THE UNIVERSITY *of* LIVERPOOL

Fortran 90 Programming

(5 Day Course)

—

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with acknowledgements to Steve Morgan and Lawrie Schonfelder.

Lecture 1: Introduction

Course Philosophy

The course:

- assumes a familiarity with a high level language;
- stresses modern scientific programming syntax, for example, array language, modules, defined types, recursion and overloaded operators;
- gives many examples;

Fortran Evolution

History:

- FORmula TRANslation.
- first compiler: 1957.
- first official standard 1972: 'Fortran 66'.
- updated in 1980 to Fortran 77.
- updated further in 1991 to Fortran 90.
- next upgrade due in 1995 - remove obsolescent features, correct mistakes and add limited basket of new facilities such as `ELEMENTAL` and `PURE` user-defined procedures and the `FORALL` statement.
- Fortran is now an ISO/IEC and ANSI standard.

Drawbacks of Fortran 77

Fortran 77 was limited in the following areas,

1. awkward ‘punched card’ or ‘fixed form’ source format;
2. inability to represent intrinsically parallel operations;
3. lack of dynamic storage;
4. non-portability;
5. no user-defined data types;
6. lack of explicit recursion;
7. reliance on unsafe storage and sequence association features.

Fortran 90 New features

Fortran 90 supports,

1. free source form;
2. array syntax and many more (array) intrinsics;
3. dynamic storage and pointers;
4. portable data types (`KIND`s);
5. derived data types and operators;
6. recursion;
7. `MODULE`s
   - procedure interfaces;
   - enhanced control structures;
   - user defined generic procedures;
   - enhanced I/O.

Advantages of Additions

Fortran 90 is:

- more natural;
- greater flexibility;
- enhanced safety;
- parallel execution;
- separate compilation;
- greater portability;

but is

- larger;
- more complex;

Language Obsolescence

Fortran 90 has a number of features marked as obsolescent, this means,

- they are already redundant in Fortran 77;
- better methods of programming already existed in the Fortran 77 standard;
- programmers should stop using them;
- the standards committee's intention is that many of these features will be removed from the next revision of the language, Fortran 95;

Obsolescent Features

The following features are labelled as obsolescent and will be removed from the next revision of Fortran, Fortran 95,

- the arithmetic `IF` statement;
- `ASSIGN` statement;
- `ASSIGN`ed `GOTO` statements;
- `ASSIGN`ed `FORMAT` statements;
- Hollerith format strings;
- the `PAUSE` statement;
- `REAL` and `DOUBLE PRECISION` `DO`-loop control expressions and index variables;
- shared `DO`-loop termination;
- alternate `RETURN`;
- branching to an `ENDIF` from outside the `IF` block;

Undesirable Features

- fixed source form layout - use free form;
- implicit declaration of variables - use `IMPLICIT NONE`;
- `COMMON` blocks - use `MODULE`;
- assumed size arrays - use assumed shape;
- `EQUIVALENCE` statements;
- `ENTRY` statements;
- the computed `GOTO` statement - use `IF` statement;

Object Oriented Facilities

Fortran 90 has some Object Oriented facilities such as:

- *data abstraction* — user-defined types;
- *data hiding* — `PRIVATE` and `PUBLIC` attributes;
- *encapsulation* — Modules and data hiding facilities;
- *inheritance* and *extensibility* — super-types, operator overloading and generic procedures;
- *polymorphism* — user can program his / her own polymorphism by generic overloading;
- *reusability* — Modules;

Availability

Compiler vendors include:

- Edinburgh Portable Compilers (Sun, RS/6000, SGI and MIPS);
- NAg / Salford (unix, VMS and PC);
- NA Software (386/486, SPARC, T800 and T9000);
- Microway (386/486/586 and i860);
- Pacific Sierra Research — vast90 (translates to Fortran 77);
- ParaSoft;
- IBM (XLF for RS/6000)
- Cray Research (Cray);
- Lahey Computer Systems (PCs / 586);
- Fujitsu for Solaris 2;
- DEC for Alpha AXP (OSF/1 and OpenVMS).

Lecture 2: Elements of Fortran 90

Example

Example Fortran 90 program:

```
PROGRAM Triangle
 IMPLICIT NONE
 REAL :: a, b, c, Area
 PRINT*, 'Welcome, please enter the&
          &lengths of the 3 sides.'
 READ*, a, b, c
 PRINT*,'Triangle''s area: ',Area(a,b,c)
END PROGRAM Triangle
FUNCTION Area(x,y,z)
 IMPLICIT NONE
 REAL :: Area       ! function type
 REAL, INTENT( IN ) :: x, y, z
 REAL :: theta, height
 theta=ACOS((x**2+y**2-z**2)/(2.0*x*y))
 height=x*SIN(theta); Area=0.5*y*height
END FUNCTION Area
```

Coding Style

It is recommended that the following coding convention is adopted:

- *always* use `IMPLICIT NONE`.
- Fortran 90 keywords, intrinsic functions and user defined entities should be in upper case,
- other user entities should be in lower case but may start with a capital letter.
- indentation should be 1 or 2 spaces and should be applied to the bodies of program units, control blocks, `INTERFACE` blocks, etc.
- the names of program units are always included in their `END` statements,
- argument keywords are always used for optional arguments,

Please note: In order that a program fit onto a slide these rules are sometimes relaxed here.

Source Form

Free source form:

- 132 characters per line;
- extended character set;
- '`!`' comment initiator;
- '`&`' line continuation character;
- '`;`' statement separator;
- significant blanks.

Character Set

The following are valid in a Fortran 90 program:

- alphanumeric:

  `a-z`, `A-Z`, `0-9`, and `_` (the underscore)

- symbolic:

Symbol	Description	Symbol	Description
	space	=	equal
+	plus	-	minus
*	asterisk	/	slash
(	left paren	)	right paren
,	comma	.	period
'	single quote	"	double quote
:	colon	;	semicolon
!	shriek	&	ampersand
%	percent	<	less than
>	greater than	$	dollar
?	question mark		

Significance of Blanks

In *free form* source code blanks must not appear:

- within keywords
- within names

```
INTEGER        ! is a valid keyword
INT EGER       ! is not
running_total  ! is a valid name
running total  ! is not
```

Blanks must appear:

- between two separate keywords
- between keywords and names not otherwise separated by punctuation or other special characters.

```
INTEGER FUNCTION fit(i) ! is valid
INTEGERFUNCTION fit(i)  ! is not
INTEGER :: hours, mins  ! is valid
INTEGERhours, mins      ! not valid
```

Blanks are optional between some keywords mainly '`END` < *construct* >' and a few others; *if in doubt add a blank* (it looks better too).

Comments

It is good practise to use lots of comments:

```
INTEGER schminteger        ! comment here
!HPF$ PROCESSORS P(3,3,3) ! HPF directive
```

- everything after the `!` is a comment;
- the `!` in a character context does **not** begin a comment;
- many compilation systems interpret formatted comments, for example, HPF systems.

Names

Fortran 90 names

- must start with a letter

```
a1 ! valid name
1a ! not valid name
```

- may use only letters, digits and the underscore

```
atoz ! valid name
a-z  ! not valid name
```

- underscore should be used to separate words in long names

```
user_name ! valid name
username  ! different valid name
```

- may not be longer than 31 characters

Statement Ordering

The following table details the prescribed ordering:

<table>
<tr><td colspan="3">PROGRAM, FUNCTION, SUBROUTINE, MODULE or BLOCK DATA statement</td></tr>
<tr><td colspan="3">USE statement</td></tr>
<tr><td rowspan="4">FORMAT and ENTRY statements</td><td colspan="2">IMPLICIT NONE</td></tr>
<tr><td>PARAMETER statement</td><td>IMPLICIT statements</td></tr>
<tr><td>PARA-METER and DATA statements</td><td>Derived-Type Definition, Interface blocks, Type declaration statements, Statement function statements and specification statements</td></tr>
<tr><td>DATA statements</td><td>Executable constructs</td></tr>
<tr><td colspan="3">CONTAINS statement</td></tr>
<tr><td colspan="3">Internal or module procedures</td></tr>
<tr><td colspan="3">END statement</td></tr>
</table>

Intrinsic Types

Fortran 90 has three broad classes of object type,

- character;
- boolean;
- numeric.

these give rise to six simple intrinsic types, known a default types,

- `CHARACTER` for strings of one or more characters;
- `LOGICAL` for objects which have the values true or false;
- `REAL` (and `DOUBLE PRECISION`) for approximate, possibly fractional numbers;
- `COMPLEX` for complex numbers;
- `INTEGER` for exact whole numbers.

Other intrinsic types will be described later.

Literal Constants

A literal constant is an entity with a fixed value:

```
+12345      ! INTEGER
2.          ! REAL
1.0         ! REAL
-6.6E-06    ! REAL
-6.6D-06    ! DOUBLE PRECISION
.FALSE.     ! LOGICAL
'Mau''dib'  ! CHARACTER
"Mau'dib"   ! CHARACTER
```

Note,

- there are only two `LOGICAL` values;
- integers are represented by a sequence of digits;
- reals contain a decimal point and can be represented in exponential form
- reals and integers may contain + or -.
- character literals are delimited by the double or single quote symbols, " and ';
- two occurrences of the delimiter inside a string produce one occurrence on output;
- there is only a finite range of values that numeric literals can take.

Implicit Typing

Undeclared variables have an implicit type,

- if first letter is `I, J, K, L, M` or `N` then type is `INTEGER`;
- any other letter then type is `REAL`s.

Implicit typing is potentially very dangerous and should **always** be turned off by adding:

```
IMPLICIT NONE
```

as the first line after any `USE` statements.

Consider,

```
    DO 30 I = 1.1000
     ...
 30 CONTINUE
```

in fixed format with implicit typing this declares a `REAL` variable `DO30I` and sets it to `1.1000` instead of performing a loop 1000 times!

Numeric and Logical Declarations

With `IMPLICIT NONE` variables must be declared. A simplified syntax follows,

< *type* > [,< *attribute*-list >] [::] < *variable*-list > &
[=< *value* >]

If < *attribute*-list > or =< *value* > are present then so must be `::`.

The following are all valid declarations,

```
REAL x
INTEGER :: i,j
LOGICAL, POINTER :: ptr
REAL, DIMENSION(10,10) :: y, z
DOUBLE PRECISION, DIMENSION(0:9,0:9) :: x
INTEGER :: k = 4
```

The `DIMENSION` attribute declares a 10×10 array.

Character Declarations

Character variables are declared in a similar way to numeric types. `CHARACTER` variables can

- refer to one character;
- refer to a string of characters which is achieved by adding a length specifier to the object declaration.

The following are all valid declarations,

```
CHARACTER(LEN=10)  :: name
CHARACTER          :: sex
CHARACTER(LEN=32)  :: str
CHARACTER(LEN=10), DIMENSION(10,10) :: Harray
CHARACTER(LEN=32), POINTER :: Pstr
```

Constants (Parameters)

Symbolic constants, oddly known as *parameters* in Fortran, can easily be set up either in an attributed declaration or parameter statement,

```
REAL, PARAMETER :: pi = 3.14159
CHARACTER(LEN=*), PARAMETER :: &
                  son = 'bart', dad = "Homer"
```

`CHARACTER` constants can assume their length from the associated literal (`LEN=*`).

Parameters should be used:

- if it is known that a variable will only take one value;
- for legibility where a 'magic value' occurs in a program such as π;
- for maintainability when a 'constant' value could feasibly be changed in the future.

Initialisation

Variables can be given initial values:

- can use *initialisation expressions*,
- may only contain PARAMETERs or literals.

```
REAL                :: x, y =1.0D5
INTEGER             :: i = 5, j = 100
CHARACTER(LEN=5)    :: light = 'Amber'
CHARACTER(LEN=9)    :: gumboot = 'Wellie'
LOGICAL  :: on = .TRUE., off = .FALSE.
REAL, PARAMETER :: pi = 3.141592
REAL, PARAMETER :: radius = 3.5
REAL :: circum = 2 * pi * radius
```

gumboot will be padded, to the right, with blanks.

In general, intrinsic functions *cannot* be used in initialisation expressions, the following can be: REPEAT, RESHAPE, SELECTED_INT_KIND, SELECTED_REAL_KIND, TRANSFER, TRIM, LBOUND, UBOUND, SHAPE, SIZE, KIND, LEN, BIT_SIZE and numeric inquiry intrinsics, for, example, HUGE, TINY, EPSILON.

Expressions

Each of the three broad type classes has its own set of intrinsic (in-built) operators, for example, `+`, `//` and `.AND.`,

The following are valid expressions,

```
a+6*g(i)/5.0-(a**2) ! numeric valued
name//" is a wally" ! character valued
lhs .GT. rhs        ! logical valued
```

Expressions can be used in many contexts and can be of any intrinsic type.

Assignment

Assignment is defined between all expressions of the same type:

Examples,

```
a = b
c = SIN(.7)*12.7  ! SIN in radians
name = initials//surname
bool = (a.EQ.b.OR.c.NE.d)
```

The LHS is an object and the RHS is an expression.

Intrinsic Numeric Operations

The following operators are valid for numeric expressions,

- `**` — exponentiation, dyadic operator, for example, `10**2`, (evaluated right to left);
- `*` and `/` — multiply and divide, dyadic operators, for example, `10*7/4`;
- `+` and `-` — plus and minus or add and subtract, monadic and dyadic operators, for example, `10+7-4` and `-3`;

Can be applied to literals, constants, scalar and array objects. The only restriction is that the RHS of `**` must be scalar.

Example,

```
a = b - c
f = -3*6/5
```

Relational Operators

The following *relational operators* deliver a `LOGICAL` result when combined with numeric operands,

`.GT.`	`>`	greater than
`.GE.`	`>=`	greater than or equal to
`.LE.`	`<=`	less than or equal to
`.LT.`	`<`	less than
`.NE.`	`/=`	not equal to
`.EQ.`	`==`	equal to

For example,

```
bool = i .GT. j
boule = i > j
IF (i .EQ. j) c = D
WHERE (a(:) /= 0) a(:) = 1/a(:)
```

Intrinsic Logical Operations

A `LOGICAL` or boolean expression returns a `.TRUE.` / `.FALSE.` result. The following are valid with `LOGICAL` operands,

- `.NOT.` — monadic 'negation'. `.TRUE.` if operand is `.FALSE.`, for example, `.NOT.(a .LT. b)`,
- `.AND.` — logical 'and'. `.TRUE.` if both operands are `.TRUE.`;
- `.OR.` — logical 'or'. `.TRUE.` if at least one operand is `.TRUE.`;
- `.EQV.` — equivalence. `.TRUE.` if operands are the same;
- `.NEQV.` — non-equivalence.. `.TRUE.` if operands are different.

for example,

```
REAL :: a, b, x, y
LOGICAL :: l1, l2
 ...
l1 = (.NOT.(x.EQ.y.AND.a.EQ.b))
l2 = (l1.EQV.((x.GT.a.OR.y.LT.b).NEQV.a.EQ.b))
```

Intrinsic Character Operations — Substrings

Consider,

```
CHARACTER(LEN=*), PARAMETER :: string = "abcdefgh"
```

substrings can be taken,

- `string` is 'abcdefgh'
- `string(1:1)` is 'a' (1st letter)
- `string(2:4)` is 'bcd' (2nd, 3rd and 4th letters).
- `string(1)` is an error.

Intrinsic Character Operations — Concatenation

There is only one intrinsic character operator — most of the manipulation is done using intrinsic functions.

The concatenation operator, //, is used to join two strings.

```
CHARACTER(LEN=4), PARAMETER :: name = "Coal"
CHARACTER(LEN=10) :: song = "Firey "//name
PRINT*, "Rowche "//"Rumble"
PRINT*, song(1:1)//name(2:4)
```

would produce

```
Rowche Rumble
Foal
```

Operator Precedence

Category	Operator	Precedence
Extension	user-defined monadic	Highest
Numeric	**	.
Numeric	* or /	.
Numeric	monadic + or -	.
Numeric	dyadic + or -	.
Character	//	.
Relational	.GT., .GE.,.LE., .LT., .EQ. or .NE.	.
Logical	.NOT.	.
Logical	.AND.	.
Logical	.OR.	.
Logical	.EQV. or .NEQV.	.
Extension	user-defined dyadic	Lowest

Note:

- in an expression with no parentheses, the highest precedence operator is combined with its operands first;

- in contexts of equal precedence left to right evaluation is performed except for **.

Precedence Example

It is easy to make mistakes by forgetting the implications of precedence, the following expression,

```
x = a+b/5.0-c**d+1
```

is equivalent to

```
x = ((a+(b/5.0))-(c**d))+1
```

Likewise the following expression,

```
.NOT.A.OR.B.EQV.C.AND.D.OR..NOT.E
```

is equivalent to

```
((.NOT.A).OR.B).EQV.((C.AND.D).OR.(.NOT.E))
```

Parentheses can be added to any expression to modify the order of evaluation.

Precision Errors

Since real numbers are stored approximately:

- every operation yields a slight loss of accuracy,
- after many operations such 'round-off' errors build up,
- catastrophic accuracy loss can arise when values that are almost equal are subtracted, leading digit are cancelled and a rounding errors become visible.

Consider,

```
x = 0.123456; y = 0.123446
PRINT*, "x = ",x," y = ",y
PRINT*, "x-y = ",x-y," should be 0.100d-4"
```

May produce:

```
x = 0.123457  y = 0.123445
x-y = 0.130d-4 should be 0.100d-4
```

which is 30% in error.

A whole branch of Numerical Analysis is dedicated to minimising this class of errors in algorithms. Be careful!

Lecture 3: Control Constructs, Intrinsics and Basic I/O

Control Flow

Control constructs allow the normal sequential order of execution to be changed. Fortran 90 supports:

- conditional execution statements and constructs, (`IF` ... and `IF` ... `THEN` ... `ELSE` ... `END IF`);
- loops, (`DO` ... `END DO`);
- multi-way choice construct, (`SELECT CASE`);

and less importantly,

- unconditional jump statements, (`GOTO`);
- I/O exception branching, (`ERR=`);

`IF` Statement

The basic form is,

`IF`(< *logical-expression* >)< *exec-stmt* >

If < *logical-expression* > evaluates to `.TRUE.` then the < *exec-stmt* > is executed otherwise control of the program passes to the next line.

A < *logical-expression* > is often:

< *expression* >< *relational-operator* >< *expression* >

For example,

```
IF (bool_val) A = 3
IF (x .GT. y) GOTO 56
IF (i .NE. 0 .AND. j .EQ. 0) k = 1/(k*j)
IF (i /= 0 .AND. j == 0) k = 1/(k*j) ! same
```

When using real-valued expressions (which are approximate) `.EQ.` and `.NE.` have no real meaning.

IF Construct

The block-IFis a more flexible version of the single line IF,

IF(< *logical-expression* >)THEN
        < *then-block* >
[ELSEIF(< *logical-expression* >)THEN
        < *elseif-block* >
...]
[ELSE
        < *else-block* >]
END IF

The first branch to have a true < *logical-expression* > is the one that is executed. If none are found then the < *else-block* >, if present, is executed.

For example,

```
IF (x .GT. 3) THEN
 CALL SUB1
ELSEIF (x .EQ. 3) THEN
 A = B*C-D
ELSE
 IF (y .NE. 0) A=B
ENDIF
```

IF blocks may also be nested.

Nested and Named `IF` Constructs

All control constructs can be both named and nested.

```
outa: IF (a .NE. 0) THEN
 x = b/a
 inna1: IF (c .NE. 0) THEN
  y = d/c
 ELSE inna1
  y = -99
 END IF inna1
ELSE IF (a .GT. 0) THEN outa
 ...
ELSE outa
 ...
END IF outa
```

The names may only be used *once* per program unit and are only intended to make the code clearer.

Conditional Exit Loops

Can set up a non-incremental `DO` loop which is terminated by simply jumping out of it,

```
DO
 DO
  ...
  IF (a.GT.b) EXIT
  ...
 END DO
 ! if a.GT.b control jumps here
 IF (c.GT.d) EXIT
END DO
! if c.GT.d control jumps here
```

The `EXIT` statement tells control to jump out of the current `DO` loop.

It is not possible to jump *into* a loop.

Conditional Cycle Loops

Can set up a non-incremental `DO` loop which, on some iterations, only executes a subset of the statements in the body of the loop,

```
DO
 DO
  ...
  IF (a.GT.b) EXIT
  ...
  IF (a.EQ.b) CYCLE
  ...
 END DO
 IF (c.GT.d) EXIT
END DO
```

`CYCLE` forces control to the **innermost** active `DO` statement and the loop begins a new iteration.

Named and Nested Loops

Loops can be given names and an `EXIT` or `CYCLE` statement can be made to refer to a particular loop.

```
outa: DO
 inna: DO
  ...
  IF (a.GT.b) EXIT outa
  ...
  IF (a.EQ.b) CYCLE outa
  ...
  IF (c.GT.d) EXIT inna
  ...
 END DO inna
 ...
END DO outa
```

The (optional) name following the `EXIT` or `CYCLE` highlights which loop the statement refers to.

Loop names can only be used once per program unit.

DO ... WHILE Loops

If a condition is to be tested at the top of a loop a DO ... WHILE loop could be used,

```
DO WHILE (a .EQ. b)
 ...
END DO
```

The loop only executes if the logical expression evaluates to .TRUE.. Clearly, here, the values of a or b must be modified within the loop otherwise it will never terminate.

The above loop is functionally equivalent to,

```
DO; IF (a .NE. b) EXIT
 ...
END DO
```

Indexed `DO` Loops

Loops can be written which cycle a fixed number of times.

The syntax is as follows,

`DO` < `DO-`*var* >`=`< *expr1* >`,`< *expr2* > [`,`< *expr3* >]
    < *exec-stmts* >
`END DO`

For example,

```
DO i1 = 1, 100, 1
  ...
END DO
```

The number of iterations, which is evaluated **before** execution of the loop begins, is calculated as

`MAX(INT((`< *expr2* >`-`< *expr1* >`+`< *expr3* >`)/`< *expr3* >`),0)`

If this is zero or negative then the loop is not executed.

If < *expr3* > is absent it is assumed to be equal to `1`.

Examples of Loop Counts

A few examples of different loops,

1. upper bound not exact,

```
loopy: DO i = 1, 30, 2
 ... ! 15 iterations
END DO loopy
```

2. negative stride,

```
DO j = 30, 1, -2
 ... ! 15 iterations
END DO
```

3. a zero-trip loop,

```
DO k = 30, 1, 2
 ... ! 0 iterations
 ... ! loop skipped
END DO
```

4. missing stride,

```
DO l = 30,1
 ... ! zero-trip loop
END DO
```

Scope of `DO` Variables

1. `I` is recalculated at the top of the loop and then compared with $< expr2 >$,

2. if the loop has finished, execution jumps to the statement after the corresponding `END DO`,

3. `I` retains the value that it had just been assigned.

For example,

```
DO i = 4, 45, 17
 PRINT*, "I in loop = ",i
END DO
PRINT*, "I after loop = ",i
```

will produce

```
I in loop =  4
I in loop =  21
I in loop =  38
I after loop =  55
```

An index variable may not have its value changed in a loop.

`SELECT CASE` Construct

This is useful if one of several paths must be chosen based on the value of a single expression.

The syntax is as follows,

```
 [ <name>:] SELECT CASE (<case-expr>)
        [ CASE (<case-selector>)[ <name> ]
                <exec-stmts> ] ...
        [ CASE DEFAULT [ <name> ]
                <exec-stmts> ]
END SELECT [ <name> ]
```

Note,

- the *< case-expr >* must be scalar and `INTEGER`, `LOGICAL` or `CHARACTER` valued;
- the *<case-selector>* is a parenthesised single value or range, for example, `(.TRUE.)`, `(1)` or `(99:101)`;
- there can only be one `CASE DEFAULT` branch;
- control cannot jump into a `CASE` construct.

Example Of SELECT CASE Construct

```
 SELECT CASE (num)

  CASE (6,9,99,66)
! IF(num==9.OR. .. .OR.char==66) THEN
   PRINT*, "Woof woof"

  CASE (10:65,67:98)
! ELSEIF((num.GE.10.AND.LE.65) .OR. ...
   PRINT*, "Bow wow"

  CASE (100:)
! ELSEIF (num.GE.100) THEN
   PRINT*, "Bark"

  CASE DEFAULT
! ELSE
   PRINT*, "Meeeoow"

 END SELECT
! ENDIF
```

An IF .. ENDIF construct could be used but a SELECT CASE is neater and more efficient.

Mixed Numeric Expressions

If an expression mixes type, the compiler must automatically convert (promote) one type to another. Default types have an implied ordering:

1. `INTEGER` — lowest
2. `REAL`
3. `DOUBLE PRECISION`
4. `COMPLEX` — highest

For example, if an `INTEGER` is mixed with a `REAL` the `INTEGER` is promoted to (represented as) a `REAL` and then the calculation performed.

Consider,

```
int*real*dp*c
```

the types are coerced as follows: `int` to `REAL` `int*real` to `DOUBLE PRECISION` and `(int*real)*dp` to `COMPLEX`. The above expression is `COMPLEX` valued.

Mixed Type Assignment

Problems often occur with mixed-type arithmetic; the rules for type conversion are given below.

- LHS `INTEGER`; RHS `REAL` or `DOUBLE PRECISION` — the RHS is evaluated, truncated (all the decimal places lopped off) then assigned to the LHS.

- LHS `REAL` or `DOUBLE PRECISION`; RHS `INTEGER`— the RHS is coerced and stored (approximately) in the LHS.

For example,

```
REAL a, b; INTEGER i, j
a = 3.0; b = 4.0
i = b - a
j = -0.9
a = j
```

- `b - a` would be around `1.0`; due to truncation `i` would be `0` or `1`.

- `j` would be truncated to `0`.

- `a` would be set to (about) `0.000`.

Integer Division

Confusion often arises about integer division; in short, division of two integers produces an integer result by truncation (towards zero). Consider,

```
REAL a, b, c, d, e
a = 1999/1000
b = -1999/1000
c = (1999+1)/1000
d = 1999.0/1000
e = 1999/1000.0
```

- `a` is (about) `1.000`
- `b` is (about) `-1.000`
- `c` is (about) `2.000`
- `d` is (about) `1.999`
- `e` is (about) `1.999`

Great care must be taken when using mixed type arithmetic.

Intrinsic Procedures

Fortran 90 has 113 in-built or *intrinsic* procedures to perform common tasks efficiently, they belong to a number of classes:

- elemental such as:
  - mathematical, for example, `SIN` or `LOG`.
  - numeric, for example, `SUM` or `CEILING`;
  - character, for example, `INDEX` and `TRIM`;
  - bit, for example, `IAND` and `IOR`;
- inquiry, for example, `ALLOCATED` and `SIZE`;
- transformational, for example, `REAL` and `TRANSPOSE`;
- miscellaneous (non-elemental `SUBROUTINE`s), for example, `SYSTEM_CLOCK` and `DATE_AND_TIME`.

Note all intrinsics which take `REAL` valued arguments also accept `DOUBLE PRECISION` arguments.

Type Conversion Functions

It is easy to transform the type of an entity,

- `REAL(i)` converts `i` to a real approximation,
- `INT(x)` truncates `x` to the integer equivalent,
- `DBLE(a)` converts `a` to `DOUBLE PRECISION`,
- `IACHAR(c)` returns the position of `CHARACTER c` in the ASCII collating sequence,
- `ACHAR(i)` returns the i^{th} character in the ASCII collating sequence.

All above are intrinsic functions. For example,

```
PRINT*, REAL(1), INT(1.7), INT(-0.9999)
PRINT*, IACHAR('C'), ACHAR(67)
```

are equal to

```
1.000000 1 0
67 C
```

Mathematical Intrinsic Functions

Summary,

`ACOS(x)`	arccosine
`ASIN(x)`	arcsine
`ATAN(x)`	arctangent
`ATAN2(y,x)`	arctangent of complex number (x, y)
`COS(x)`	cosine where x is in radians
`COSH(x)`	hyperbolic cosine where x is in radians
`EXP(x)`	e raised to the power x
`LOG(x)`	natural logarithm of x
`LOG10(x)`	logarithm base 10 of x
`SIN(x)`	sine where x is in radians
`SINH(x)`	hyperbolic sine where x is in radians
`SQRT(x)`	the square root of x
`TAN(x)`	tangent where x is in radians
`TANH(x)`	tangent where x is in radians

Numeric Intrinsic Functions

Summary,

`ABS(a)`	absolute value
`AINT(a)`	truncates `a` to whole `REAL` number
`ANINT(a)`	nearest whole `REAL` number
`CEILING(a)`	smallest `INTEGER` greater than or equal to `REAL` number
`CMPLX(x,y)`	convert to `COMPLEX`
`DBLE(x)`	convert to `DOUBLE PRECISION`
`DIM(x,y)`	positive difference
`FLOOR(a)`	biggest `INTEGER` less than or equal to real number
`INT(a)`	truncates a into an `INTEGER`
`MAX(a1,a2,a3,...)`	the maximum value of the arguments
`MIN(a1,a2,a3,...)`	the minimum value of the arguments
`MOD(a,p)`	remainder function
`MODULO(a,p)`	modulo function
`NINT(x)`	nearest `INTEGER` to a `REAL` number
`REAL(a)`	converts to the equivalent `REAL` value
`SIGN(a,b)`	transfer of sign — `ABS(a)*(b/ABS(b))`

Character Intrinsic Functions

Summary,

`ACHAR(i)`	i^{th} character in ASCII collating sequence
`ADJUSTL(str)`	adjust left
`ADJUSTR(str)`	adjust right
`CHAR(i)`	i^{th} character in processor collating sequence
`IACHAR(ch)`	position of character in ASCII collating sequence
`ICHAR(ch)`	position of character in processor collating sequence
`INDEX(str,substr)`	starting position of substring
`LEN(str)`	Length of string
`LEN_TRIM(str)`	Length of string without trailing blanks
`LGE(str1,str2)`	lexically `.GE.`
`LGT(str1,str2)`	lexically `.GT.`
`LLE(str1,str2)`	lexically `.LE.`
`LLT(str1,str2)`	lexically `.LT.`
`REPEAT(str,i)`	repeat i times
`SCAN(str,set)`	scan a string for characters in a set
`TRIM(str)`	remove trailing blanks
`VERIFY(str,set)`	verify the set of characters in a string

PRINT Statement

This is the simplest form of directing unformatted data to the standard output channel, for example,

```
CHARACTER(LEN=*), PARAMETER :: &
  long_name = "Llanphair...gogogoch"
REAL :: x, y, z
LOGICAL lacigol
x = 1; y = 2; z = 3
lacigol = (y .eq. x)
PRINT*, long_name
PRINT*, "Spock says ""illogical&
         &Captain"" "
PRINT*, "X = ",x," Y = ",y," Z = ",z
PRINT*, "Logical val: ",lacigol
END
```

produces on the screen,

```
Llanphair...gogogoch
Spock says "illogical Captain"
X =  1.000  Y =  2.000  Z =  3.000
Logical val:  F
```

`PRINT` Statement

Note,

- each `PRINT` statement begins a new line;
- the `PRINT` statement can transfer any object of intrinsic type to the standard output;
- strings may be delimited by the double or single quote symbols, " and ’;
- two occurrences of the string delimiter inside a string produce one occurrence on output;

`READ` Statement

`READ` accepts unformatted data from the standard input channel, for example, if the type declarations are the same as for the `PRINT` example,

```
READ*, long_name
READ*, x, y, z
READ*, lacigol
```

accepts

```
Llanphairphwyll...gogogoch
0.4 5. 1.0e12
T
```

Note,

- each `READ` statement reads from a newline;
- the `READ` statement can transfer any object of intrinsic type from the standard input;

Lecture 4: Arrays

Array Terminology

Examples of declarations:

```
REAL, DIMENSION(15)        :: A
REAL, DIMENSION(-4:0,0:2) :: B
REAL  :: C(5,3), D(0:4,0:2) ! Shorthand
```

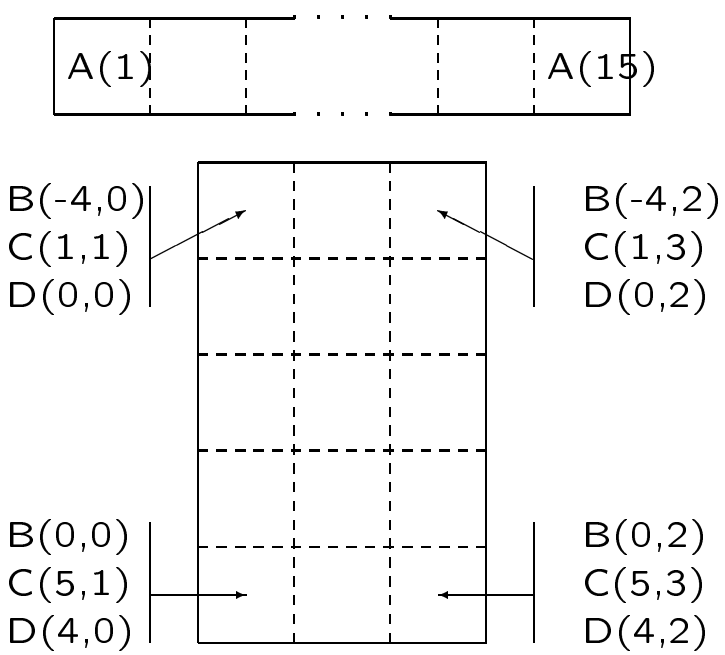
The above are *explicit-shape* arrays.

Terminology:

- *rank* — number of dimensions;
- *bounds* — upper and lower limits of indices;
- *extent* — number of elements in dimension;
- *size* — either the total number of elements or, if particular dimension is specified, the number of elements in that dimension;
- *shape* — rank and extents;
- *conformable* — same shape, `B` and `C` and `D`.

Visualisation of Arrays

```
REAL, DIMENSION(15)        :: A
REAL, DIMENSION(-4:0,0:2) :: B
REAL  :: C(5,3), D(0:4,0:2) ! Shorthand
```



Declarations

Literals and constants can be used in array declarations,

```
INTEGER, PARAMETER :: lda = 5
REAL, DIMENSION(-10:-1)    :: X
REAL, DIMENSION(0:lda-1)   :: Y
REAL, DIMENSION(1+lda*lda,10) :: Z
```

- bounds can begin and end anywhere,
- default lower bound is 1,
- arrays can be zero-sized (if `lda = 0`),

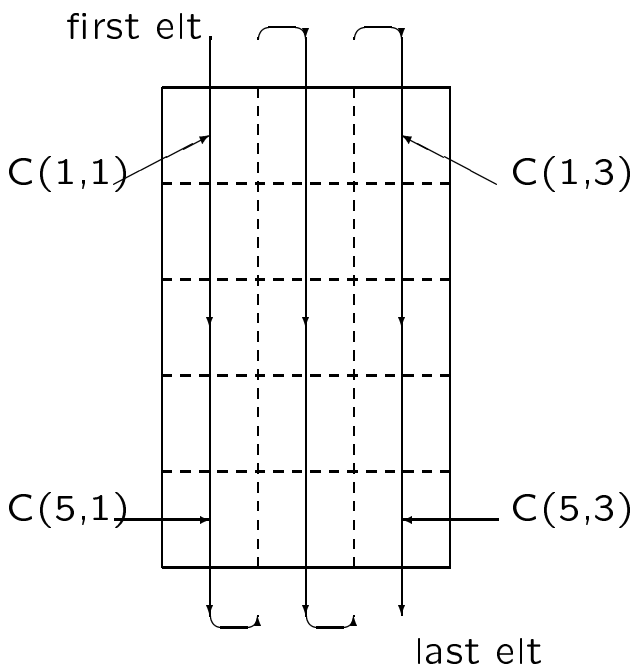
Array Element Ordering

Organisation in memory:

- Fortran 90 does not specify anything about how arrays should be located in memory. **It has no storage association.**

- Fortran 90 does define an array element ordering for certain situations which is of column major form,

The array is conceptually ordered as:




```
C(1,1),C(2,1),..,C(5,1),C(1,2),C(2,2),..,C(5,3)
```

Array Syntax

Using the earlier declarations, references can be made to:

- whole arrays (conformable)
  - `A = 0` sets whole array `A` to zero;
  - `B = C + 1` adds one to all elements, of `C` and then assigns each element to the corresponding element of `B`.
- elements
  - `A(1) = 0.0` sets one element to zero,
  - `B = A(3) + C(5,1)` sets whole array `B` to the sum of two elements.
- array sections
  - `A(2:6) = 0` sets section of `A` to zero,
  - `B(-1:0,1:2) = C(1:2,2:3) + 1` adds one to the subsection of `C` and assigns to the subsection of `B`.

Whole Array Expressions

Arrays can be treated like a single variable in that:

- can use intrinsic operators between conformable arrays (or sections),

  ```
  B = C * D - B**2
  ```

  this is equivalent to concurrent execution of:

  ```
  B(-4,0) = C(1,1)*D(0,0)-B(-4,0)**2 ! in ||
  B(-3,0) = C(2,1)*D(1,0)-B(-3,0)**2 ! in ||
   ...
  B(-4,1) = C(1,2)*D(0,1)-B(-4,1)**2 ! in ||
   ...
  B(0,2)  = C(5,3)*D(4,2)-B(0,2)**2  ! in ||
  ```

- elemental intrinsic functions can be used,

  ```
  B = SIN(C)+COS(D)
  ```

  the function is applied element by element.

Array Conformance

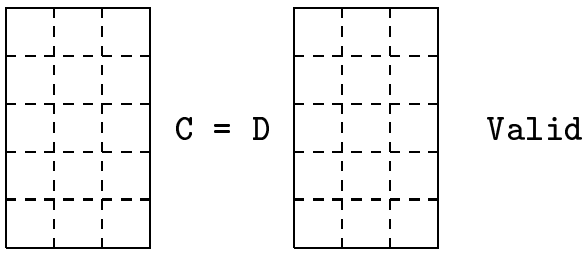
Arrays or sub-arrays must conform with all other objects in an expression:

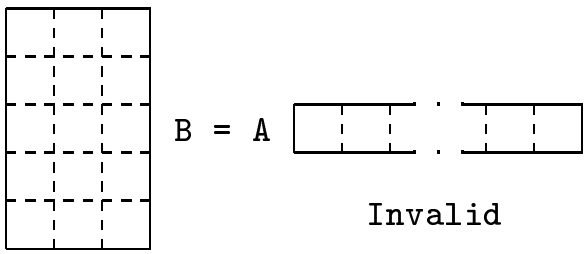
- a scalar conforms to an array of any shape with the same value for every element:

```
C = 1.0   ! is valid
```

- two array references must conform in their shape.

Using the declarations from before:





`A` and `B` have the same size but have different shapes so cannot be directly equated.

Array Sections

An array can be subscripted by a *subscript-triplet* (a shorthand notation for a linear function) which will give rise to a sub-array of the original. The general form is:

[< *bound1* >]:[< *bound2* >][:< *stride* >]

the section starts at < *bound1* > and ends at or before < *bound2* >. < *stride* > is the increment by which the locations are selected.

< *bound1* >, < *bound2* > and < *stride* > must all be scalar integer expressions. Thus

```
A(m:m) = 0      ! m to m 1 elt array
A(m:n:k) = 0    ! m to n step k
A(8:3:-1) = 0   ! 8 to 3 backwards
A(8:3) = 2      ! step 1 => Zero size
A(M::4) = 1     ! default UPB, step 4
A(::2) = 1.0    ! default LWB and UPB
A(m**2:n*k/3) = 1.0
```

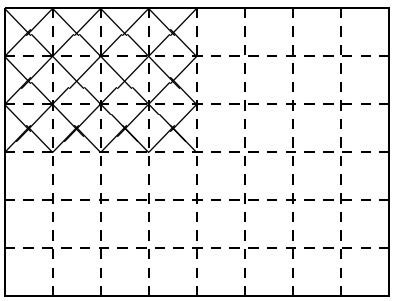
are all valid.

Array Sections — Visualisation

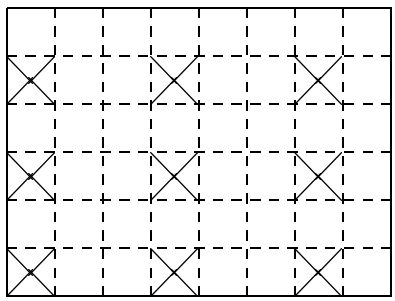
Given,

```
REAL, DIMENSION(1:6,1:8) :: P
```

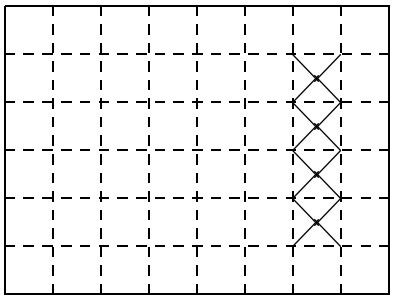
the following are valid sections,



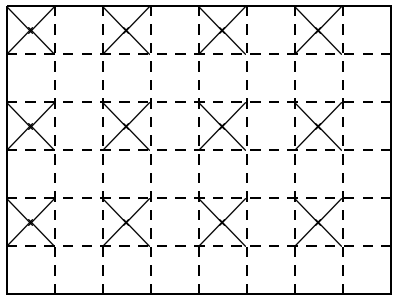
P(1:3,1:4)



P(2::2,:7:3)



P(2:5,7) P(2:5,7:7)



P(::2,::2)

Consider the following assignments,

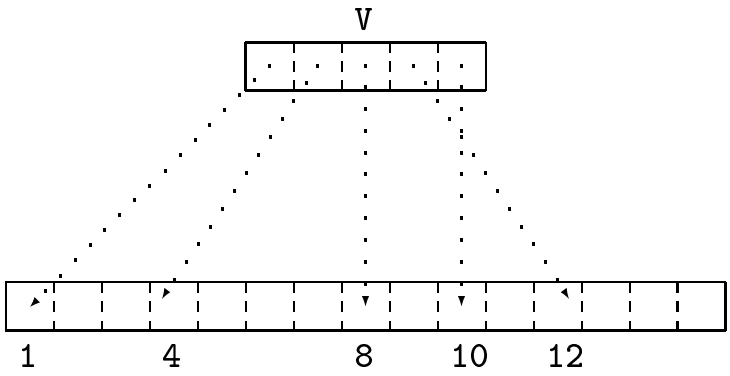
- `P(1:3,1:4) = P(::2,::2)` and `P(1:3,1:4) = 1.0` are valid.
- `P(2::2,:7:3) = P(1:3,1:4)` and `P(2::2,:7:3) = P(2:5,7)` are not.
- `P(2:5,7)` is a 1D section whereas `P(2:5,7:7)` is a 2D section

Vector-valued Subscripts

A 1D array can be used to subscript an array in a dimension. Consider:

```
INTEGER, DIMENSION(5) :: V = (/1,4,8,12,10/)
INTEGER, DIMENSION(3) :: W = (/1,2,2/)
```

- `A(V)` is `A(1)`, `A(4)`, `A(8)`, `A(12)`, and `A(10)`.



- the following are valid assignments:

```
A(V) = 3.5
C(1:3,1) = A(W)
```

- it would be invalid to assign values to `A(W)` as `A(2)` is referred to twice.

- only 1D vector subscripts are allowed, for example,

```
A(1) = SUM(C(V,W))
```

Array Constructors

Used to give arrays or sections of arrays specific values. For example,

```
IMPLICIT NONE
INTEGER                          :: i
INTEGER, DIMENSION(10)           :: ints
CHARACTER(len=5), DIMENSION(3) :: colours
REAL, DIMENSION(4)               :: heights
heights = (/5.10, 5.6, 4.0, 3.6/)
colours = (/'RED  ','GREEN','BLUE '/)
! note padding so strings are 5 chars
ints    = (/ 100, (i, i=1,8), 100 /)
 ...
```

- constructors and array sections must conform.
- must be 1D.
- for higher rank arrays use `RESHAPE` intrinsic.
- `(i, i=1,8)` is an *implied* `DO` and is 1,2,..,8, it is possible to specify a stride.

The RESHAPE Intrinsic Function

RESHAPE is a general intrinsic function which delivers an array of a specific shape:

```
RESHAPE(SOURCE, SHAPE)
```

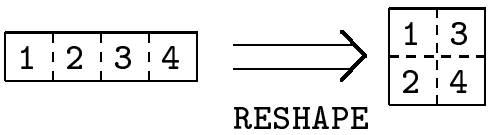
For example,

```
A = RESHAPE((/1,2,3,4/),(/2,2/))
```

A is filled in array element order and looks like:

```
1  3
2  4
```

Visualisation,



Array Constructors in Initialisation Statements

Named array constants can be created:

```
INTEGER, PARAMETER :: Unit_vec = (/1,1,1/)
CHARACTER(LEN=*), DIMENSION(3),    &
 PARAMETER :: lights =             &
         (/'RED  ','BLUE ','GREEN'/)
REAL, DIMENSION(3,3), PARAMETER :: &
      unit_matrix = RESHAPE( &
      (/1,0,0,0,1,0,0,0,1/),(/3,3/))
```

In the second statement all strings must be same length.

Masked Array Assignment — Where Statement

This is achieved using `WHERE`:

```
WHERE (I .NE. 0) A = B/I
```

the LHS of the assignment must be array valued and the mask, (the logical expression,) and the RHS of the assignment must all conform;

For example, if

$$\mathtt{B} = \begin{pmatrix} 1.0 & 2.0 \\ 3.0 & 4.0 \end{pmatrix}$$

and,

$$\mathtt{I} = \begin{pmatrix} \boxed{2} & 0 \\ 0 & \boxed{2} \end{pmatrix}$$

then

$$\mathtt{A} = \begin{pmatrix} \boxed{0.5} & . \\ . & \boxed{2.0} \end{pmatrix}$$

Only the indicated elements, corresponding to the non-zero elements of `I`, have been assigned to.

Where Construct

- there is a block form of masked assignment:

```
WHERE(A > 0.0)
 B = LOG(A)
 C = SQRT(A)
ELSEWHERE
 B = 0.0
ENDWHERE
```

- the mask must conform to the RHS of each assignment; `A`, `B` and `C` must conform;

- `WHERE ... END WHERE` is *not* a control construct and cannot currently be nested;

- the execution sequence is as follows: evaluate the mask, execute the `WHERE` block (in full) then execute the `ELSEWHERE` block;

- the separate assignment statements are executed sequentially but the individual elemental assignments within each statement are (conceptually) executed in parallel.

Allocatable Arrays

Fortran 90 allows arrays to be created on-the-fly; these are known as *deferred-shape* arrays and use dynamic heap storage.

Deferred-shape arrays are:

- declared like explicit-shape arrays but without the extents and with the `ALLOCATABLE` attribute:

```
INTEGER, DIMENSION(:), ALLOCATABLE :: ages
REAL, DIMENSION(:,:), ALLOCATABLE :: speed
```

- given a size in an `ALLOCATE` statement which assigns an area of memory to the object:

```
ALLOCATE(ages(1:10), STAT=ierr)
ALLOCATE(speed(-lwb:upb,-50:0),STAT=ierr)
```

- the optional `STAT=` field reports on the success of the storage request. If the `INTEGER` variable `ierr` is zero the request was successful otherwise it failed.

Deallocating Arrays

Heap storage can be reclaimed using the `DEALLOCATE` statement:

```
IF (ALLOCATED(ages)) DEALLOCATE(ages,STAT=ierr)
```

- it is an error to deallocate an array without the `ALLOCATE` attribute or one that has not been previously allocated space,
- there is an intrinsic function, `ALLOCATED`, which returns a scalar `LOGICAL` values reporting on the status of an array,
- the `STAT=` field is optional but its use is recommended,
- if a procedure containing an allocatable array which does not have the `SAVE` attribute is exited without the array being `DEALLOCATE`d then this storage becomes inaccessible.

Random Number Intrinsic

- `RANDOM_NUMBER(HARVEST)` will return a scalar (or array of) pseudorandom number(s) in the range $0 \leq x < 1$.

  For example,

```
REAL HARVEST, HARVEYS(100,100,100)
CALL RANDOM_NUMBER(HARVEST)
CALL RANDOM_NUMBER(HARVEYS)
```

- `RANDOM_SEED([SIZE=`< *int* >`])` finds the size of the seed.

- `RANDOM_SEED([PUT=`< *array* >`])` seeds the random number generator.

```
CALL RANDOM_SEED(SIZE=isze)
CALL RANDOM_SEED(PUT=IArr(1:isze))
```

Vector and Matrix Multiply Intrinsics

There are two types of intrinsic matrix multiplication:

- `DOT_PRODUCT(VEC1, VEC2)` — inner (dot) product of two rank 1 arrays.

  For example,

  ```
  DP = DOT_PRODUCT(A,B)
  ```

  is equivalent to:

  ```
  DP = A(1)*B(1) + A(2)*B(2) + ...
  ```

  For `LOGICAL` arrays, the corresponding operation is a logical `.AND.`.

  ```
  DP = LA(1) .AND. LB(1) .OR. &
       LA(2) .AND. LB(2) .OR. ...
  ```

- `MATMUL(MAT1, MAT2)` — 'traditional' matrix-matrix multiplication:

  - if `MAT1` has shape (n, m) and `MAT2` shape (m, k) then the result has shape (n, k);
  - if `MAT1` has shape (m) and `MAT2` shape (m, k) then the result has shape (k);
  - if `MAT1` has shape (n, m) and `MAT2` shape (m) then the result has shape (n);

  For `LOGICAL` arrays, the corresponding operation is a logical `.AND.`.

Array Reduction Intrinsics

- `PRODUCT(SOURCE[,DIM][,MASK])`— product of array elements (in an optionally specified dimension under an optional mask);

- `SUM(SOURCE[,DIM][,MASK])`— sum of array elements (in an optionally specified dimension under an optional mask).

For example, if

$$A = \begin{pmatrix} 1 & 3 & 5 \\ 2 & 4 & 6 \end{pmatrix}$$

```
PRINT*, PRODUCT(A)
PRINT*, PRODUCT(A,DIM=1)
PRINT*, PRODUCT(A,DIM=2)
```

gives

```
  720
  2  12  30
 15  48
```

Array Reduction Intrinsics (Cont'd)

These functions operate on arrays and produce a result with less dimensions that the source object:

- `ALL(MASK[,DIM])`— `.TRUE.` if *all* values are `.TRUE.`, (in an optionally specified dimension);
- `ANY(MASK[,DIM])`— `.TRUE.` if *any* values are `.TRUE.`, (in an optionally specified dimension);
- `COUNT(MASK[,DIM])`— number of `.TRUE.` elements in an array, (in an optionally specified dimension);
- `MAXVAL(SOURCE[,DIM][,MASK])`— maximum Value in an array (in an optionally specified dimension under an optional mask);
- `MINVAL(SOURCE[,DIM][,MASK])`— minimum value in an array (in an optionally specified dimension under an optional mask);

If `DIM` is absent or the source array is of rank 1 then the result is scalar, otherwise the result is of rank $n - 1$.

Maximum and Minimum Intrinsics

There are two intrinsics in this class:

- `MAX(SOURCE1,SOURCE2[,SOURCE3[,...]])`— maximum values over all source objects
- `MIN(SOURCE1,SOURCE2[,SOURCE3[,...]])`— minimum values over all source objects
- `MAX(1,2,3)` is `3`
- `MIN((/1,2/),(/-3,4/))` is `(/-3,2/)`
- `MAX((/1,2/),(/-3,4/))` is `(/1,4/)`

Array Location Intrinsics

There are two intrinsics in this class:

- `MINLOC(SOURCE[,MASK])`— Location of a minimum value in an array under an optional mask.
- `MAXLOC(SOURCE[,MASK])`— Location of a maximum value in an array under an optional mask.

For example, if

$$\texttt{Array} = \begin{pmatrix} 0 & -1 & 1 & 6 & -4 \\ 1 & -2 & 5 & 4 & -3 \\ 3 & 8 & 3 & -7 & 0 \end{pmatrix}$$

then

- `MINLOC(Array)` is `(/3,4/)`
- `MAXLOC(Array,Array.LE.7)` is `(/1,4/)`
- `MAXLOC(MAXLOC(Array,Array.LE.7))` is `(/2/)` (array valued).

Array Inquiry Intrinsics

These are often useful in procedures, consider the declaration:

```
REAL, DIMENSION(-10:10,23,14:28) :: A
```

- `LBOUND(SOURCE[,DIM])` — lower bounds of an array (or bound in an optionally specified dimension).
  - `LBOUND(A)` is `(/-10,1,14/)` (array);
  - `LBOUND(A,1)` is `-10` (scalar).
- `UBOUND(SOURCE[,DIM])` — upper bounds of an array (or bound in an optionally specified dimension).
- `SHAPE(SOURCE)` — shape of an array,
  - `SHAPE(A)` is `(/21,23,15/)` (array);
  - `SHAPE((/4/))` is `(/1/)` (array).
- `SIZE(SOURCE[,DIM])` — total number of array elements (in an optionally specified dimension),
  - `SIZE(A,1)` is 21;
  - `SIZE(A)` is 7245.
- `ALLOCATED(SOURCE)` — array allocation status;

Array I/O

The conceptual ordering of array elements is useful for defining the order in which array elements are output. If `A` is a 2D array then:

```
PRINT*, A
```

would produce output in the order:

```
A(1,1),A(2,1),A(3,1),..,A(1,2),A(2,2),..
```

```
READ*, A
```

would assign to the elements in the above order.

This order could be changed by using intrinsic functions such as `RESHAPE`, `TRANSPOSE` or `CSHIFT`.

Array I/O Example

```
INTEGER, DIMENSION(1:3,1:3) :: a
a = RESHAPE((/1,2,3,4,5,6,7,8,9/),&
                          (/3,3/))
PRINT*, 'Array element   =',a(3,2)
PRINT*, 'Array section   =',a(:,1)
PRINT*, 'Sub-array       =',a(:2,:2)
PRINT*, 'Whole Array     =',a
PRINT*, 'Array Transp''d =',TRANSPOSE(a)
END
```

produces on the screen,

```
Array element    = 6
Array section    = 1 2 3
Sub-array        = 1 2 4 5
Whole Array      = 1 2 3 4 5 6 7 8 9
Array Transposed = 1 4 7 2 5 8 3 6 9
```

Lecture 5: Procedures

Program Units

Fortran 90 has four useful program units

- main `PROGRAM`,

  the place where execution begins and where control should eventually return before the program terminates.

- `SUBROUTINE`,

  a parameterised named sequence of code which performs a specific task and can be invoked from within other program units.

- `FUNCTION`,

  as a `SUBROUTINE` but returns a result in the function name (of any specified type and kind).

- `MODULE`.

  a program unit which can contain procedures and declarations. It is intended to be attached to any other program unit where the entities defined within it become accessible.

Procedure Classes

A Fortran 90 program *must* contain a main program, it can invoke other user-defined procedures which may be:

- *external* — external to the procedure which calls them, can be compiled separately.
- *internal* — contained within the procedure or main program that calls them (called the *host*).
- *module-procedures* — have some characteristics of both internal and external procedures (see later).

Main Program Syntax

```
PROGRAM Main
 !  ...
CONTAINS ! Internal Procs
   SUBROUTINE Sub1(..)
    !  Executable stmts
   END SUBROUTINE Sub1
    !  etc.
   FUNCTION Funkyn(...)
    !  Executable stmts
   END FUNCTION Funkyn
 END PROGRAM Main
```

```
SUBROUTINE ExtSub1(...)
 !  etc
END SUBROUTINE ExtSub1
```

```
 !  etc.
```

```
FUNCTION ExtFunn(...)
 !  etc.
END FUNCTION ExtFunn
```

[PROGRAM [< *main program name* >]]
        < *declaration of local objects* >
                ...
        < *executable stmts* >
                ...
[CONTAINS
        < *internal procedure definitions* >]
END [PROGRAM [< *main program name* >]]

Program Example

```
PROGRAM Main
 IMPLICIT NONE
 REAL x
 INTRINSIC FLOOR
 REAL, EXTERNAL :: TenTimes
  READ*, x
  PRINT*, FLOOR(x)
  PRINT*, Negative(x)
  PRINT*, TenTimes(x)
CONTAINS
 REAL FUNCTION Negative(a)
  REAL, INTENT(IN) :: a
   Negative = -a
 END FUNCTION Negative
END PROGRAM Main

REAL FUNCTION TenTimes(a)
 IMPLICIT NONE
 REAL, INTENT(IN) :: a
  TenTimes = 10.0*a
END FUNCTION TenTimes
```

Introduction to Procedures

The first question should be: "Do we really need to write a procedure?"

Functionality often exists,

- intrinsics, Fortran 90 has 113,
- libraries, for example, NAg `f190` Numerical Library has 300+,
- modules, number growing, many free! See WWW.

Subroutine Syntax

Syntax of a (non-recursive) subroutine declaration:

```
SUBROUTINE Ext_1(...)
 !  ...
CONTAINS ! Internal Procs
   SUBROUTINE Int_1(...)
    !  Executable stmts
   END SUBROUTINE Int_1
    !  etc.
   FUNCTION Int_n(...)
    !  Executable stmts
   END FUNCTION Int_n
END SUBROUTINE Ext_1
```

```
SUBROUTINE Ext_2(...)
 !  etc
END SUBROUTINE Ext_2
```

SUBROUTINE < *procname* >[(< *dummy args* >)]
< *declaration of dummy args* >
< *declaration of local objects* >
...
< *executable stmts* >
[CONTAINS
< *internal procedure definitions* >]
END [SUBROUTINE [< *procname* >]]

Subroutine Example

- A subroutine is invoked by a `CALL` statement as in:

```
CALL sub1(arg1,arg2,arg3)
```

`arg1`, `arg2` and `arg3` are *actual arguments*.

- `a`, `b` and `c` are *dummy arguments* and must match the actual arguments in type, rank, kind and number.

```
SUBROUTINE sub1(a,b,c)
 IMPLICIT NONE
 REAL :: a, b, c, s
   ...
  CALL sum_sq(a,b,c,s)
   ...
CONTAINS
 SUBROUTINE sum_sq(aa,bb,cc,ss)
  REAL, INTENT(IN) :: aa, bb, cc
  REAL, INTENT(OUT) :: ss
   ss = aa*aa + bb*bb + cc*cc
 END SUBROUTINE sum_sq
END SUBROUTINE sub1
```

- the above shows any external subroutine can invoke one of its own internal procedures,

- external subroutines should be declared,

```
 EXTERNAL sub1
```

External Subroutine Example

An external procedure may invoke a further external procedure,

```
SUBROUTINE sub1(a,b,c)
 IMPLICIT NONE
 EXTERNAL sum_sq  !Must declare
 REAL :: a, b, c, s
   ...
  CALL sum_sq(a,b,c,s)
  ...
END SUBROUTINE sub1
```

calls,

```
SUBROUTINE sum_sq(aa,bb,cc,ss)
 IMPLICIT NONE
 REAL, INTENT(IN) :: aa, bb, cc
 REAL, INTENT(OUT) :: ss
  ss = aa*aa + bb*bb + cc*cc
END SUBROUTINE sum_sq
```

Function Syntax

Syntax of a (non-recursive) function:

[< *prefix* >] `FUNCTION` < *procname* >([< *dummy args* >])
        < *declaration of dummy args* >
        < *declaration of local objects* >
                ...
        < *executable stmts, assignment of result* >
 [`CONTAINS`
        < *internal procedure definitions* >]
`END` [`FUNCTION` [< *procname* >]]

here < *prefix* >, specifies the result type. or,

`FUNCTION` < *procname* >([< *dummy args* >])
        < *declaration of dummy args* >
        < *declaration of result type* >
        < *declaration of local objects* >
                ...
        < *executable stmts, assignment of result* >
 [`CONTAINS`
        < *internal procedure definitions* >]
`END` [`FUNCTION` [< *procname* >]]

here, < *procname* > must be declared.

Function Example

- A function is invoked by its appearance in an expression at the place where its result value is needed,

```
total = total + largest(a,b,c)
```

- external functions should be declared,

```
INTEGER, EXTERNAL :: largest
```

- The function is defined as follows,

```
INTEGER FUNCTION largest(i,j,k)
 IMPLICIT NONE
 INTEGER :: i, j, k
 largest = i
 IF (j .GT. largest) largest = j
 IF (k .GT. largest) largest = k
END FUNCTION largest
```

or equivalently as,

```
FUNCTION largest(i,j,k)
 IMPLICIT NONE
 INTEGER :: i, j, k
 INTEGER :: largest
  ...
END FUNCTION largest
```

Side Effect Functions

If, in

```
rezzy = funky1(a,b,c) + funky2(a,b,c)
```

`funky1` and `funky2` modify the value of, `a` then the order of execution could be important. Consider:

```
INTEGER FUNCTION funky1(a,b,c)
 ...
a = a*a
funky1 = a/b
```

and

```
INTEGER FUNCTION funky2(a,b,c)
 ...
a = a*2
funky2 = a/c
```

With `a=4`, `b=2` and `c=4` the following happens:

- if `funky1` executed first then `rezzy=8+8=16`
- if `funky2` executed first then `rezzy=2+32=34`

A properly constructed function should *not* change its arguments or any global entities.

Procedure Arguments

If external procedures are to be used as arguments they must be declared at the call site as:

- `INTRINSIC` — for in-built external procedures.

```
INTRINSIC MVBITS
REAL, INTRINSIC :: ASIN
```

- `EXTERNAL` — for external or dummy procedures.

```
EXTERNAL My_Subby
INTEGER, EXTERNAL :: My_Funky
```

  If an intrinsic procedure name is used in an `EXTERNAL` statement then only the external procedure of that name is visible in that scope; the intrinsic becomes unavailable.

In both cases the *specific*, not generic, procedure name must be used as an actual argument.

Example of Procedure Arguments

The following example demonstrates the use of procedures as arguments:

```
PROGRAM main
 IMPLICIT NONE
 INTRINSIC ASIN
 REAL, EXTERNAL :: my_sin
 EXTERNAL diffo1
 CALL subby(ASIN,my_sin,diffo1,SIN(0.5))
END PROGRAM

SUBROUTINE subby(fun1,fun2,sub1,x)
 IMPLICIT NONE
 REAL, INTENT(IN)  :: x
 REAL, EXTERNAL :: fun2, fun1
 EXTERNAL sub1
  PRINT*, fun1(x), fun2(x)
  CALL sub1(fun2(x),fun1,x)
END SUBROUTINE subby

SUBROUTINE diffo1(y,f,x)
 IMPLICIT NONE
 REAL, INTENT(IN)  :: x,y
 REAL, EXTERNAL :: f
 print*, "Diffo1 = ",y-f(x)
END SUBROUTINE diffo1

REAL FUNCTION my_sin(x)
 ...
END FUNCTION my_sin
```

Scoping Rules

Fortran 90 is *not* a traditional block-structured language:

- the *scope* of an entity is the range of program unit where it is visible and accessible;
- usually the program unit which contains declaration;
- internal procedures can inherit entities by *host association*.
- objects declared in modules can be made visible by *use-association* (the `USE` statement) — useful for global data;

Host Association

Consider

```
SUBROUTINE calculate_pay
 IMPLICIT NONE
 EXTERNAL hex
 REAL :: pay, tax
 pay = ...;  tax = ...
 CALL print_pay
CONTAINS
 SUBROUTINE print_pay
  REAL :: tax_paid
   tax_paid = pay*tax; PRINT*, tax_paid
   CALL change_pay;    PRINT*, pay*tax
   CALL hex
 END SUBROUTINE print_pay
 SUBROUTINE change_pay
  pay = ...; tax = ...
 END SUBROUTINE change_pay
END SUBROUTINE calculate_pay

SUBROUTINE hex
 REAL :: pay, tax
  ...
END SUBROUTINE hex
```

- `pay` and `tax` in `print_pay` are the same variables as in the host subroutine, they are accessible by *host association*.

- `pay` and `tax` in `hex` is unrelated.

Scope of Names

Consider the following example,

```
SUBROUTINE sub1          ! scope sub1
 EXTERNAL sub4           ! scope sub1
 REAL A, B, C            ! scope sub1
  ...                    ! scope sub1
 CALL sub3(A)            ! scope sub1
 CALL sub4(A)            ! scope sub1
CONTAINS
 SUBROUTINE sub3(D)     ! scope sub3
  REAL C, D             ! local C, D
   ...                  ! scope sub3
  C = A**3      ! A cant be changed
  D = D**3 + C ! D can be changed
  B = C  ! B from sub1; C from sub3
   ...                  ! scope sub3
 END SUBROUTINE sub3
END SUBROUTINE sub1

SUBROUTINE sub4(C)      ! scope sub4
 REAL B, C              ! scope sub4
   ...                  ! scope sub4
  B = C                 ! scope sub4
   ...                  ! scope sub4
END SUBROUTINE sub4
```

In sub3, A may not be changed but may be referenced.

`SAVE` Statement

Local objects:

- are created each time a procedure is invoked,
- are destroyed when the procedure completes,
- *do not* retain their values between calls.

A local variable with the `SAVE` attribute will retain its value and allocation status between calls. For example,

```
SUBROUTINE sub1
 REAL, SAVE :: keep
 REAL       :: chuck
 REAL, ALLOCATABLE, DIMENSION(:,:), SAVE :: X
  ...
 IF (.NOT.ALLOCATED(X)) ALLOCATE(X(20,20))
```

- `keep` and `X` will retain their values between calls.
- `X` will remain allocated between calls,
- `chuck` will disappear between calls,
- `keep` and `X` have *static* storage class.

Implicit SAVE Attribute and the SAVE Statement

The SAVE attribute is given implicitly if:

- the variable is initialised*.

```
SUBROUTINE Barmy
 IMPLICIT NONE
 REAL :: s = 3.5 ! set on first call to 3.5
!REAL, SAVE :: s = 3.5 ! Exactly the same
  ...
```

- the default mode is changed to SAVE,

```
SUBROUTINE Mad
 REAL :: saved
 SAVE
 REAL :: saved_an_all
```

Here the default storage class of the procedure is changed by the SAVE statement. Note that SAVE applies to *all* local objects in the procedure.

*or is in a COMMON block

Procedure Interfaces

For `EXTERNAL` procedures it is possible to provide an *explicit interface* for a procedure. Consider:

```
SUBROUTINE expsum( n, k, x, sum )! in interface
 IMPLICIT NONE
 INTEGER, INTENT(IN) :: n         ! in interface
 REAL, INTENT(IN) :: k,x          ! in interface
 REAL, INTENT(OUT) :: sum         ! in interface
 REAL, SAVE :: cool_time
  ...
END SUBROUTINE expsum             ! in interface
```

The explicit `INTERFACE` for this routine is given by the statements:

```
INTERFACE ! for EXTERNAL procedure
 SUBROUTINE expsum( n, k, x, sum )
  INTEGER, INTENT(IN) :: n
  REAL, INTENT(IN) :: k,x
  REAL, INTENT(OUT)  :: sum
 END SUBROUTINE expsum
END INTERFACE
```

This could be included in the declarations part of any other program unit which calls `expsum`.

Interfaces are *not* needed for internal (or module) procedures.

What Appears in an Interface?

An interface only contains:

- the `SUBROUTINE` or `FUNCTION` header,
- (if not included in the header) the `FUNCTION` type,
- declarations of the dummy arguments (including attributes),
- the `END SUBROUTINE` or `END FUNCTION` statement

Interfaces are only ever needed for `EXTERNAL` procedures.

Interface Example

The following program includes an explicit interface,

```
PROGRAM interface_example
 IMPLICIT NONE

 INTERFACE
  SUBROUTINE expsum(N,K,X,sum)
   INTEGER, INTENT(IN) :: N
   REAL, INTENT(IN) :: K,X
   REAL, INTENT(OUT) :: sum
  END SUBROUTINE expsum
 END INTERFACE

 REAL :: sum
  ...
 CALL expsum(10,0.5,0.1,sum)
  ...
END PROGRAM interface_example
```

Explicit interfaces permit separate compilation, optimisation and type checking.

Argument Intent

Hints to the compiler can be given as to whether a dummy argument will:

- only be referenced — `INTENT(IN)`;
- be assigned to before use — `INTENT(OUT)`;
- be referenced and assigned to — `INTENT(INOUT)`;

```
SUBROUTINE example(arg1,arg2,arg3)
 IMPLICIT NONE
 REAL, INTENT(IN) :: arg1
 INTEGER, INTENT(OUT) :: arg2
 CHARACTER, INTENT(INOUT) :: arg3
 REAL :: r
  r = arg1*ICHAR(arg3)
  arg2 = ANINT(r)
  arg3 = CHAR(MOD(127,arg2))
END SUBROUTINE example
```

The use of `INTENT` attributes is recommended as it:

- allows good compilers to check for coding errors,
- facilitates efficient compilation and optimisation.

Keyword Arguments

Can supply dummys in any order using *keyword arguments*, for example, given

```
INTERFACE
 SUBROUTINE axis(x0,y0,l,min,max,i)
  REAL, INTENT(IN) :: x0,y0,l,min,max
  INTEGER, INTENT(IN) :: i
 END SUBROUTINE axis
END INTERFACE
```

can invoke procedure:

- using positional argument invocation:

```
CALL AXIS(0.0,0.0,100.0,0.1,1.0,10)
```

- using keyword arguments:

```
CALL AXIS(0.0,0.0,Max=1.0,Min=0.1, &
                  L=100.0,I=10)
```

  The names are from the *dummy arguments*.

An `INTERFACE` declaration is mandatory at the call site.

Keyword Arguments

Keyword arguments:

- allow arguments to be specified in any order.
- makes it easy to add an extra argument — no need to modify any calls.
- helps improve the readability of the program.
- are used when a procedure has optional arguments.

Note: once a keyword is used all subsequent arguments must be keyword arguments.

Optional Arguments

Optional arguments:

- allow defaults to be used for missing arguments;
- make some procedures easier to use.

Also:

- once an argument has been omitted all subsequent arguments must be keyword arguments,
- the `PRESENT` intrinsic can be used to check for missing arguments.

An `INTERFACE` declaration is mandatory at the call site.

Optional Arguments Example

For example,

```
SUBROUTINE SEE(a,b)
 IMPLICIT NONE
 REAL, INTENT(IN), OPTIONAL    :: a
 INTEGER, INTENT(IN), OPTIONAL :: b
 REAL    :: ay; INTEGER :: bee
 ay = 1.0; bee = 1 ! defaults
 IF(PRESENT(a)) ay  = a
 IF(PRESENT(b)) bee = b
  ...
```

both `a` and `b` have the optional attribute so `SEE` can be called in the following ways

```
CALL SEE()
CALL SEE(1.0,1); CALL SEE(b=1,a=1.0) ! same
CALL SEE(1.0);   CALL SEE(a=1.0)     ! same
CALL SEE(b=1)
```

Required Interfaces

Explicit interfaces are mandatory if an `EXTERNAL` procedure has:

- dummy arguments that are assumed-shape arrays, pointers or targets;
- `OPTIONAL` arguments;
- an array valued or pointer result (functions);
- a result that has an inherited `LEN=*` length specifier (character functions);

and when the reference:

- has a keyword argument;
- is a defined assignment;
- is a call to the generic name;
- is a call to a defined operator (functions).

Lecture 6: More Procedures

Dummy Array Arguments

There are two main types of dummy array argument:

- *explicit-shape* — all bounds specified;

  ```
  REAL, DIMENSION(8,8), INTENT(IN) :: expl_shape
  ```

  The actual argument that becomes associated with an explicit-shape dummy must conform in size and shape.

- *assumed-shape* — no bounds specified, all inherited from the actual argument;

  ```
  REAL, DIMENSION(:,:), INTENT(IN) :: ass_shape
  ```

  An explicit interface *must* be provided.

- dummy arguments cannot be (unallocated) `ALLOCATABLE` arrays.

Explicit-shape Arrays

A dummy argument that is an explicit-shape array must conform in size and shape to the associated actual argument; no bound information is passed to the procedure.

```
 INTEGER, DIMENSION(8,8)   :: A1
 INTEGER, DIMENSION(64)    :: A2
 INTEGER, DIMENSION(16,32) :: A3
  ...
 CALL subby(A1)                  ! OK
 CALL subby(A2)     ! non conforming
 CALL subby(A3(::2,::4))         ! OK
 CALL subby(RESHAPE(A2,(/8,8/)) ! OK
  ...
SUBROUTINE subby(expl_shape)
 INTEGER, DIMENSION(8,8) :: expl_shape
  ...
END SUBROUTINE subby
```

Assumed-shape Arrays

Should declare dummy arrays as assumed-shape arrays:

```
 INTERFACE
  SUBROUTINE gimlet(a,b)
    ...
 END INTERFACE
  ...
 REAL, DIMENSION(40)    :: X
 REAL, DIMENSION(40,40) :: Y
  ...
 CALL gimlet(X,Y)
 CALL gimlet(X(1:39:2),Y(2:4,4:4))
 CALL gimlet(X(1:39:2),Y(2:4,4)) ! invalid
END PROGRAM

SUBROUTINE gimlet(a,b)
 REAL, INTENT(IN)   :: a(:), b(:,:)
  ...
END SUBROUTINE gimlet
```

Note:

- an explicit `INTERFACE` block is mandatory.
- the actual arguments cannot be a vector subscripted array,
- the actual argument cannot be an assumed-size array.
- in procedure bounds begin at 1.

Automatic Arrays

Other arrays can depend on dummy arguments, these are called *automatic* arrays and:

- their size is determined by dummy arguments,
- they cannot have the `SAVE` attribute (or be initialised);

Consider,

```
 INTERFACE ! etc
  ...
 END INTERFACE
  ...
 CALL une_bus_riot(IX,2,3)
 CALL une_bus_riot(IY,7,2)
END PROGRAM

SUBROUTINE une_bus_riot(A,M,N)
 INTEGER, INTENT(IN) :: M, N
 INTEGER, INTENT(INOUT) :: A(:,:)
 REAL :: A1(M,N)                    ! auto
 REAL :: A2(SIZE(A,1),SIZE(A,2)) ! auto
  ...
END SUBROUTINE
```

The `SIZE` intrinsic or dummy arguments can be used to declare automatic arrays. `A1` and `A2` may have different sizes for different calls.

Explicit Length Character Dummy Arguments

- An *explicit-length* dummy `CHARACTER` argument **must** match the actual in kind and rank.

- If the actual is a scalar default character variable then the length of the dummy must be less than or equal to the length of the actual.

```
 CHARACTER(LEN=10), DIMENSION(10) :: wurd
  ...
 CALL char_example(wurd(3))
 CALL char_example(wurd(6:))
  ...
SUBROUTINE char_example(wird,werds)
 CHARACTER(LEN=10), :: wird
 CHARACTER(LEN=10), :: werds(:)
  ...
END SUBROUTINE char_example
```

Assumed Length Character Dummy Arguments

- `CHARACTER` dummys can inherit their length specifier (`LEN=`) from the actual argument;
- the kind and rank must still match;
- such an argument is an *assumed-length* character dummy;

```
 ...
CHARACTER(LEN=10) :: vari1
CHARACTER(LEN=20) :: vari2
 ...
CALL char_lady(vari1)
CALL char_lady(vari2)
 ...
SUBROUTINE char_lady(word)
 IMPLICIT NONE
 CHARACTER(LEN=*), INTENT(IN) :: word
  ...
  PRINT*, "Length of arg is", LEN(word)
END SUBROUTINE char_lady
```

will produce,

```
Length of arg is 10
Length of arg is 20
```

Array-valued Functions

Functions can return arrays, for example,

```
 INTERFACE
  FUNCTION funnie(ima,scal)
   ...
 END INTERFACE
 INTEGER, PARAMETER      :: m = 6
 INTEGER, DIMENSION(M,M) :: im1, im2
  ...
 IM2 = funnie(IM1,1) ! invoke
END PROGRAM

FUNCTION funnie(ima,scal)
 IMPLICIT NONE
 INTEGER, INTENT(IN) :: ima(:,:)
 INTEGER, INTENT(IN) :: scal
 INTEGER, DIMENSION(SIZE(ima,1),SIZE(ima,2)) &
                     :: funnie
 funnie(:,:) = ima(:,:)*scal
END FUNCTION funnie
```

An explicit interface is mandatory for array-valued external functions.

Character-valued Functions

Can define a function that returns a `CHARACTER` string of a given length:

```
FUNCTION reverse(word)
 CHARACTER(LEN=*), INTENT(IN) :: word
 CHARACTER(LEN=LEN(word)) :: reverse
 INTEGER :: lw
 lw = LEN(word)
 ! reverse characters
 DO I = 1,lw
    reverse(lw-I+1:lw-I+1) = word(I:I)
 END DO
END FUNCTION reverse
```

Here the length of the function result is determined by the dummy argument.

An explicit interface in the calling procedure is mandatory if `LEN=*` is used.

Recursive Procedures

In Fortran 77 recursion had to be simulated by a user defined stack and corresponding manipulation functions, in Fortran 90 it is supported as a feature.

- recursive procedures call themselves (either directly or indirectly),
- recursion is a neat way of expressing a wide variety of problems,
- recursion incurs certain efficiency overheads,
- recursive procedures must be explicitly declared using the `RECURSIVE` keyword,
- recursive functions declarations must contain a `RESULT` keyword, and one type declaration refers to both the function name and the result variable.

Recursive Function Example

The following example calculates the factorial of a number and uses $n! = n(n-1)!$

```
RECURSIVE FUNCTION fact(N) RESULT(N_Fact)
 IMPLICIT NONE
 INTEGER, INTENT(IN)  :: N
 INTEGER :: N_Fact ! also defines type of fact
 IF (N > 0) THEN
   N_Fact = N * fact(N-1)
 ELSE
   N_Fact = 1
 END IF
END function FACT
```

To calculate 4!,

1. 4! is $4 \times 3!$, so calculate 3! then multiply by 4,

2. 3! is $3 \times 2!$, need to calculate 2!,

3. 2! is $2 \times 1!$, 1! is $1 \times 0!$ and $0! = 1$

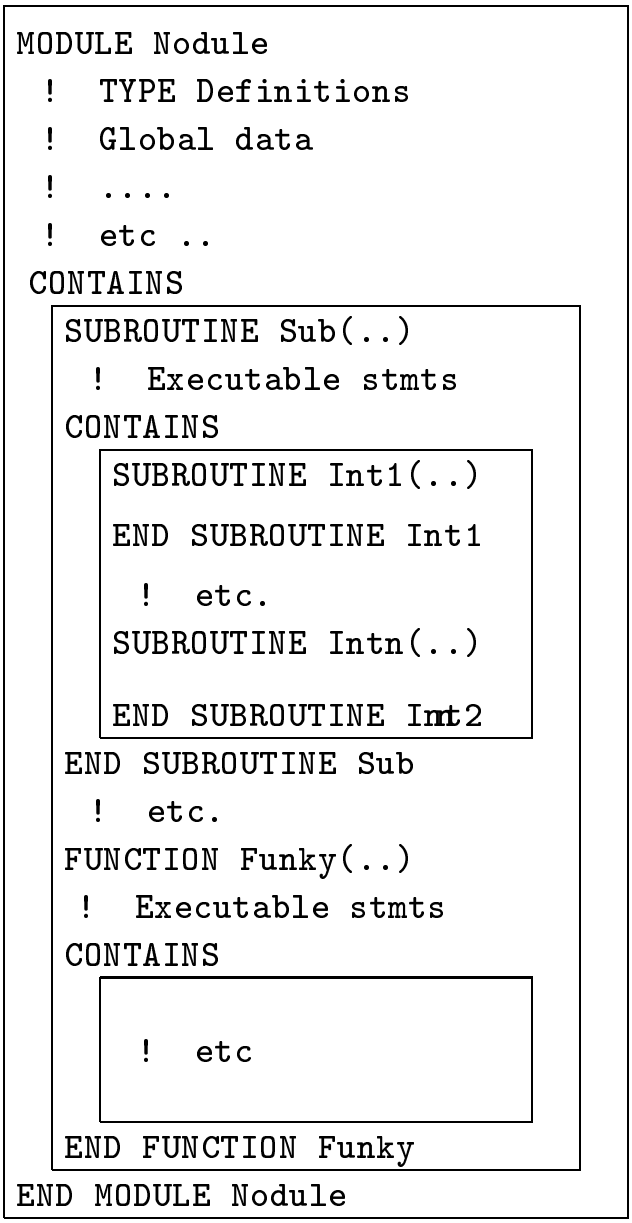
4. can now work back up the calculation and fill in the missing values.

Modules — An Overview

The `MODULE` program unit provides the following facilities:

- global object declaration;
- procedure declaration (includes operator definition);
- semantic extension;
- ability to control accessibility of above to different programs and program units;
- ability to package together whole sets of facilities;

General Form



MODULE < *module name* >
< *declarations and specifications statements* >
[CONTAINS
< *definitions of module procedures* >]
END [MODULE [< *module name* >]]

Modules — Global Data

Fortran 90 implements a new mechanism to implement global data:

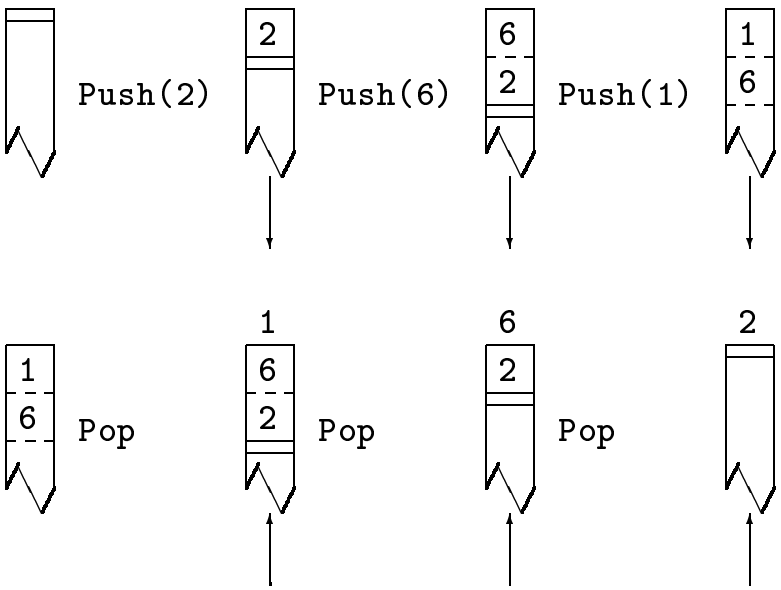
- declare the required objects within a module;
- give them the `SAVE` attribute;
- `USE` the module when global data is needed.

For example, to declare `pi` as a global constant

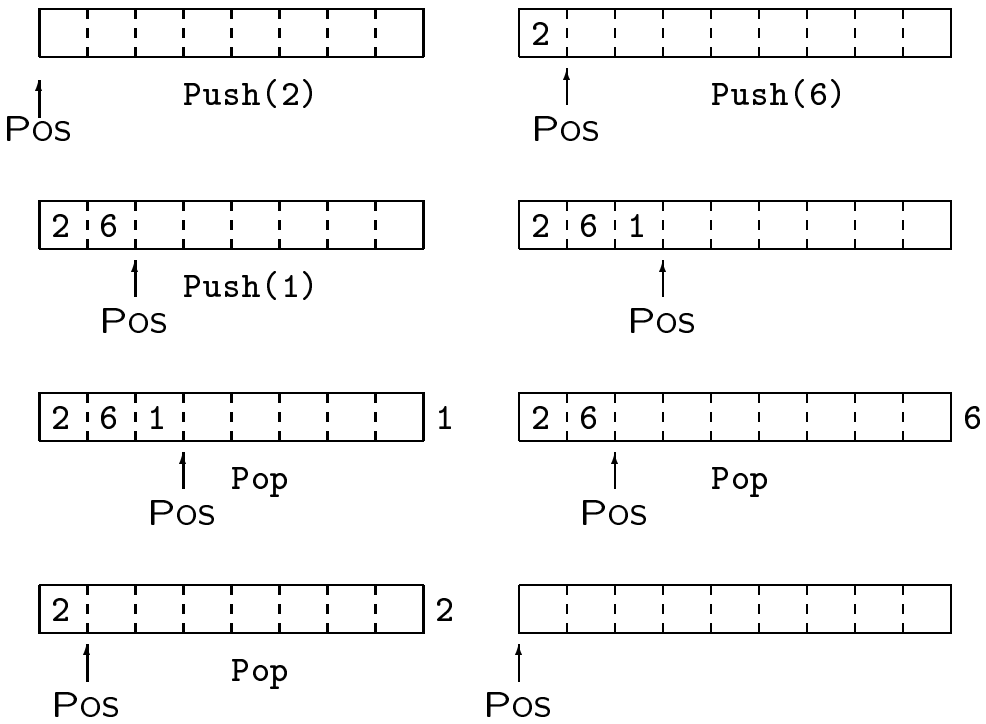
```
MODULE  Pye
 REAL, SAVE :: pi = 3.142
END MODULE Pye

PROGRAM Area
 USE Pye
 IMPLICIT NONE
 REAL :: r
  READ*, r
  PRINT*, "Area= ",pi*r*r
END PROGRAM Area
```

`MODULE`s should be placed *before* the program.

Stack Simulation



Implementation of a Stack



Module Global Data Example

For example, the following defines a very simple 100 element integer stack

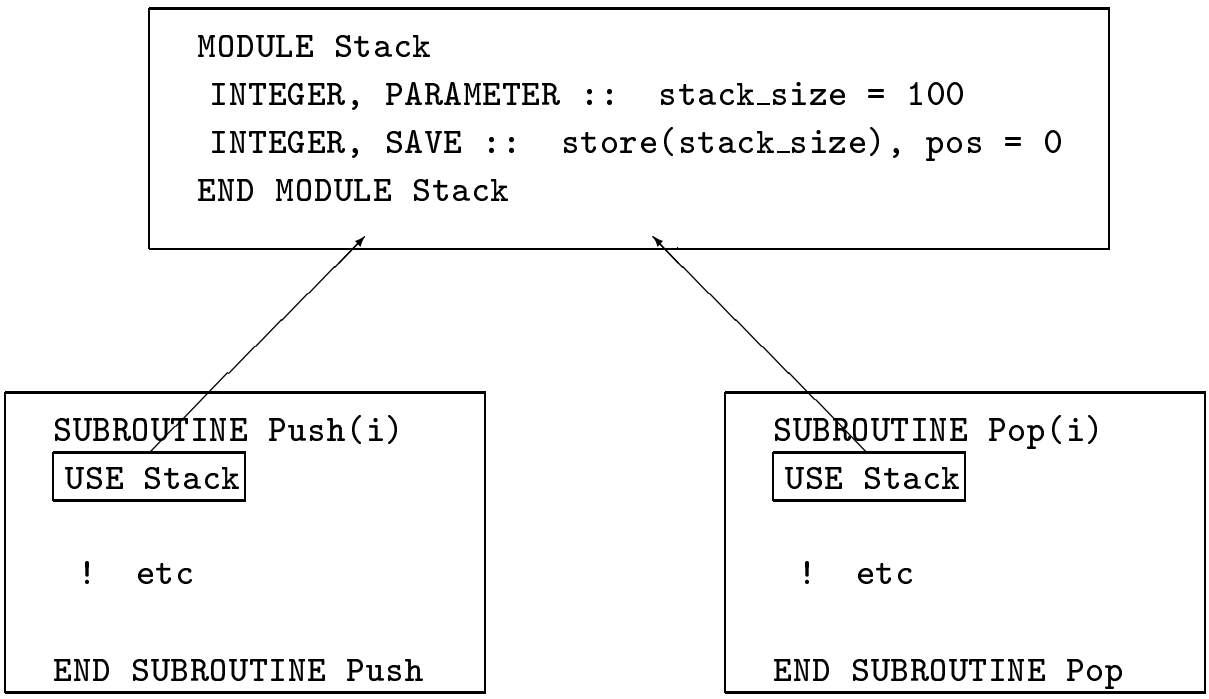
```
MODULE stack
 INTEGER, PARAMETER :: stack_size = 100
 INTEGER, SAVE :: store(stack_size), pos=0
END MODULE stack
```

and two access functions,

```
SUBROUTINE push(i)
 USE stack
 IMPLICIT NONE
  ...
END SUBROUTINE push
SUBROUTINE pop(i)
 USE stack
 IMPLICIT NONE
  ...
END SUBROUTINE pop
```

A main program can now call `push` and `pop` which simulate a 100 element `INTEGER` stack — this is much neater than using `COMMON` block.

Visualisation of Global Storage



Both procedures access the same (global) data in the MODULE.

Modules — Interface Declaration

It is good practice (and often mandatory) to explicitly declare procedure interfaces, however, in a single program there will be:

- a large number of procedures;
- a large amount of duplicated source with great opportunity for text mismatch;

can put *all* interfaces in a `MODULE`, all interfaces are visible when the module is used.

Modules Interface Declaration Example

Consider the following module containing procedure interfaces:

```
MODULE my_interfaces
 INTERFACE
  SUBROUTINE sub1(A,B,C)
   ... ! etc
  END SUBROUTINE sub1
  SUBROUTINE sub2(time,dist)
   ... ! etc
  END SUBROUTINE sub2
 END INTERFACE
END MODULE my_interfaces

PROGRAM use_of_module
 USE my_interfaces
 CALL sub1((/1.0,3.14,0.57/),2,'Yobot')
 CALL sub2(t,d)
END PROGRAM use_of_module
SUBROUTINE sub1(A,B,C)
  ...
END SUBROUTINE sub1
SUBROUTINE sub2(time,dist)
  ...
END SUBROUTINE sub2
```

The module containing the interfaces is used in the main program.

Modules — Procedure Declaration

Placing interfaces in modules for visibility purposes has the following problems,

- procedures may be inter-related and hence call one another;
- the procedure interfaces need to be explicit to one another;
- using the module means that each procedure would contain its *own* interface declaration which is an error.

```
SUBROUTINE Sub1(A,B,C)
 USE my_interfaces ! contains Sub1 stuff
  ...
```

The solution to this is to package the actual procedures in the module; the interfaces become visible and the above problems are solved.

These are now called *module procedures* and are *encapsulated* into the module.

Modules — Procedure Encapsulation

Module procedures are specified after the `CONTAINS` separator,

```
MODULE related_procedures
 IMPLICIT NONE
 ! INTERFACEs of MODULE PROCEDURES do
 ! not need to be specified they are
 ! 'already present'
CONTAINS
 SUBROUTINE sub1(A,B,C)
  ! Can see Sub2's INTERFACE
  ...
 END SUBROUTINE sub1
 SUBROUTINE sub2(time,dist)
  ! Can see Sub1's INTERFACE
  ...
 END SUBROUTINE sub2
END MODULE related_procedures
```

The main program attaches the procedures by *use-association*

```
PROGRAM use_of_module
 USE related_procedures ! includes INTERFACES
 CALL sub1((/1.0,3.14,0.57/),2,'Yobot')
 CALL sub2(t,d)
END PROGRAM use_of_module
```

`sub1` can call `sub2` or vice versa.

Encapsulation - Stack example

We can also encapsulate the `stack` program,

```
MODULE stack
 IMPLICIT NONE
 INTEGER, PARAMETER :: stack_size = 100
 INTEGER, SAVE :: store(stack_size), pos=0
CONTAINS
 SUBROUTINE push(i)
  INTEGER, INTENT(IN) :: i
   ...
 END SUBROUTINE push
 SUBROUTINE pop(i)
  INTEGER, INTENT(OUT) :: i
   ...
 END SUBROUTINE pop
END MODULE stack
```

Any program unit that includes the line:

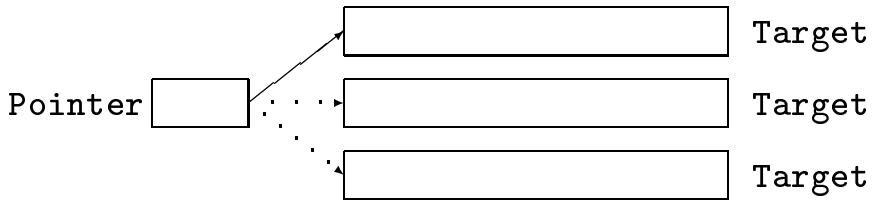
```
USE stack
CALL push(2); CALL push(6); ..
CALL pop(i); ....
```

can access `pop` and `push` therefore use the 100 element global integer stack.

Lecture 7: Pointers and Derived Types

Pointers and Targets

It is often useful to have variables where the space referenced by the variable can be changed as well as the values stored in that space.



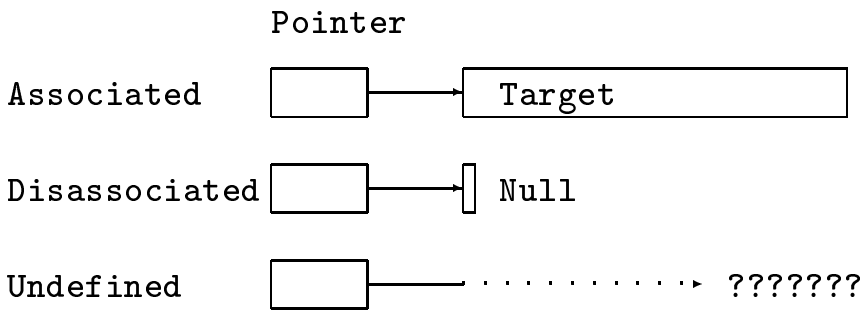
- The pointer often uses less space than the target.
- A reference to the pointer will in general be a reference to the target, (pointers are automatically dereferenced).

Terminology

A pointer has 3 possible states:

- if a pointer has a particular target then the pointer is said to be *associated* with that target,
- a pointer can be made to have no target — the pointer is *disassociated*,
- the initial status of a pointer is *undefined*,

Visualisation,



Use `ASSOCIATED` intrinsic to get the (association) status of a pointer.

Pointer Declaration

A `POINTER`:

- is a variable with the `POINTER` attribute;
- has static type, kind and rank determined by its declaration, for example,

```
REAL, POINTER :: Ptor
REAL, DIMENSION(:,:), POINTER :: Ptoa
```

  - `Ptor` is a pointer to a scalar real target,
  - `Ptoa` is a pointer to a 2-D array of reals.

So,

- the declaration fixes the type, kind and rank of the target;
- pointers to arrays are declared with deferred-shape array specifications;
- the rank of a target is fixed but the shape may vary.

Target Declaration

Targets of a pointer must have the `TARGET` attribute.

```
REAL, TARGET :: x, y
REAL, DIMENSION(5,3), TARGET :: a, b
REAL, DIMENSION(3,5), TARGET :: c
```

With these declarations (and those from the previous slide):

- `x` or `y` may become associated with `Ptor`;
- `a`, `b` or `c` may become associated with `Ptoa`.

Pointer Manipulation

The following operators manipulate pointers:

- `=>`, *pointer assignment* — alias a pointer with a given target;

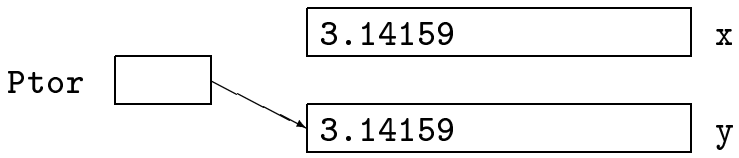
- `=`, *'normal' assignment* — assign a value to the space pointed at by the pointer.

Pointer assignment makes the pointer and the variable reference the same space while the normal assignment alters the value contained in that space.

Pointer Assignment

Consider,

```
x = 3.14159
Ptor => y
Ptor = x
```



- `x` and `Ptor` have the same value.
- `Ptor` is an alias for `y` so the last statement sets `y = 3.14159`.
- if the value of `x` is subsequently changed, the value of `Ptor` and `y` do not.

Coding,

```
Ptor = 5.0
```

sets `y` to `5.0`.

Association with Arrays

An array pointer may be associated a *regular section* of a target of the correct rank (and type and kind). It cannot, however, be associated with a vector subscripted array section.

Assuming the same declarations as the previous slide:

- these are valid (2D sections):

```
Ptoa => a(3:5,::2)
Ptoa => a(1:1,2:2)
```

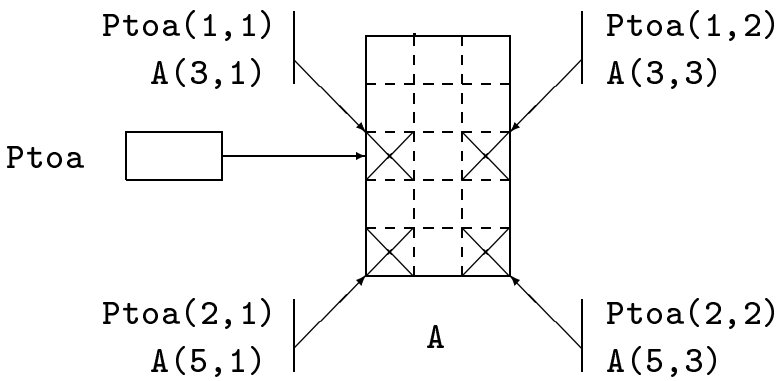
- these are invalid (wrong rank):

```
Ptoa => a(1:1,2)
Ptoa => a(1,2)
Ptoa => a(1,2:2)
```

- this is invalid (vector subscript):

```
v = (/2,3,1,2/)
Ptoa => a(v,v)
```

Visualisation of Pointers to Sections




```
Ptoa => a(3::2,::2)
```

Here the top left subsection element can be referred to through TWO names

- `A(3,1)`
- `Ptoa(1,1)`

Dynamic Targets

Targets can also be created dynamically by allocation. `ALLOCATE` can make space become the target of a pointer.

```
ALLOCATE(Ptor,STAT=ierr)
ALLOCATE(Ptoa(n*n,2*k-1),STAT=ierr)
```

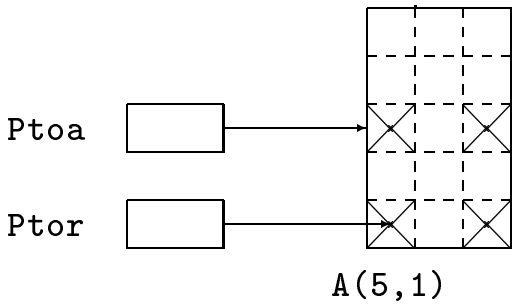
- the first statement allocates a single real as the target of `Ptor`.
- the second allocates a rank 2 real array as the target of `Ptoa`.

It is not an error to allocate an array pointer that is already associated.

Automatic Attributing

Pointer variables implicitly have the `TARGET` attribute.

```
Ptoa => A(3::2,1::2)
Ptor => Ptoa(2,1)
```



Element `(2,1)` of `Ptoa` is associated with `Ptor`.

Here the bottom left subsection element can be referred to through THREE names:

- `Ptor`
- `A(5,1)`
- `Ptoa(2,1)`

When a new association for a pointer is established any previous association with a target is broken.

Pointer Disassociation

Pointers can be disassociated with their targets by:

- nullification

  ```
  NULLIFY(Ptor)
  ```

  - breaks the connection of its pointer argument with its target (if any),
  - disassociates the pointer.

  Note: it is good practise to nullify *all* pointers before use.

- deallocation

  ```
  DEALLOCATE(Ptoa, STAT=ierr)
  ```

  - breaks the connection between the pointer and its target,
  - deallocates the target.

Pointers to Arrays vs. Allocatable Arrays

There are a number of subtle differences between `ALLOCATABLE` and `POINTER` arrays:

- `ALLOCATABLE` arrays are more efficient,
- `TARGET` arrays may be referred to by a number of different names,
- unallocated `ALLOCATABLE` arrays cannot be actual arguments but unassociated (unallocated) `POINTER` arrays can be.

In summary,

- `ALLOCATABLE` arrays are more efficient,
- `POINTER`s are more flexible.

Practical Example

Pointers can be of great use in iterative problems. Iterative methods:

- make guess at required solution;
- use guess as input to an equation to produce better approximation;
- use new approximation to obtain better approximation;
- repeat until degree of accuracy is obtained;

```
REAL, DIMENSION(100,100), TARGET :: app1, app2
REAL, DIMENSION(:,:), POINTER :: prev_app, &
                                 next_app, swap
prev_app => app1
next_app => app2
prev_app = initial_app(.....)
DO
 next_app = iteration_function_of(prev_app)
 IF(ABS(MAXVAL(next_app-prev_app))<0.0001)EXIT
 swap => prev_app
 prev_app => next_app
 next_app => swap
END DO
```

Using pointers here avoids having to copy the large matrices.

Pointers and Procedures

A actual pointer argument can be interpreted in two ways:

- immediately dereference and pass the target — the corresponding dummy argument does **not** have the `POINTER` attribute;

- pass the pointer so it can be manipulated as a pointer in the procedure — the corresponding dummy argument must have the `POINTER` attribute.

For example,

```
INTEGER, POINTER :: Pint1, Pint2
 INTERFACE ! mandatory
  SUBROUTINE Beer(arg1,arg2)
   INTEGER, POINTER :: arg1
   INTEGER, INTENT(IN) :: arg2
  END SUBROUTINE Beer
 END INTERFACE ! mandatory
  ...
 CALL Beer(Pint1,Pint2)
  ...
```

Note: a `POINTER` dummy argument **cannot** have the `INTENT` attribute.

An explicit interface is required if a pointer is used as an actual argument to a procedure.

Copy In / Copy Out

Consider the following code fragment,

```
 INTERFACE
  SUBROUTINE subby(Ptoi,t)
   INTEGER, POINTER :: Ptoi
   INTEGER, TARGET  :: t
  END SUBROUTINE subby
 END INTERFACE
 INTEGER, POINTER :: ptr
 INTEGER, TARGET  :: tgt
 ptr => tgt
 CALL subby(ptr,tgt)
END
SUBROUTINE subby(Ptoi,t)
 INTEGER, POINTER :: Ptoi
 INTEGER, TARGET  :: t
 PRINT*, ASSOCIATED(Ptoi,t)
END SUBROUTINE subby
```

Consider the question, 'What will be the result of the `PRINT` statement?' The standard is unclear whether the association of a pointer and its target is upheld across a procedure boundary.

Do **not** assume that the association is upheld. (The NAg and EPC compiler give different results!)

Pointer Valued Functions

A function may be pointer valued,

```
PROGRAM main
 IMPLICIT NONE
 INTEGER, TARGET :: a, b
 INTEGER, POINTER :: largest
 a = ...; b = ...
 largest => ptr()
 print*, largest
CONTAINS
 FUNCTION ptr()
  INTEGER, POINTER :: ptr
  IF (a .GT. b) THEN
   ptr => a
  ELSE
   ptr => b
  END IF
 END FUNCTION ptr
END PROGRAM main
```

The interface of a pointer valued function must always be explicit.

Pointer I/O

Pointers which appear in input/output lists:

- are always dereferenced;
- must not be disassociated as dereferencing would make no sense;

```
REAL, DIMENSION(3), TARGET :: arr=(/1.,2.,3./)
REAL, DIMENSION(:), POINTER :: p, q
p => arr
PRINT*, p
ALLOCATE(q(5))
READ*,  q
PRINT*, q
DEALLOCATE(q)
PRINT*, q ! invalid, no valid target
END
```

Derived Types

It is often advantageous to express some objects in terms of aggregate structures, for example: coordinates, (x, y, z).

Fortran 90 allows compound entities or *derived types* to be defined:

```
TYPE COORDS_3D
 REAL :: x, y, z
END TYPE COORDS_3D
TYPE(COORDS_3D) :: pt1, pt2
```

Supertypes

Previously defined types can be used as components of other derived types,

```
TYPE SPHERE
 TYPE (COORDS_3D) :: centre
 REAL             :: radius
END TYPE SPHERE
```

Objects of type `SPHERE` can be declared:

```
TYPE (SPHERE) :: bubble, ball
```

Derived Type Assignment

Values can be assigned to derived types in two ways:

- component by component;
- as an object.

An individual component may be selected, using the `%` operator:

```
pt1%x = 1.0
bubble%radius = 3.0
bubble%centre%x = 1.0
```

The whole object may be selected and assigned to using a constructor:

```
pt1 = COORDS_3D(1.,2.,3.)
bubble%centre = COORDS_3D(1.,2.,3.)
bubble = SPHERE(bubble%centre,10.)
bubble = SPHERE(COORDS_3D(1.,2.,3.),10.)
```

The derived type component of `SPHERE` must also be assigned to using a constructor.

Assignment between two objects of the same derived type is intrinsically defined,

```
ball = bubble
```

Arrays and Derived Types

It is possible to define derived type objects which contain non-ALLOCATABLE arrays and arrays of derived type objects.

Consider,

```
TYPE FLOBBLE
 CHARACTER(LEN=6)           :: nom
 INTEGER, DIMENSION(10,10) :: harry
END TYPE FLOBBLE
 ...
TYPE (FLOBBLE)                  :: bill
TYPE (FLOBBLE), DIMENSION(10) :: ben
```

We can refer to an element or subsection of the array component:

```
bill%harry(7,7)
bill%harry(:,::2)
ben(1)%harry(7,7)
ben(9)%harry(:,:)
ben(:)%harry(7,7)
```

but not a collection of elements or subsections of the array component:

```
ben(9:9)%harry(:,:) ! invalid
ben(:)%harry(:,::2) ! invalid
```

Derived Type I/O

Derived type objects which do not contain pointers (or private) components may be input or output using 'normal' methods:

```
PRINT*, bubble
```

is exactly equivalent to

```
PRINT*, bubble%centre%x, bubble%centre%y, &
        bubble%centre%z, bubble%radius
```

Derived types are handled on a component by component basis.

Derived Types and Procedures

Derived types can be used as arguments to procedures, however, textual definitions of a `TYPE` are not sufficient:

```
TYPE vec
 REAL r
 REAL theta
END TYPE vec
TYPE(vec) :: north
CALL subby(north)
 ...
END PROGRAM
SUBROUTINE subby(arg)
 TYPE vec          ! illegal because
  REAL r           ! the two vec types
  REAL theta       ! are different
 END TYPE vec
 TYPE(vec), INTENT(IN) :: arg
  ...
```

is illegal as the two instances of the `vec` type definition are in no way related.

Type definitions can only become accessible by *host* or *use* association.

Association of Type Definition

Given the following:

```
MODULE type_dec
 TYPE vec
  REAL r
  REAL theta
 END TYPE vec
END MODULE type_dec
```

then the next two code fragments are legal:

```
USE type_dec
TYPE (vec) :: north
CALL subby(north)
 ...
SUBROUTINE subby(arg)
 USE type_dec
 TYPE (vec), INTENT(IN) :: arg
 ...
```

and

```
USE type_dec
TYPE (vec) :: natty, dreads
natty = funquie(dreads)
 ...
CONTAINS
 FUNCTION funquie(arg)    ! host assoc
  TYPE (vec), INTENT(IN) :: arg
  TYPE (vec) :: funquie
   ...
```

So long as the type definition is visible, derived type arguments behave like intrinsically typed arguments.

Derived Type Valued Functions

Functions can return results of an arbitrary defined type

```
FUNCTION Poo(kanga, roo)
 USE type_dec
 TYPE (vec) :: Poo
 TYPE (vec), INTENT(IN) :: kanga, roo
 Poo = ...
END FUNCTION Poo
```

An explicit interface must be provided at the call site.

Lecture 8: Modules and Facility Packaging

POINTER Components of Derived Types

- ALLOCATABLE arrays cannot be used as components in a derived type,

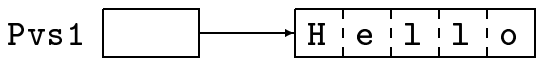
- POINTERs can be,

Dynamically sized structures can be created and manipulated, for example,

```
TYPE VSTRING
 CHARACTER, DIMENSION(:), POINTER :: chars
END TYPE VSTRING
```

this has a component which is a pointer to a 1-D array of characters.

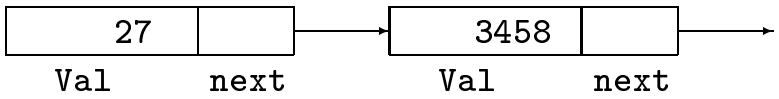
```
TYPE(VSTRING) :: Pvs1
 ...
ALLOCATE(Pvs1%chars(5))
Pvs1%chars = (/"H","e","l","l","o"/)
```



Pointers and Recursive Data Structures

- Derived types which include pointer components provide support for recursive data structures such as linked lists.

```
TYPE CELL
 INTEGER :: val
 TYPE (CELL), POINTER :: next
END TYPE CELL
```



- Assignment between structures containing pointer components is subtlely different to normal,

```
TYPE(CELL) :: A
TYPE(CELL), TARGET :: B
A = B
```

is equivalent to:

```
A%val = B%val
A%next => B%next
```

Practical Example of Linked Lists

The following fragment would create a linked list of cells starting at `head` and terminating with a cell whose `next` pointer is null (disassociated).

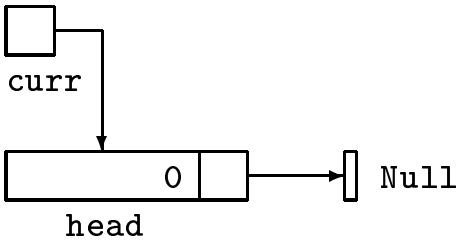
```
TYPE (CELL), TARGET  :: head
TYPE (CELL), POINTER :: curr, temp
INTEGER              :: k
head%val = 0             ! listhead = default
NULLIFY(head%next)       ! un-undefine
curr => head             ! curr head of list
DO
 READ*, k                ! get value of k
 ALLOCATE(temp)          ! create new cell
 temp%val = k            ! assign k to new cell
 NULLIFY(temp%next)      ! set disassociated
 curr%next => temp       ! attach new cell to
                         ! end of list
 curr => temp            ! curr points to new
                         ! end of list
END DO
```

Example (Continued)

The statements,

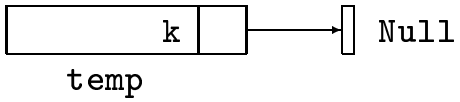
```
head%val = 0; NULLIFY(head%next); curr => head
```

give,



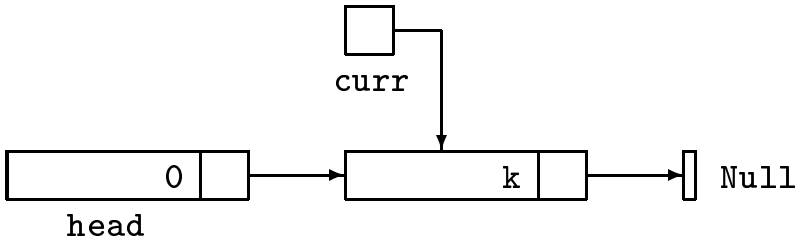

```
ALLOCATE(temp); temp%val = k; NULLIFY(temp%next)
```

give,

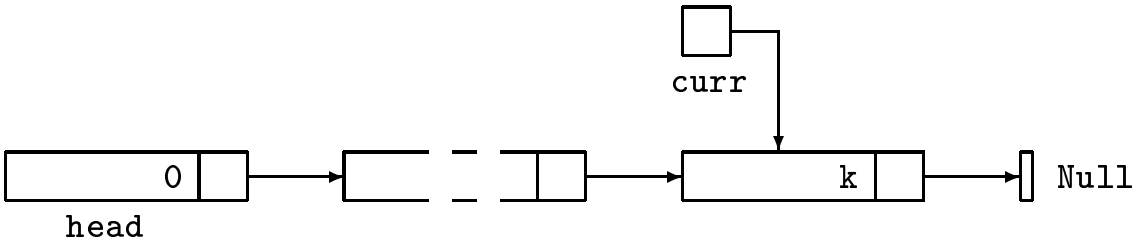



```
curr%next => temp; curr => temp
```

give,



The final list structure is,



Example (Continued)

A "walk-through' the previous linked list could be written as follows:

```
curr => head
DO
 PRINT*, curr%val
 IF(.NOT.ASSOCIATED(curr%next)) EXIT
 curr => curr%next
ENDDO
```

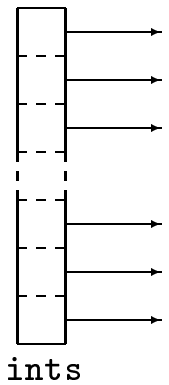
All sorts of multiply linked lists can be created and manipulated in analogous ways.

Arrays of Pointers

It is possible to create what are in effect arrays of pointers:

```
TYPE iPTR
 INTEGER, POINTER :: compon
END TYPE iPTR
TYPE(iPTR), DIMENSION(100) :: ints
```

Visualisation,



cannot refer to a whole array (or sub-array) of pointers,

```
ints(10)%compon ! valid
ints(:)%compon  ! not valid
```

Modules — Type and Procedure Packaging

Derived types are of limited use as no intrinsic functions are defined for them, however,

- procedure arguments can be derived types;
- functions can return results of derived types;
- operators can be overloaded by writing procedures.

So we can write a ‘package’ which contains

- type definitions,
- overloaded intrinsics,
- overload set of operators,
- generic overload set definitions,
- other useful procedures.

This form of bundling is known as ‘encapsulation’. An example is the varying string module which is to be an ancillary standard.

Generic Procedures

Most intrinsics are generic in that their type is determined by their argument(s). For example, `ABS(X)`:

- returns a `REAL` value if `X` is `COMPLEX` (`CABS`) or `REAL` (`ABS`);
- returns a `INTEGER` value if `X` is `INTEGER` (`IABS`).

A user may write his own generic procedures, this is done by specifying a generic interface block:

```
INTERFACE CLEAR
 SUBROUTINE clear_int(a)
  INTEGER, DIMENSION(:), INTENT(INOUT) :: a
 END SUBROUTINE clear_int
 SUBROUTINE clear_real(a)
  REAL, DIMENSION(:), INTENT(INOUT) :: a
 END SUBROUTINE clear_real
END INTERFACE ! CLEAR
```

The *generic name*, `CLEAR`, is associated with *specific* names `clear_int` and `clear_real`.

This set of procedures is known as an *overload set*.

Generic Interfaces Using Module Procedures

- can encapsulate specific procedure definitions and the generic interface specification in the same module,
- all interfaces are thus already visible,
- the overload set is specified by a series of `MODULE PROCEDURE` statements:

```
INTERFACE CLEAR ! generic int
 MODULE PROCEDURE clear_int
 MODULE PROCEDURE clear_real
END INTERFACE ! CLEAR
```

- the specific procedure used is determined by the *number, type, kind* or *rank* of the non-optional arguments,
- the overload set of procedures must be unambiguous with respect to their dummy arguments,
- default intrinsic types *should not* be used in generic interfaces, use parameterised tyoes.

Example

Given,

```
MODULE schmodule
 INTERFACE CLEAR ! generic int
  MODULE PROCEDURE clear_int
  MODULE PROCEDURE clear_real
 END INTERFACE ! CLEAR
CONTAINS
 SUBROUTINE clear_int(a)
  INTEGER,DIMENSION(:),INTENT(INOUT) :: a
   .... ! actual code
 END SUBROUTINE clear_int
 SUBROUTINE clear_real(a)
  REAL,DIMENSION(:),INTENT(INOUT) :: a
  .... ! actual code
 END SUBROUTINE clear_real
END MODULE schmodule

PROGRAM Main
 IMPLICIT NONE
 USE schmodule
 REAL :: prices(100)
 INTEGER :: counts(50)
  CALL CLEAR(prices) ! generic call
  CALL CLEAR(counts) ! generic call
END PROGRAM Main
```

The first procedure invocation would be resolved with `clear_real` and the second with `clear_int`.

Overloading Intrinsic Procedures

When a new type is added, it is a simple process to add a new overload to any relevant intrinsic procedures.

The following extends the LEN_TRIM intrinsic to return the number of letters in the owners name for objects of type HOUSE,

```
MODULE new_house_defs
 IMPLICIT NONE
 TYPE HOUSE
  CHARACTER(LEN=16) :: owner
  INTEGER           :: residents
  REAL              :: value
 END TYPE HOUSE
 INTERFACE LEN_TRIM
  MODULE PROCEDURE owner_len_trim
 END INTERFACE
CONTAINS
 FUNCTION owner_len_trim(ho)
  TYPE(HOUSE), INTENT(IN) :: ho
  INTEGER owner_len_trim
  owner_len_trim = LEN_TRIM(ho%owner)
 END FUNCTION owner_len_trim
  .... ! other encapsulated stuff
END MODULE new_house_defs
```

The user defined procedures are added to the existing generic overload set.

Overloading Operators

Intrinsic operators, such as -, = and *, can be overloaded to apply to all types in a program:

- specify the generic operator symbol in an `INTERFACE OPERATOR` statement,
- specify the overload set in a generic interface,
- declare the `MODULE PROCEDURE`s (`FUNCTION`s) which define how the operations are implemented.

These functions must have one or two non-optional arguments with `INTENT(IN)` which correspond to monadic and dyadic operators.

Overloads are resolved as normal.

Operator Overloading Example

The '*' operator can be extended to apply to the rational number data type as follows:

```
MODULE rational_arithmetic
 TYPE RATNUM
  INTEGER :: num, den
 END TYPE RATNUM
 INTERFACE OPERATOR (*)
  MODULE PROCEDURE rat_rat,int_rat,rat_int
 END INTERFACE
CONTAINS
  FUNCTION rat_rat(l,r)       ! rat * rat
   TYPE(RATNUM), INTENT(IN) :: l,r
    ...
     rat_rat = ...
  FUNCTION int_rat(l,r)       ! int * rat
   INTEGER, INTENT(IN)       :: l
   TYPE(RATNUM), INTENT(IN) :: r
   ...
  FUNCTION rat_int(l,r)       ! rat * int
   TYPE(RATNUM), INTENT(IN) :: l
   INTEGER, INTENT(IN)       :: r
   ...
END MODULE rational_arithmetic
```

The three new procedures are added to the operator overload set allowing them to be used as operators in a normal arithmetic expressions.

Example (Cont'd)

With,

```
USE rational_arithmetic
TYPE (RATNUM) :: ra, rb, rc
```

we could write,

```
rc = rat_rat(int_rat(2,ra),rb)
```

but better:

```
rc = 2*ra*rb
```

Defining New Operators

can define new monadic and dyadic operators. They have the form,

.<*name*>.

Note:

- monadic operators have precedence over dyadic.
- names must be 31 letters (no numbers or underscore) or less.
- basic rules same as for overloading procedures.

Defined Operator Example

For example, consider the following definition of the .TWIDDLE. operator in both monadic and dyadic forms,

```
MODULE twiddle_op
 INTERFACE OPERATOR (.TWIDDLE.)
  MODULE PROCEDURE itwiddle, iitwiddle
 END INTERFACE ! (.TWIDDLE.)
CONTAINS
 FUNCTION itwiddle(i)
  INTEGER itwiddle
  INTEGER, INTENT(IN) :: i
  itwiddle = -i*i
 END FUNCTION
 FUNCTION iitwiddle(i,j)
  INTEGER iitwiddle
  INTEGER, INTENT(IN) :: i,j
  iitwiddle = -i*j
 END FUNCTION
END MODULE
```

The following

```
PROGRAM main
 USE twiddle_op
 print*, 2.TWIDDLE.5, .TWIDDLE.8, &
           .TWIDDLE.(2.TWIDDLE.5), &
           .TWIDDLE.2.TWIDDLE.5
END PROGRAM
```

produces

```
-10 -64 -100 20
```

Precedence

- user defined monadic operators are most tightly binding.
- user defined dyadic operators are least tightly binding.

For example,

```
.MONA.e**j/a.DYAD.b+c.AND.d
```

is equivalent to

```
(((.MONA.e)**j)/a).DYAD.((b+c).AND.d)
```

User-defined Assignment

Assignment between two different user defined types must be explicitly programmed; a `SUBROUTINE` with two arguments specifies what to do,

- the first argument is the result variable and must have `INTENT(OUT)`;
- the second is the expression whose value is converted and must have `INTENT(IN)`.

Overloading the assignment operator differs from other operators:

- assignment overload sets do **not** have to produce an unambiguous set of overloads;
- later overloads override earlier ones if there is an ambiguity;

Defined Assignment Example

Should put in a module,

```
INTERFACE ASSIGNMENT(=)
 MODULE PROCEDURE rat_ass_int, real_ass_rat
END INTERFACE
```

specifiy subroutines in the `CONTAINS` block:

```
SUBROUTINE rat_ass_int(var, exp)
  TYPE (RATNUM), INTENT(OUT) :: var
  INTEGER, INTENT(IN) :: exp
  var%num = exp
  var%den = 1
END SUBROUTINE rat_ass_int
SUBROUTINE real_ass_rat(var, exp)
  REAL, INTENT(OUT) :: var
  TYPE (RATNUM), INTENT(IN) :: exp
  var = REAL(exp%num) / REAL(exp%den)
END SUBROUTINE real_ass_rat
```

Wherever the module is used the following is valid:

```
ra = 50
x = rb*rc
```

for real `x`.

Restricting Visibility

- Objects in a `MODULE` can be given visibility attributes:

```
PRIVATE :: rat_ass_int, real_ass_rat
PRIVATE :: rat_int, int_rat, rat_rat
PUBLIC :: OPRATOR(*)
PUBLIC :: ASSIGNMENT(=)
```

  only allows access to symbolic versions of multiply and assignment (`*` and `=`).

- This allows the internal structure of a module to be changed without modifying the users program.

- default visibility is `PUBLIC`, this can be reversed by a `PRIVATE` statement.

- individual declarations can also be attributed,

```
INTEGER, PRIVATE :: Intern
```

Derived Types with Private Components

The type RATNUM is declared with PRIVATE internal structure,

```
TYPE RATNUM
 PRIVATE
 INTEGER :: num, den
END TYPE RATNUM
```

The user is unable to access specific components,

```
TYPE (RATNUM) :: splodge
 splodge = RATNUM(2,3) ! invalid
 splodge%num = 2       ! invalid
 splodge%den = 3       ! invalid
 splodge = set_up_RATNUM(2,3) ! OK
! set_up_RATNUM must be module procedure
  CALL Print_out_RATNUM(splodge)
! Print_out_RATNUM must be module procedure
```

this allows the internal representation of the type to be changed:

```
TYPE RATNUM
 PRIVATE
 REAL :: numb
END TYPE RATNUM
```

Accessibility Example

We can update our stack example,

```
MODULE stack
 IMPLICIT NONE
 PRIVATE
 INTEGER, PARAMETER :: stack_size = 100
 INTEGER, SAVE :: store(stack_size), pos = 0
 PUBLIC push, pop
CONTAINS
 SUBROUTINE push(i)
  INTEGER, INTENT(IN) :: i
   ... ! as before
 END SUBROUTINE push
 SUBROUTINE pop(i)
  INTEGER, INTENT(OUT) :: i
   ... ! as before
 END SUBROUTINE pop
END MODULE stack
```

User cannot now alter the value of `store` or `pos`.

Another Accessibility Example

The visibility specifiers can be applied to all objects including type definitions, procedures and operators:

For example,

```
MODULE rational_arithmetic
 IMPLICIT NONE
 PUBLIC :: OPERATOR (*)
 PUBLIC :: ASSIGNMENT (=)
 TYPE RATNUM
  PRIVATE
  INTEGER :: num, den
 END TYPE RATNUM
 TYPE, PRIVATE :: INTERNAL
  INTEGER lhs, rhs
 END TYPE INTERNAL
 INTERFACE OPERATOR (*)
  MODULE PROCEDURE rat_rat,int_rat,rat_int
 END INTERFACE ! OPERATOR (*)
 PRIVATE rat_rat, int_rat, rat_int
   ... ! and so on
```

The type `INTERNAL` is only accessible from within the module.

The USE Renames Facility

The USE statement names a module whose public definitions are to be made accessible.

Syntax:

USE < *module-name* > &
[,< *new-name* > => < *use-name* >...]

module entities can be renamed,

```
USE HOUSE_DEFS, GET_HOME => GET_HOUSE
```

The module object GET_HOUSE is renamed to GET_HOME when used locally.

`USE ONLY` Statement

Another way to avoid name clashes is to only use those objects which are necessary. It has the following form:

`USE` < *module-name* > [`ONLY:`< *only*-list >...]

The < *only*-list > can also contain renames (`=>`).

For example,

```
USE HOUSE_DEF, ONLY:HOME => HOUSE, &
        GET_HOME => GET_HOUSE
```

Only `HOME` and `GET_HOME` are made accessible.

The `ONLY` statement gives the compiler the option of including only those entities specifically named.

Semantic Extension Modules

The real power of the `MODULE` / `USE` facilities appears when coupled with derived types and operator and procedure overloading to provide *semantic extensions* to the language.

Semantic extension modules require:

- a mechanism for defining new types;
- a method for defining operations on those types;
- a method of overloading the operations so user can use them in a natural way;
- a way of encapsulating all these features in such a way that the user can access them as a combined set;
- details of underlying data representation in the implementation of the associated operations to be kept hidden (desirable).

This is an Object Oriented approach.

Lecture 9: Parametrised Intrinsic Types Plus

Complex Data

This data type has the same precision as default `REAL`.

- `COMPLEX` object declaration:

```
COMPLEX :: z, j, za(1:100)
```

- symbolic constants are expressed in the same way:

```
COMPLEX, PARAMETER :: i = (0.0,1.0)
```

- complex constants are represented as co-ordinate pairs: `(1.0,1.0)` or `(3.141,1.0E-9)`.

- complex values can be constructed using the `CMPLX` function,

```
z = CMPLX(x,y)
```

- complex expressions can be used in the same way as other types

```
REAL :: x; COMPLEX :: a, b, c,
 ...
a = x*((b+c)*CMPLX(0.1,-0.1))
b = 1
```

  The real value `x` will be promoted to the complex value `CMPLX(x,0)`. `b` will be set to `CMPLX(1.0,0)`.

Complex Intrinsic Functions

`AIMAG(z)`	Imaginary part of a complex number
`REAL(z)`	Real part of a complex number
`CONJG(z)`	Conjugate of a complex number
`ABS(z)`	Absolute value of a complex number
`SIN(z)` etc	All appropriate mathematical functions

Parameterised Data Types

- Fortran 77 had a problem with numeric portability, the precision (and exponent range) between processors could differ,

- Fortran 90 implements a portable precision selecting mechanism,

- intrinsic types can be parameterised by a kind value (an integer). For example,

```
INTEGER(KIND=1) :: ik1
REAL(4) :: rk4
```

- the kind parameters correspond to differing precisions supported by the compiler (details in the compiler manual).

- objects of different kinds can be mixed in arithmetic expressions but procedure arguments must match in type **and** kind.

Integer Data Type by Kind

- selecting kind, by an explicit integer is still **not** portable,

- must use the `SELECTED_INT_KIND` intrinsic function. For example, `SELECTED_INT_KIND(2)` returns a kind number capable of expressing numbers in the range, $(-10^2, 10^2)$.

- here the argument specifies the minimum decimal exponent range for the desired model. For example,

```
INTEGER :: short, medium, long, vlong
PARAMETER (short = SELECTED_INT_KIND(2), &
           medium= SELECTED_INT_KIND(4), &
           long  = SELECTED_INT_KIND(10),&
           vlong = SELECTED_INT_KIND(100))
INTEGER(short)    :: a,b,c
INTEGER(medium)   :: d,e,f
INTEGER(long)     :: g,h,i
```

Real KIND Selection

Similar principle to INTEGER:

- SELECTED_REAL_KIND(8,9) will support numbers with a precision of 8 digits and decimal exponent range of 9. For example,

```
INTEGER, PARAMETER  ::
     r1 = SELECTED_REAL_KIND(5,20),  &
     r2 = SELECTED_REAL_KIND(10,40)
REAL(KIND=r1)       :: x, y, z
REAL(r2), PARAMETER :: diff = 100.0_r2
```

- COMPLEX variables are specified in the same way,

```
COMPLEX(KIND=r1) :: cinema
COMPLEX(r2) :: inferiority = &
           (100.0_r2,99.0_r2)
```

  Both parts of the complex number have the same numeric range.

Kind Functions

- it is often useful to be able to interrogate an object to see what kind parameter it has.

- `KIND` returns the integer which corresponds to the kind of the argument.

- for example, `KIND(a)` will return the integer parameter which corresponds to the kind of `a`. `KIND(20)` returns the kind value of the default integer type.

- the intrinsic type conversion functions have an optional argument to specify the kind of the result, for example,

```
print*, INT(1.0,KIND=3), NINT(1.0,KIND=3)
x = x + REAL(j,KIND(x))
```

Mixed Kind Expression Evaluation

Mixed kind expressions:

- If all operands of an expression have the same type and kind, then the result also has this type and kind.

- If the kinds are different, then operands with lower range are promoted before operations are performed. For example, if

```
INTEGER(short) :: members, attendees
INTEGER(long)  :: salaries, costs
```

  the expression:

  - `members + attendees` is of kind `short`,
  - `salaries - costs` is of kind `long`,
  - `members * costs` is also of kind `long`.

- Care must be taken to ensure the LHS is able to hold numbers returned by the RHS.

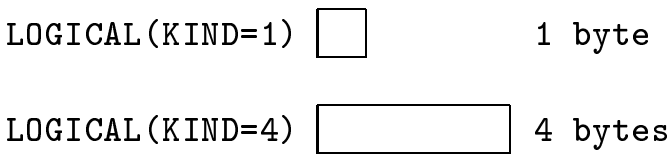
Logical KIND Selection

- There is no SELECTED_LOGICAL_KIND intrinsic, however, the KIND intrinsic can be used as normal.

  For example,

```
LOGICAL(KIND=4) :: yorn = .TRUE._4
LOGICAL(KIND=1), DIMENSION(10) :: mask
IF (yorn .EQ. LOGICAL(mask(1),KIND(yorn)))...
```

- KIND=1 may only use one byte of store per variable,



- Must refer to the compiler manual.

Character KIND Selection

- Every compiler must support at least one character set which must include all the Fortran characters. A compiler may also support other character sets:

```
INTEGER, PARAMETER :: greek = 1
CHARACTER(KIND=greek) :: zeus, athena
CHARACTER(KIND=2,LEN=25) :: mohammed
```

- Normal operations apply individually but characters of different kinds cannot be mixed. For example,

```
print*, zeus//athena   ! OK
print*, mohammed//athena ! illegal
print*, CHAR(ICHAR(zeus),greek)
```

  Note CHAR gives the character in the given position in the collating sequence.

- Literals can also be specified:

  greek_"$\alpha\delta\alpha\mu$"

  Notice how the kind is specified first.

Kinds and Procedure Arguments

Dummy and actual arguments must match exactly in kind, type and rank, consider,

```
SUBROUTINE subbie(a,b,c)
 USE kind_defs
 IMPLICIT NONE
 REAL(r2), INTENT(IN)  :: a, c
 REAL(r1), INTENT(OUT) :: b
  ...
```

an invocation of `subbie` must have matching arguments, for example,

```
 USE kind_defs
 IMPLICIT NONE
 REAL(r1) :: arg2
 REAL(r2) :: arg3
  ...
 CALL subbie(1.0_r2, arg2, arg3)
```

Using `1.0` instead of `1.0_r2` will not be correct on every compiler.

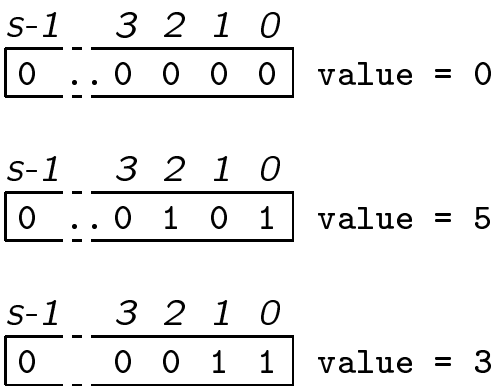
This is very important with generics.

Bit Manipulation Intrinsic Functions

Summary,

`BTEST(i,pos)`	bit testing
`IAND(i,j)`	AND
`IBCLR(i,pos)`	clear bit
`IBITS(i,pos,len)`	bit extraction
`IBSET(i,pos)`	set bit
`IEOR(i,j)`	exclusive OR
`IOR(i,j)`	inclusive OR
`ISHFT(i,shft)`	logical shift
`ISHFTC(i,shft)`	circular shift
`NOT(i)`	complement
`MVBITS(ifr,ifrpos, len,ito,itopos)`	move bits (`SUBROUTINE`)

Variables used as bit arguments must be `INTEGER` valued. The model for bit representation is that of an unsigned integer, for example,



The number of bits in a single variable depends on the compiler

Array Construction Intrinsics

There are four intrinsics in this class:

- `MERGE(TSOURCE,FSOURCE,MASK)`— merge two arrays under a mask,
- `SPREAD(SOURCE,DIM,NCOPIES)`— replicates an array by adding `NCOPIES` of a dimension,
- `PACK(SOURCE,MASK[,VECTOR])`— pack array into a one-dimensional array under a mask.
- `UNPACK(VECTOR,MASK,FIELD)`— unpack a vector into an array under a mask.

`MERGE` Intrinsic

`MERGE(TSOURCE,FSOURCE,MASK)`— merge two arrays under mask control. `TSOURCE`, `FSOURCE` and `MASK` must all conform and the result is `TSOURCE` where `MASK` is `.TRUE.` and `FSOURCE` where it is `.FALSE.`.

If,

$$\texttt{MASK} = \begin{pmatrix} T & T & F \\ F & F & T \end{pmatrix}$$

and

$$\texttt{TSOURCE} = \begin{pmatrix} 1 & 5 & 9 \\ 3 & 7 & 11 \end{pmatrix}$$

and

$$\texttt{FSOURCE} = \begin{pmatrix} 0 & 4 & 8 \\ 2 & 6 & 10 \end{pmatrix}$$

we find

$$\texttt{MERGE(TSOURCE, FSOURCE, MASK)} = \begin{pmatrix} \boxed{1} & \boxed{5} & 8 \\ 2 & 6 & \boxed{11} \end{pmatrix}$$

SPREAD Intrinsic

SPREAD(SOURCE,DIM,NCOPIES)— replicates an array by adding NCOPIES of in the direction of a stated dimension.

If A is (/5, 7/), then

$$\texttt{SPREAD}(\texttt{A}, 2, 4) = \begin{pmatrix} 5 & 5 & 5 & 5 \\ 7 & 7 & 7 & 7 \end{pmatrix}$$

and

$$\texttt{SPREAD}(\texttt{A}, 1, 4) = \begin{pmatrix} 5 & 7 \\ 5 & 7 \\ 5 & 7 \\ 5 & 7 \end{pmatrix}$$

PACK Intrinsic

PACK(SOURCE,MASK[,VECTOR])— pack a arbitrary shaped array into a one-dimensional array under a mask. VECTOR, if present, must be 1-D and must be of same type and kind as SOURCE.

If

$$\texttt{MASK} = \begin{pmatrix} T & T & F \\ F & F & T \end{pmatrix}$$

and

$$\texttt{A} = \begin{pmatrix} \boxed{1} & \boxed{5} & 9 \\ 3 & 7 & \boxed{11} \end{pmatrix}$$

then

- PACK(A,MASK) is (/1, 5, 11/);
- PACK(A,MASK,(/3,4,5,6/)) is (/1, 5, 11, 6/).
- PACK(A,.TRUE.,(/1,2,3,4,5,6,7,8,9/)) is (/1,3,5,7,9,11,7,8,9/).

UNPACK Intrinsic

UNPACK(VECTOR,MASK,FIELD)— unpack a vector into an array under a mask. FIELD, must conform to MASK and and must be of same type and kind as VECTOR. The result is the same shape as MASK.

If

$$\texttt{FIELD} = \begin{pmatrix} 9 & 5 & 1 \\ 7 & 7 & 3 \end{pmatrix}$$

and

$$\texttt{MASK} = \begin{pmatrix} T & T & F \\ F & F & T \end{pmatrix}$$

then

$$\texttt{UNPACK}((/6,5,4/),\texttt{MASK},\texttt{FIELD}) = \begin{pmatrix} \boxed{6} & \boxed{5} & 1 \\ 7 & 7 & \boxed{4} \end{pmatrix}$$

and

$$\texttt{UNPACK}((/3,2,1/),.\texttt{NOT},\texttt{MASK},\texttt{FIELD}) = \begin{pmatrix} 9 & 5 & \boxed{1} \\ \boxed{3} & \boxed{2} & 3 \end{pmatrix}$$

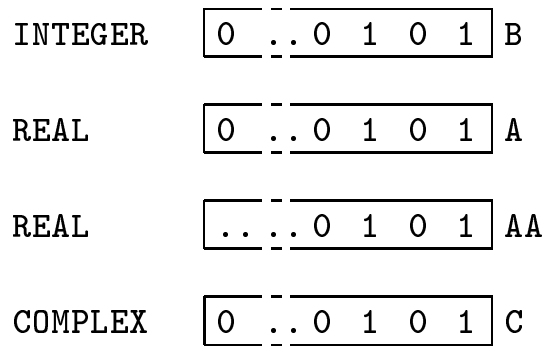
TRANSFER Intrinsic

TRANSFER converts (not coerces) physical representation between data types; it is a retyping facility. Syntax:

TRANSFER(SOURCE,MOLD)

- SOURCE is the object to be retyped,
- MOLD is an object of the target type.

```
REAL A(10), AA(10)
INTEGER B(20)
COMPLEX C(5)
 ...
A  = TRANSFER(B, (/ 0.0 /))
AA = TRANSFER(B, 0.0)
C  = TRANSFER(B, (/ (0.0,0.0) /))
 ...
```



Lecture 10: Odds and Ends

Input / Output

Fortran 90 has a wealth of I/O, too much to cover here.

Fortran 90 allows a number of different streams (files) to be connected to a program for both reading and writing.

In Fortran 90 a file is connected to a *logical unit* denoted by a number. Each unit can have many properties, for example,

- file — the name of the file connected to the unit,
- action — read, write, read and write, etc.
- status — old, new, replace, etc.
- access method — sequential, direct,

`OPEN` Statement

The syntax is,

```
OPEN([UNIT=]< integer >,&
       FILE=< filename >, ERR=< label >, &
       STATUS=< status >, ACCESS=< method >,&
       ACTION=< mode >, RECL=< int-expr >)
```

where,

- < *filename* > is a string,
- < *status* > is `'OLD'`, `'NEW'`, `'REPLACE'`, `'SCRATCH'` or `'UNKNOWN'`,
- < *method* > is `'DIRECT'` or `'SEQUENTIAL'`
- < *mode* > is `'READ'`, `'WRITE'` or `'READWRITE'`
- if the file is direct access the `RECL` must be specified,

For example,

```
OPEN(17,FILE='output.dat',ERR=10, &
    STATUS='REPLACE', &
    ACCESS='SEQUENTIAL',ACTION='WRITE')
OPEN(14,FILE='input.dat',ERR=10, &
    STATUS='OLD', RECL=iexp, &
    ACCESS='DIRECT',ACTION='READ')
```

`READ` Statement

Not all the specifiers can be used at the same time,

`READ([UNIT=]`< *unit* >`, [FMT=]`< *format* >`, IOSTAT= &`
`        `< *int-variable* >`, ERR=`< *label* >`, END=`< *label* >`, &`
`        EOR=`< *label* >`, ADVANCE=`< *advance-mode* >`, &`
`        REC=`< *int-expr* >`, SIZE=`< *num-chars* >`)` < *output-list* >

where

- < *unit* > is a number or `*`.
- < *format* > is a string or a `FORMAT` statement label.
- < *int-variable* > holds a return code, zero means no error.
- < *label* > is an executable statement label.
- < *advance-mode* > is `'YES'` or `'NO'`.
- < *num-chars* > is the number of characters read.
- < *int-expr* > is a record number (for direct access).

For example

```
READ(14,FMT='(3(F10.7,1x))',REC=iexp) a,b,c
READ(*,'(A)',ADVANCE='NO',EOR=12,SIZE=nch) str
```

`WRITE` Statement

Can interchange `READ` and `WRITE` in the following. Not all the specifiers can be used at the same time,

`WRITE(`[`UNIT=`]< *unit* >, [`FMT=`]< *format* >, `&`
`IOSTAT=`< *int-variable* >, `ERR=`< *label* >, `&`
`ADVANCE=`< *advance-mode* >, `&`
`REC=`< *int-expr* >) < *output-list* >

where

- < *unit* > is a number or `*`,
- < *format* > is a string or a `FORMAT` statement label,
- < *int-variable* > holds a return code, zero means no error,
- < *label* > is an executable statement label,
- < *advance-mode* > is `'YES'` or `'NO'`,
- < *int-expr* > is a record number (for direct access).

For example

```
WRITE(17,FMT='(I4)',IOSTAT=istat,ERR=10) ival
WRITE(*,'(A)',ADVANCE='NO') 'Yello'
```

FORMAT Statement / FMT= Specifier

FMT= can specify either a line number of a FORMAT statement, an actual format string or a *.

Fortran 90 has a rich formatting syntax, only the highlights are given here.

An example,

```
    WRITE(17,FMT=&
     '(2X,2I4,1X,''name '',A7)')i,j,str
    READ(14,*) x,y
    WRITE(*,FMT=10) a,b
 10 FORMAT('vals',2(F15.6,2X))
```

The data is formatted using edit descriptors.

The following is written,

```
    11-195 name Philip
vals      -1.051330    333356.000033
```

Edit Descriptors

Summary,

I*w*	*w* chars of integer data,
F*w.d*	*w* chars of real data (*d* dec. pl.),
E*w.d*	*w* chars of real data (*d* dec. pl.),
L*w*	*w* chars of logical data,
A[*w*]	*w* chars of CHARACTER data,
*n*X	skip *n* chars (*n* spaces),

For example,

```
WRITE(*,FMT='(2X,2(I4,1X),''name '',&
                A4,F13.5,1X,E13.5)') &
 77778,3,'abcdefghi',14.45,14.5666666
```

gives

```
****    3 name abcd     14.45000   0.14567E+02
```

Here 77778 will not fit into 4 spaces

Other I/O Statements

- `CLOSE` — unattaches the unit number specified in the statement.
- `REWIND` — puts the file pointer back to the start of the file,
- `BACKSPACE` — the file pointer is moved back one record.
- `ENDFILE` — forces an end-of-file to be written into the file.

The above statements have other specifiers such as `IOSTAT`,

For example,

```
REWIND (UNIT=14)
BACKSPACE (UNIT=17)
ENDFILE (17)
CLOSE (17, IOSTAT=ival)
```

The DATA Statement

The DATA statement is good for initialising odd shaped sections of arrays.

Syntax,

DATA < *var1*-list >/< *data1*-list >/,&
...< *varn*-list >/< *datan*-list >/

The number of constants in each < *data*-list > must be equal to the number of variables / array elements in the corresponding < *var*-list >.

Any object initialised by the DATA statement has the SAVE attribute

`DATA` Statement Example

As an example, consider initialising a 1000×1000 array with all the edge values equal to `1` and with the rest of the array zero. This is not as simple to do with an initialisation statement as it is with a `DATA` statement:

```
REAL :: matrix(100,100)
DATA matrix(1,    1:100) /100*1.0 /!top row
DATA matrix(100,  1:100) /100*1.0 /!bot row
DATA matrix(2:99, 1)     /98*1.0  /!left col
DATA matrix(2:99, 100)   /98*1.0  /!right col
DATA matrix(2:99, 2:99)  /9604*0.0/!interior
```

The expression `100*1.0` means "100 occurrences of 1.0", the `*` is the repetition specifier. In this context it cannot be confused with the multiplication operator because such operators are not allowed in a `DATA` statement.

Data Statement — Implied `DO` Loop

In a `DATA` statement the < *var*-list > may be specified by means of an implied-`DO`.

Initialising a matrix to have a given constant value, say, `5.0` on the diagonal and zero everywhere else is simple to do using this method.

The object section is specified by a tight loop which is more expressive than array syntax would allow:

```
REAL :: diag(100,100)
DATA (diag(i,i), i=1,100) / 100*5.0 /
          ! sets diagonal elements
DATA ((diag(i,j),diag(j,i),&
      j=i+1,100),i=1,100)/ 9900*0.0 /
! sets the upper and lower triangles
```

`GOTO` Statement

The `GOTO` statement:

- is a powerful but undisciplined branching statement;
- can be used to create jumps to almost anywhere in a program unit;
- can be dangerous;
- can lead to unstructured code (logical spaghetti).
- can be very useful!

The basic syntax is

`GOTO` < *numeric-label* >

The label must exist, be in the same scoping unit as the statement and be executable.

GOTO Statement Example

Consider the following example of an atrocious use of the GOTO statement,

```
    GOTO 10   ! jump forward
 23 CONTINUE
    i = i - 1
    IF (i .eq. 0) GOTO 99
 10 PRINT*, "Line 10"
 69 j = j - 1 ! loop
     ...
    IF (j .ne. 0) GOTO 69
    GOTO 23   ! jump back
099 CONTINUE
```

The code fragment demonstrates forward and backward transfer of control and the simulation of a loop.

The best use of GOTO statements is in jumping out of a heavily nested structure when an unexpected event occurs such as a potential divide by zero.

RETURN and STOP

Can be used to program exceptions in procedures.

For example,

```
SUBROUTINE sub(ierror)
 INTEGER, INTENT(OUT) :: ierror
 ...
 ALLOCATE(A(100),STAT=ierror)
 IF (ierror>0) THEN
  PRINT*, 'memory fault'
  RETURN
 END IF
     ...
END SUBROUTINE
```

STOP could be used instead of RETURN:

```
STOP 'stopped in sub'
```

the string is optional or can be a literal integer constant of up to 5 digits. It is output upon execution of STOP at which time the program finishes.

Fortran 95

Fortran 95 will be the new Fortran Standard.

- `FORALL` statement and construct

```
FORALL(i=1:n:2,j=1:m:2)
 A(i,j) = i*j
END FORALL
```

- nested `WHERE` constructs,
- `ELEMENTAL` and `PURE` procedures,
- user-defined functions in initialisation expressions,
- automatic deallocation of arrays,
- improved object initialisation,
- remove conflicts with IEC 559 (IEEE 754/854) (floating point arithmetic),
- deleted features, for example, `PAUSE`, assigned `GOTO`, `cH` edit descriptor,
- more obsolescent features, for example, fixed source form, assumed sized arrays, `CHARACTER*`$<$ *len* $>$ declarations, statement functions,
- language tidy-ups and ambiguities (mistakes),

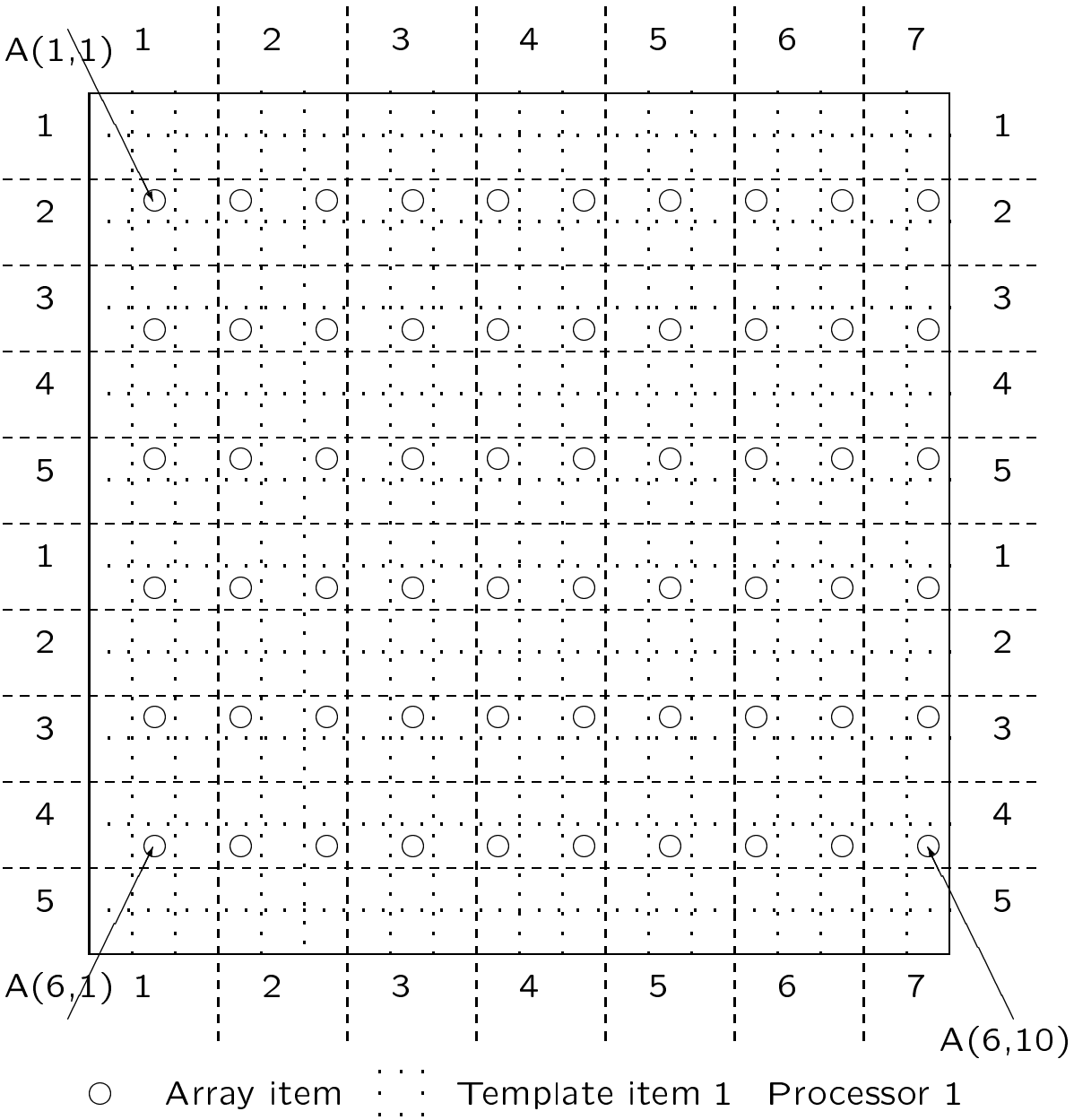
High Performance Fortran

High Performance Fortran (or HPF) is an ad-hoc standard based on Fortran 90. It contains

- Fortran 90,
- syntax extensions, `FORALL`, new intrinsics, `PURE` and `ELEMENTAL` procedures,
- discussion regarding storage and sequence association,
- compiler directives:

```
!HPF$ PROCESSORS P(5,7)
!HPF$ TEMPLATE T(20,20)
      INTEGER A(6,10)
!HPF$ ALIGN A(J,K) WITH T(J*3,K*2)
!HPF$ DISTRIBUTE T(CYCLIC(2),BLOCK(3)) ONTO P
```

Data Alignment



The End