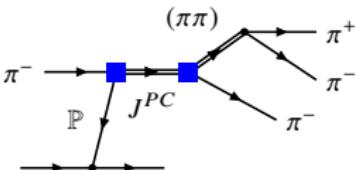
F. Haas, PhD thesis



# Forces-resonances duality



Exchange-processes are backgrounds to the resonances. It is not clear how to implement them in the mass-independent fit.



[D. Ryabchikov, PWA9/ATHOS4 meeting]

M. Mikhasev (JPAC)

Amplitude analysis

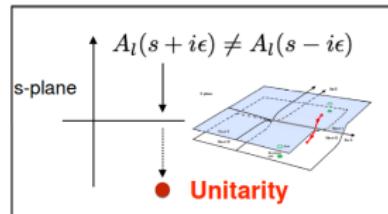
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# S-matrix principles

Crossing, Analyticity, Unitarity

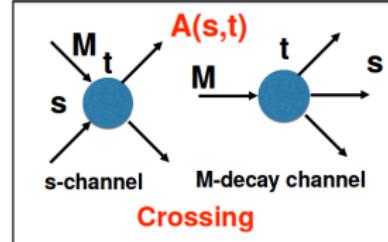
To test a hypothesis about the nature of a “peak” (e.g. resonance, etc.) one needs to construct an amplitude consistent with S-matrix principles (otherwise false singularities appear).



$$A(s, t) = \sum_l A_l(s) P_l(z_s)$$

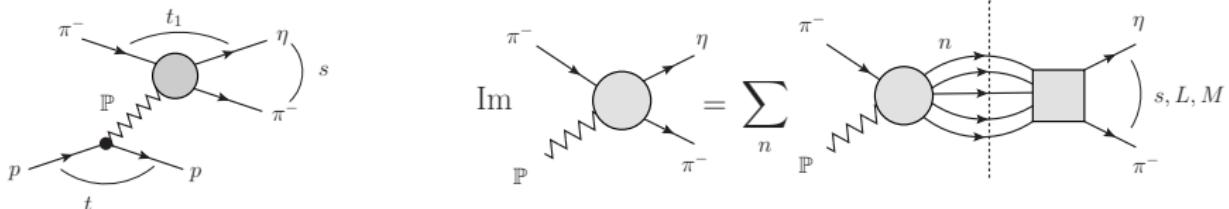
**Analyticity**

$$A_l(s) = \lim_{\epsilon \rightarrow 0} A_l(s + i\epsilon)$$

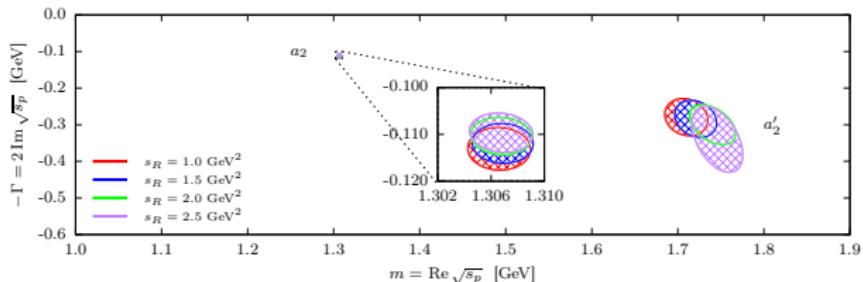
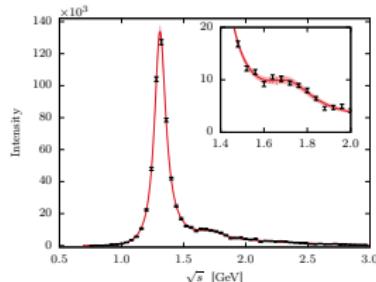


# 2<sup>++</sup> states

## Amplitude analysis of $\eta\pi$ system [A.Jackura(JPAC), arXiv:1707.02848]

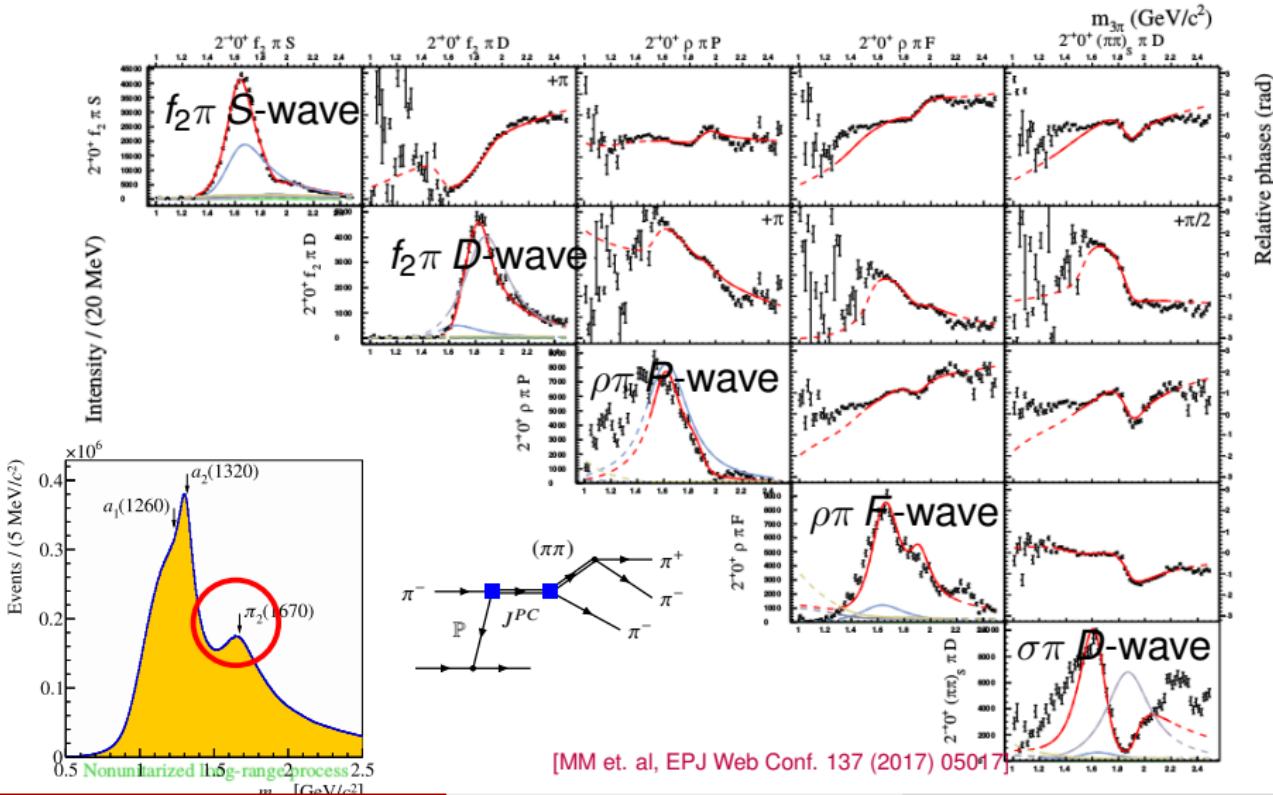


- Reaction is constrained by unitarity  $\text{Im } f(s) = f(s) \rho(s) a_{\eta\pi}^*(s)$
- Amplitude = Production  $\times$   $\eta\pi$ -interaction
- $N$ -over- $D$  parametrization of  $\eta\pi$ -amplitude.  $D = D_0(s) - \frac{s}{\pi} \int ds' \frac{\rho(s') N(s')}{s' - s}$ .
- Analytic amplitude  $\rightarrow$  second sheet  $\Rightarrow$  particles poles



# $2^{-+}$ states

## Amplitude analysis of $3\pi$ system

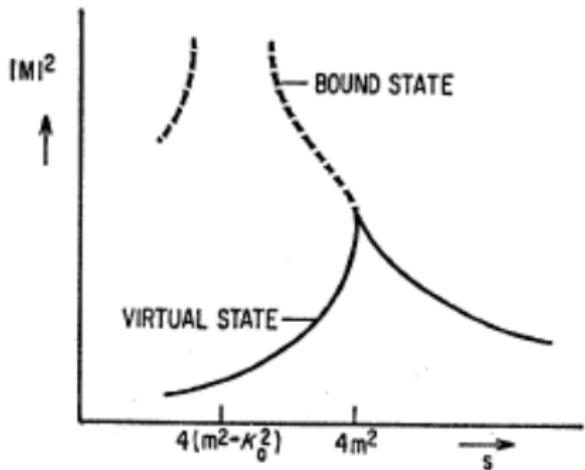


[MM et. al, EPJ Web Conf. 137 (2017) 05017]

# Importance of thresholds

Molecules candidates:  $f_0(980)$ ,  $a_0(980)$ ,  $a_1(1420)$ ,  $\Lambda(1405)$ ,  $XYZ, \dots$

Deutron is  $np$ -molecule bound by meson-exchange forces.



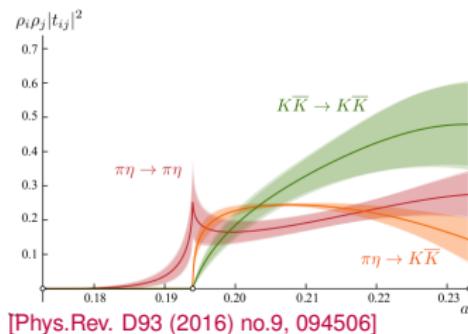
- Thresholds are “windows” to singularities (particles, visual states, forces”) located on the nearby unphysical sheet.
- Singularities appear as cusps (if below threshold) or bumps (if above)

- Bound state: pole at the physical energy plane
- Virtual state: pole at the “unphysical sheet” closest to physical region.

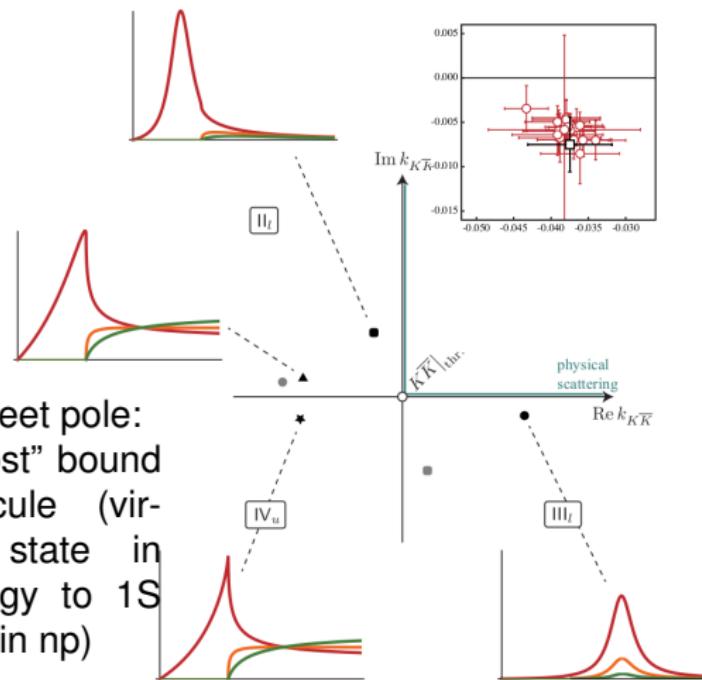
# Lattice results on $a_0(980)$

## Scattering phase shifts

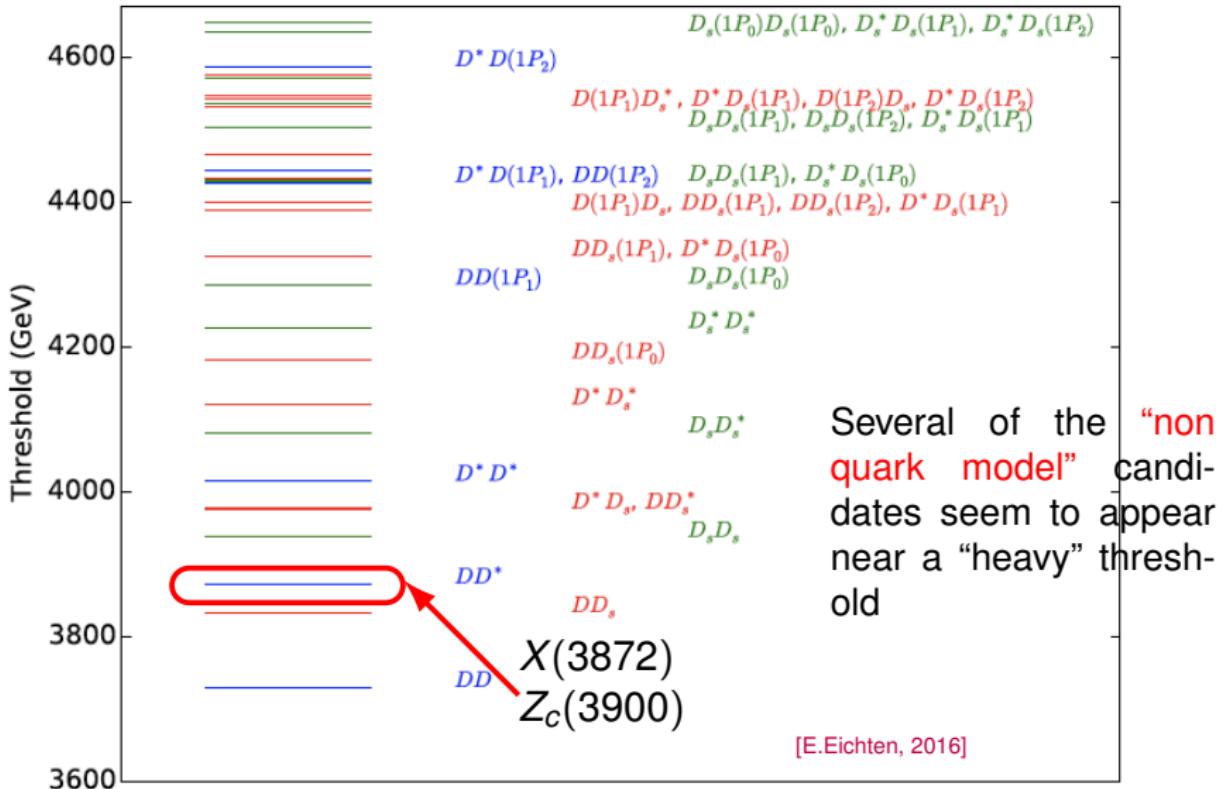
- Coupled-channel analysis of the  $K\bar{K} - \eta\pi$  operators
- $a_0(980)$  is in the scalar isovector channel



$/V$  sheet pole:  
“almost” bound  
molecule (vir-  
tual state in  
analogy to  $1S$   
state in np)



# Thresholds in the charmonium sector

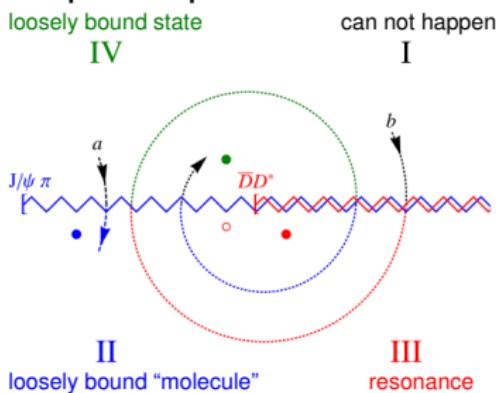


# Amplitude analysis of $Z_c(3900)$ , [Pilloni et. al, Phys.Lett. B772 (2017) 200-209]

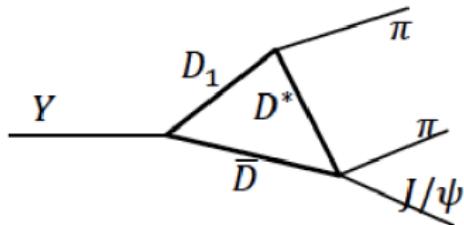
Different singularities → different natures

- reactions  $Y(4260) \rightarrow J/\psi\pi\pi$  and  $Y(4260) \rightarrow D^*\bar{D}$
- Amplitude is analytic function of  $J/\psi\pi$  mass  $s$ .
- Coupled channel analysis → 4 Riemann sheets of  $A(s)$

## Complex $s$ -plane



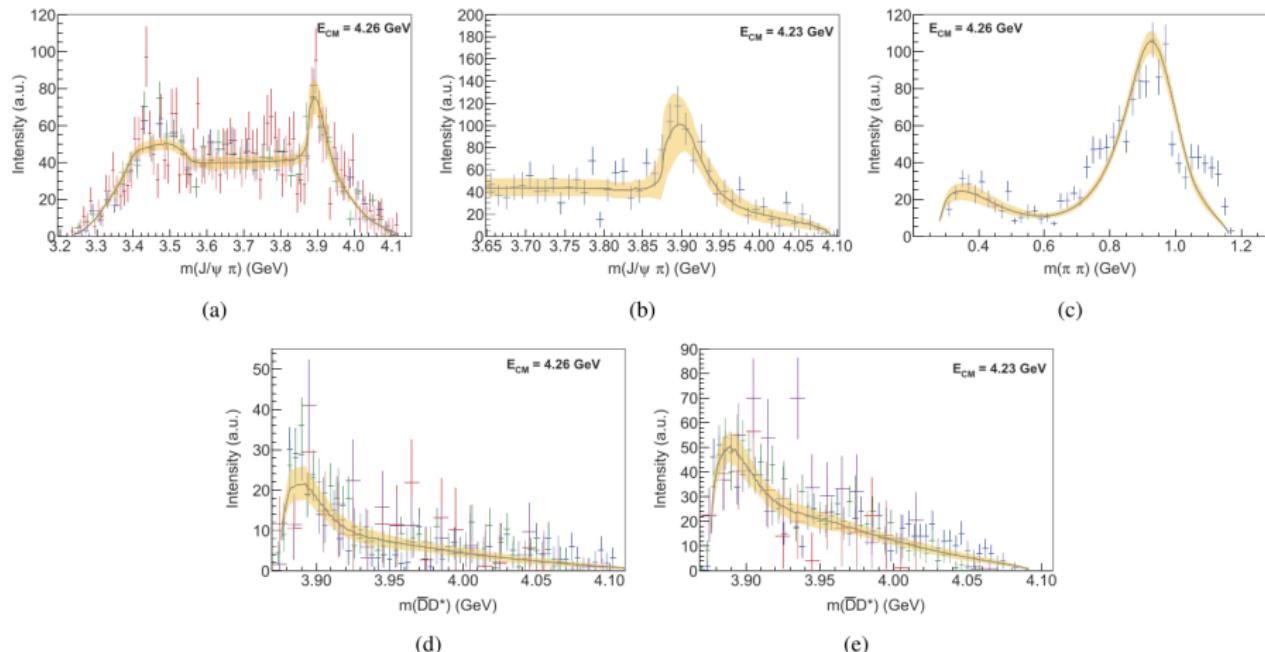
Triangle singularity from the graph



incorporated in the amplitude

# The fit, [Pilloni et. al, Phys.Lett. B772 (2017) 200-209]

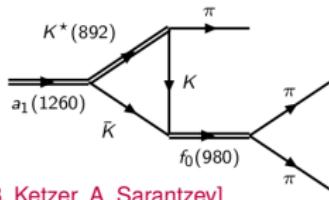
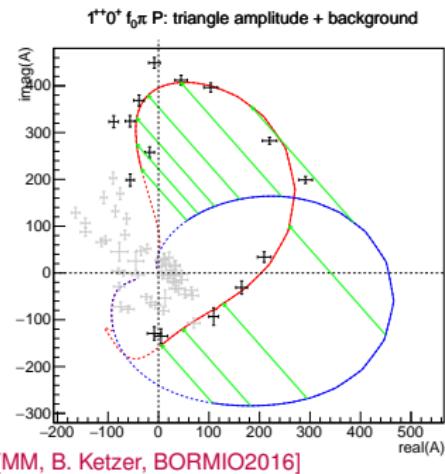
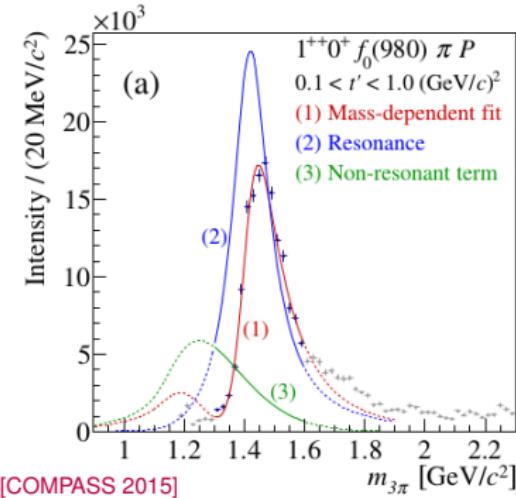
Triangle + pole at the III-sheet of  $J/\psi\pi$  amplitude



**Fig. 4.** Result of the fit for the scenario III + tr. (Flatté K-matrix, with triangle singularity). The plot legend and the comments on the fit are given in the caption of Fig. 3. (For interpretation of the references to color in this figure, the reader is referred to the web version of this article.)

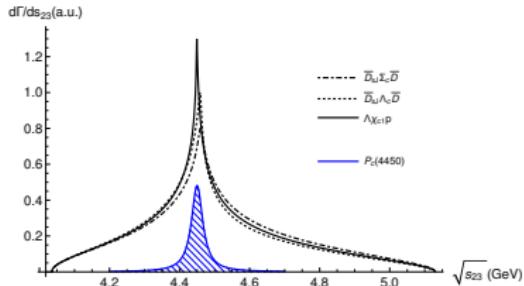
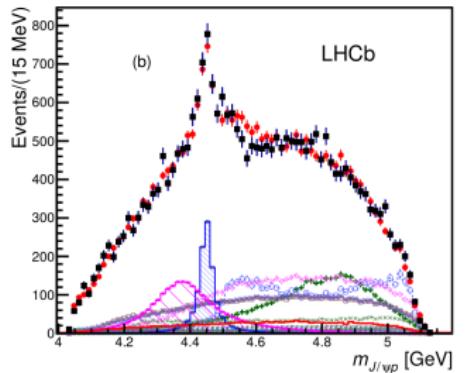
# COMPASS $a_1(1420)$ and the triangle singularity

## Unexpected peak in the $1^{++} f_0 \pi$ $P$ -wave

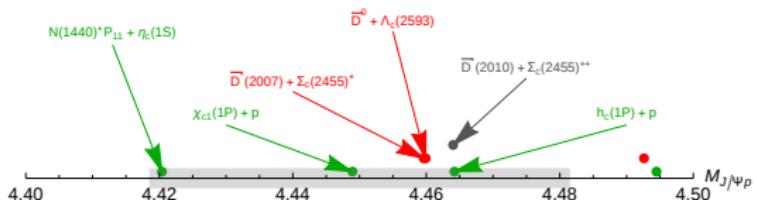


- Amplitude with the tr. diagram describes the data without free parameters
- Rescattering vs resonance – three body unitarity is required

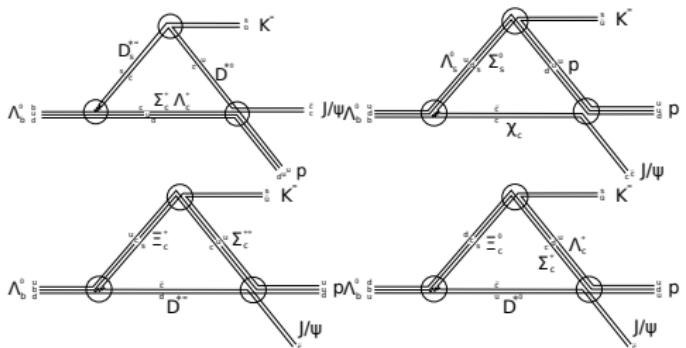
# Pentaquark, $P_c(4450)$



- Many thresholds nearby



- Difficult to find out the relevant channels



- High spin!

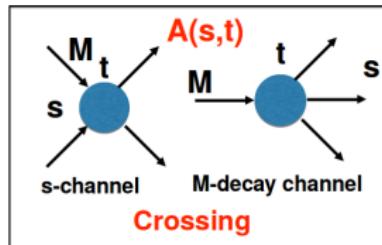
# Determination of resonances quantum numbers

Spin formalism, [T. Skwarnicki & JPAC]

- What do we know about kinematics?  $\Leftarrow$  Reps. of Rotation Group
- How can we constraint the dynamics?  $\Leftarrow$  Unitarity

Formalisms on the market:

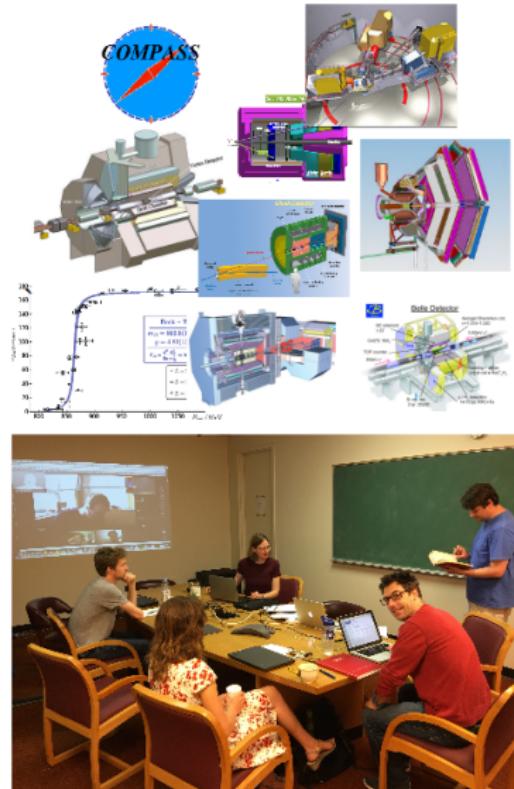
- **Helicity**, Spin-Orbit, Zemach tensors, Chung's relativistic corrections, Covariant LS by Fillipini, ...



- Models have different energy dependence,  
In general unknown, coupling const is a model
- Some introduce spurious singularities
- Some do not satisfy crossing

# Joint Physics Analysis Center(JPAC)

- Started in the Fall of 2013 to support the extraction of physics results from analysis of experimental data from JLab12 and other accelerator laboratories.
- Work is on theoretical, phenomenological and data analysis tools in close collaboration with theorists and experimentalists worldwide.
- Contribute to education of new generation of practitioners in physics of strong interactions.



*Cultura, arte e historia*

UNAM

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12 de marzo del 2017

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## Museo de la Luz

Me gusta 100

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Thank you for the attention

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